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ERRATA

VOLUME 34

Page 733, column 2, lines 17–24. The two entries in the index should appear as only a single entry.

VOLUME 36

Page 162, line 26. For «then {2}», read «then $\Theta\{2\}$ ».

Page 674, line 15 from below. For «*Méthodes*», read «*Méthode*».

Page 790, column 1, lines 24–27, 29, 31, 33. For «XXXVI 515», read «XXXVI 516».

VOLUME 37

Page 191, line 25. Insert *f* at the beginning of the line.

Page 209, line 16 from below. For «*circuites*», read «*circuits*».

Page 219, lines 1–2. For «*Elenco cronologico delle pubblicazioni di L. Campedelli e A. Barlotti*», read «*Elenco cronologico delle pubblicazioni (of Enriques)*».

Page 220, line 1. For «SYDNEY E. HOOPER», read «P. L. HEATH».

Page 220, line 2. For «257», read «254».

Page 223, line 9 from below. For «*Erkenntnistheorie*», read «*Erkenntnistheorie*».

Page 401, line 8 from below. For « $\{x_1\}$ », read « $\{x_i\}$ ».

VOLUME 38

Page 330, line 26. For «356», read «346».

Page 330, line 29. For «356», read «346».

Page 330, line 32. For «356», read «346».

Page 331, line 2 from below. For «XXXV 138(1)», read «XXXV 138(2)».

Page 338, line 10. For «357», read «347».

Page 344, line 1. For «A reprint», read «Russian translation».

Page 344, line 5. For «354», read «344», five times.

Page 346, line 22. For «330», read «320».

Page 346, line 40. For «340», read «330».

Page 346, line 43. For «340», read «330».

Page 346, line 46. For «340», read «330».

Page 347, line 2. For «348», read «338».

Page 537, line 5. For «XXXVIII 536», read «XXXVIII 537».

Page 546, last line, and page 547, lines 4, 10 and 13. For «Lewis», read «Lewy».

Page 547, lines 1 and 11. For «Lewis system», read «system Lewy».

Page 725, column 1. Between lines 3 and 4, insert «HEATH, P. L.: Review of Katsoff (XXXVII 220)».

Page 726, column 1. Delete lines 1 and 2.

Page 727, column 2, line 21. For «Review by Hooper», read «Review by Heath».

Page 735, column 1, lines 12–13. Read «Simplification des schémas par introduction de contacts à plusieurs positions».

Page 740, column 2, line 21. For «(XXXVI 530(4))», read «(XXXIV 530(4))».

Roman numeral page iv, between lines 6 and 7 from below. Insert: «Notice of the new journal *Historia Mathematica*. . . 670».