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The following contributions have been accepted for publication and will appear in 1978/79:

PETER BADER

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