

Responses of various-sized alpine glaciers and runoff to climatic change

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ABSTRACT. This paper presents a glacier ice-flow model that simulates changes to alpine glaciers of various sizes and their runoff response to climate change in the Yili river basin in the Tien Shan mountains, northwestern China. It is suggested that the sensitivity of glaciers to climatic change is determined by glacier size. The change in glacial runoff does not keep pace with climatic change. As climate warms and glaciers retreat, the glacier runoff tends to increase and then decrease. The runoff peak and its timing depend not only on glacier size but also on the rate of air-temperature rise.

1. INTRODUCTION

At present, the glaciers that have been studied for mass balance are not only few in number but also rather small. Vilesov (1969) and Kotlyakov and others (1991) estimated the changes to glaciers and their runoffs in central Asia using mass-balance data from several small glaciers in the Tien Shan mountains, China. However, the derived changes may not represent the actual changes to larger glaciers. Other investigators (e.g. Oerlemans, 1997; Schmeits and Oerlemans, 1997; Zuo and Oerlemans, 1997; Wallinga and Van de Wal, 1998) have used ice-flow models to study the responses and sensitivities to climatic change of a series of specific glaciers. It is not practical, however, to simulate each glacier individually where there are a large number of glaciers in the same region. Moreover, there is significant variation in the way glaciers respond to climate change, not only over time but also in quantitatively, due to their different sizes and shapes (Wang, 1991; Ding and Haerberli, 1996; Liu Chaohai and others, 1996). The objective of this paper is to simulate the response to climatic warming of various-sized glaciers in the Yili river basin using a glacier ice-flow model, and thus to reveal the impact of climatic change on glaciers of different sizes.

2. THE YILI RIVER BASIN

The Yili river originates in the western Tien Shan, China (42°14'–44°51' N, 80°15'–86°56' E), then flows through the Yili region of Xinjiang Uigur Autonomous Region and finally discharges into Barkshen lake in Kazakstan (Fig. 1).

The Yili river basin consists of a series of valleys and sub-basins that are separated by several mountain ranges, oriented approximately east–west. According to data from the glacier inventory of China and the former Soviet Union (Vilesov, 1969; Ding and others, 1986), 2414 glaciers with a total area of 2113 km² exist in the upper basin. These are at elevations of 2640–5568 m, with the mean snowline at about 3730 m a.s.l., and the mean annual lower boundary of permafrost at approximately 3000 m a.s.l.

3. GLACIER ICE-FLOW MODEL

The introduced glacier ice-flow model comes from Oerlemans' main glacial flowline model (Oerlemans, 1988) and considers the features and shapes of glaciers as described by Schmeits and Oerlemans (1997). The model consists of

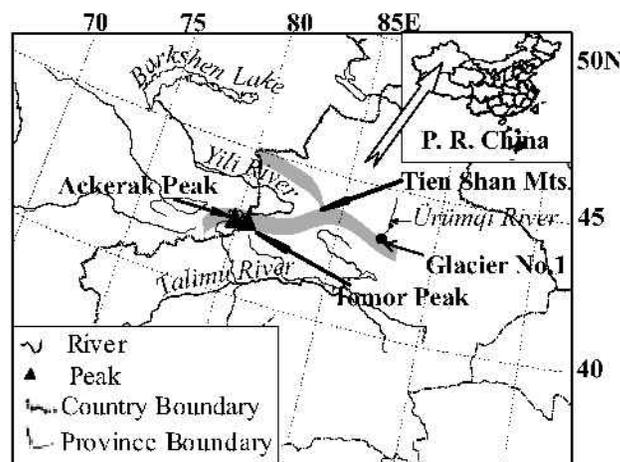


Fig. 1. Location map showing the Yili river basin and Ürümqi glacier No. 1 in the headwaters of the Ürümqi river, Tien Shan.

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glacier-continuity and glacier-flow equations with the main flowline being the x coordinate.

$$\frac{\partial S}{\partial t} = \frac{\partial}{\partial x}(US) + BW \quad (1)$$

$$U = U_d + U_s = f_1 H \tau_d^3 + \frac{f_2 \tau_d^3}{\rho g H} \quad (2)$$

$$\tau_d = -\rho g H \sin \alpha \quad (3)$$

$$S = (W - \tan(\gamma)H)H, \quad (4)$$

where S is the area of the cross-section, B the specific surface mass balance, W the width of the ice surface, U the depth-averaged ice velocity, U_d the velocity caused by internal deformation, U_s the velocity caused by sliding, τ_d the shear stress at the bottom, H the glacier thickness, α the slope of the ice surface along the flowline, γ the slope angle on the sides of the valley (γ is assumed to be 45°), f_1 the glacier-flow parameter, f_2 the ice-sliding shape parameter, and g and ρ the acceleration of gravity and density of ice, respectively ($g = 9.8 \text{ m s}^{-2}$, $\rho = 900 \text{ kg m}^{-3}$).

As the glaciers in the Tien Shan are categorized as sub-polar and polar types, their movement, except for some very large valley glaciers, is mainly attributed to glacier ice deformation (Huang, 1995). Therefore, the ice deformation should be taken into account in the glacier flow equation (Ye and Chen, 1997), and the glacier sliding item U_s in Equation (3) can be omitted. Thus, Equation (3) is modified to:

$$U = f_1 H \tau_d^3. \quad (5)$$

In this model, the effect of climatic change on glaciers is expressed as changes of glacier mass balance. Although climatic change may also alter glacier temperature, and thus lead to glacier change, this process is ignored in this study because of its complexity and the relatively small magnitudes of the glacier changes that result.

Substituting the expressions for U and S in Equation (1) leads to a non-linear diffusion equation for H . A forward time-differencing scheme is used, which is stable if the time-step is sufficiently small (Oerlemans, 1997). Tests have been done on grids with spacing of 500, 300, 100 and 50 m with a time-step of 30 days in this study. The scheme is stable for small glaciers (map area $S_g < 0.5 \text{ km}^2$) with 100 m grid spacing, and for large glaciers ($S_g > 40 \text{ km}^2$) with 300 m spacing.

3.1. Characteristic values of glacier shapes

In order to parameterize the shapes of glaciers of various sizes, some characteristic values, such as glacier area, length, altitude difference (between the maximum and minimum elevation of a glacier), maximum elevation and average slope, were statistically analyzed for more than 2000 glaciers in the Yili river basin, based on data from the glacier inventory of China (Ding and others, 1986). The results show good correlations between glacier area and altitude difference, as well as between glacier length and altitude difference. The glacier shape can thus be determined from the two correlations. The parameters representing the absolute glacier elevation can be expressed using the relationships of glacier area to maximum, mean and minimum elevation, where the relationship of the area to the maximum elevation is best. Other methods can be used to calculate initial glacier surface elevation, thickness and width along the main flowline, as described below.

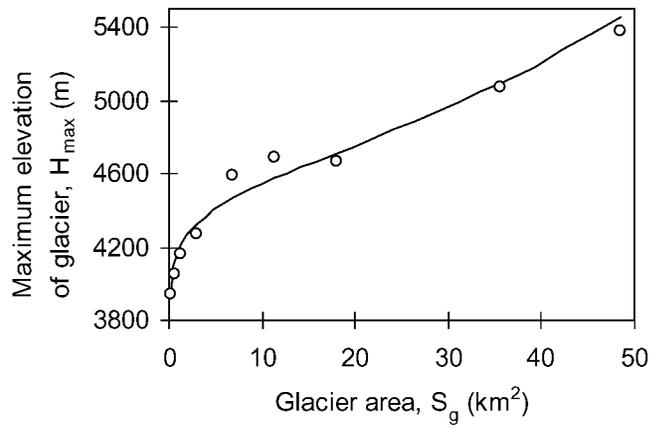


Fig. 2. The relationship between the maximum elevation and glacier area.

3.1.1. Glacier area and maximum elevation

In a basin, the maximum glacier elevation (H_{\max}) has a significant impact on the simulation result. The relationship between H_{\max} and glacier area is found using the glacier inventory; it is not good, especially for the large glaciers since most of the glaciers used in the relation are small. A statistical average of H_{\max} for the different glacier areas of the Yili river basin is derived by means of glacier area classification. The relationship between H_{\max} and area (S_g) is shown in Figure 2 and expressed by:

$$H_{\max} = a(26.391S_g + 4168.2) + (1 - a)(243 \ln S_g + 4155.9), \quad (6)$$

$$a = S_g/97 + 0.5,$$

where the unit of S_g is km^2 and the unit of H_{\max} is meters.

3.1.2. Glacier length and glacier altitude difference

Using the glacier inventory data, the relationships among glacier area (S_g), glacier length (L) and altitude difference (TZ) were derived by the regression method as:

$$L = 1.638S_g^{0.5668} \quad (n = 2242, R = 0.914), \quad (7)$$

$$\text{TZ} = 5.992S_g^{0.3888} \quad (n = 2242, R = 0.754), \quad (8)$$

where the unit of S_g is km^2 and the unit of L and TZ is meters. n is the sample size and R is the correlation coefficient.

3.1.3. Change in ice surface slope along the main flowline

Generally, the surface slope of a glacier strongly influences its flow velocity and thickness. The surface slope varies greatly, especially in places with icefalls, due to the underlying terrain, and the surface slope along the main flowline varies with glacier area and type. To estimate changes of surface slope along the main flowlines, 47 glaciers in the Yili river basin were selected for analysis from the 1:50 000 topographic map, and 29 glaciers in the Tomor peak region from the 1:200 000 glacier topographic map. Statistical analysis of the data yields the following result for the surface slope K along the main flowline:

$$K(l) = S_g^{-0.207} \exp(-5.77l + 4.51l^2 + 0.198) \quad (9)$$

$$(n = 577, R = 0.763),$$

where l is the relative distance (from the top of the glacier) along the main flowline $[0, 1]$.

3.1.4. Changes in glacier area and surface width with elevation

Based on the data from two topographic maps published in

1943 and 1977, Kuzmichenok (1993) measured and statistically analyzed glacier areas for different elevation belts of 178 glaciers in the Akcerak peak region of the western Tien Shan. He found that the distribution of glacier area with elevation was determined by:

$$\Delta S_{g_j} = S_g \sum_{i=1}^5 \frac{a_i}{i} [\cos(i\pi Z_j) - \cos(i\pi Z_{j+1})], \quad (10)$$

where Z_j is the relative elevation, $Z_j \in [0, 1]$, and a_i different factors:

$$\begin{aligned} a_1 &= 0.5 \\ a_2 &= 0.04828 \\ a_3 &= -0.162 + 0.20088 e^{-0.06645 S_{g_0}} \\ a_4 &= -0.5792 + 0.0672 e^{-0.09175 S_{g_0}} \\ a_5 &= 0.21325 + 0.2125 e^{-0.00484 S_{g_0}} \end{aligned}$$

where, when $S_g \leq 0.1 \text{ km}^2$, $S_{g_0} = 0.1$, and when $S_g \geq 70 \text{ km}^2$, $S_{g_0} = 70$, when $0.1 \text{ km}^2 \leq S_g \leq 70 \text{ km}^2$, $S_{g_0} = S_g \text{ (km}^2\text{)}$.

The glacier width, W , at a given elevation belt can be calculated according to the glacier area in the belt (ΔS_j) and the corresponding distance which is determined by the surface slope and the elevation difference. The surface slope is determined by Equation (9). W can be expressed as:

$$W_j = \Delta S_j \frac{K(l_j)}{Z_j - Z_{j+1}}, \quad (11)$$

where W_j , ΔS_j and Z_j are in meters.

3.1.5. Estimation of initial glacier thickness

According to Paterson (1981), initial glacier thickness H_0 along the main flowline can be estimated by:

$$H_0 = \frac{\tau_0}{K_h \rho g \sin \alpha}, \quad (12)$$

where τ_0 is ice yield stress, varying from 80 to 150 kPa, and K_h is a factor accounting for glacier cross-section. We determined glacier thickness in the main flowline from the slope in the main flowline. The goal of estimating glacier thickness is to determine glacier bed altitude from glacier surface altitude.

Based on the other studies (Su, 1985; You and others, 1988) that were conducted using topographic data and the thickness of Tailan glacier in the Tomor peak region and of Ürümqi glacier No. 1 (UG1) in the Tien Shan, $\tau_0/K_h \rho g$ changes from 8 to 17 m, with an average of 11.3 m for $\tau_0 = 100 \text{ kPa}$.

Based on the above analyses, the shape characteristics of glaciers of various sizes can be statistically determined by Equations (6–12). From these we can create the “representative glacier” which will have the statistical characteristics of glaciers of various sizes. The representative glacier can be regarded as the initial input parameters of the glacier ice-flow model to simulate the responses of glaciers to climatic change.

3.2. Calculation of glacier mass balance and runoff

The glacier mass balance can be calculated by the degree-day factor (Braithwaite and others, 1993; Liu Shiyin and others, 1996), and the runoff can be estimated by the water balance in various elevation bands (Konovalov, 1979). The degree-day factors of snow and ice ablation are 3.1 and 7.3 $\text{mm K}^{-1} \text{d}^{-1}$, respectively, as estimated by the mass-balance data of UG1 (Liu Shiyin and others, 1996). The elevation bands of UG1 cover a wide range (3740–4400 m a.s.l.), so the different precipitation types have been taken into account in calculating

Table 1. Estimated flow parameters of UG1

Position	Observing points	Elevation m	Slope	Velocity m a^{-1}	Thickness f_1 ($\times 10^{-25}$) $\text{m}^6 \text{N}^{-3} \text{s}^{-1}$	
					m	$\text{m}^6 \text{N}^{-3} \text{s}^{-1}$
Eastern branch	G4	4004	0.187	4.4	124	13.8
	F4	3970	0.192	5.0	122	15.6
	E2	3935	0.167	5.2	130	18.8
	C2	3845	0.278	5.7	91	20.0
Western branch	H3	4078	0.200	6.6	123	17.7
	G2	4066	0.167	6.4	131	22.5
	G+2	4054	0.250	6.9	130	7.8
	F2	4000	0.167	6.8	123	30.7
	E3	3994	0.267	8.3	97	25.2
Average						19.1

the glacier mass balance (Ye and Chen, 1997). Because most of the meteorological and hydrological stations are located below 2000 m a.s.l. in the basin, and data from high-elevation areas are limited, temperature and precipitation in high-elevation areas were estimated by the co-relationship between elevation and precipitation from data collected at mid- and low-elevation areas (Ye and others, 1997).

3.3. Determination of comprehensive glacier flow parameter (f_1)

The glacier flow parameter, f_1 , varies from 10^{-25} to $10^{-24} \text{ m}^6 \text{N}^{-3} \text{s}^{-1}$, as suggested by other studies (Oerlemans, 1997; Schmeits and others, 1997; Zuo and Oerlemans, 1997; Wallinga and Van de Wal, 1998), with the range. In this study, f_1 is calculated using Equation (6) and the observed data from UG1, close to the Yili river basin. The observed data include the surface movement velocity measured during the period 1980–86, the glacier thickness determined by radar and validated by borehole data, and the topographical data from UG1 (You and others, 1988). Values of f_1 are listed in Table 1.

For mass-balance calculation, the time interval was set to 30 days, and the distance interval was limited to 100–300 m according to glacier sizes.

4. GLACIER RESPONSE TO CLIMATIC CHANGE

Glaciers with areas of 0.5–45.0 km^2 in the upper reaches of the Yili river basin were selected to simulate glacier response to climatic change. Based on statistical analyses of glacier shape parameters, 15 different glacier schemes were calculated using Equations (6–12). The 15 schemes were regarded as initial conditions of the glacier ice-flow model, and the input data are mean monthly air-temperature and precipitation data from 1954 to 1997 in the Yili river basin.

4.1. Simulations of glacier sizes at steady state

Glaciers of different sizes were selected for simulation using the glacier ice-flow model. Glaciers with different areas, initial conditions and average temperature and precipitation during 1954–97 are the input of the model. The mass balance is calculated by the degree-day factor according to the monthly temperature and precipitation at different elevations, and then the calculated mass balance is used as input

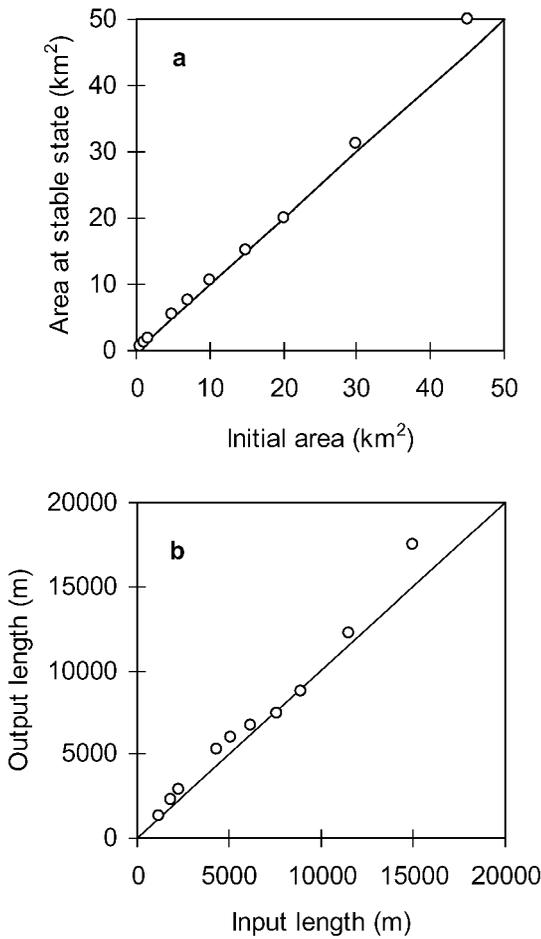


Fig. 3. Comparison of initial input values with simulated glacier sizes at steady state, (a) for glacier area, (b) for glacier length.

data for the glacier ice-flow model. The model indicates that the glaciers will reach steady state after a long period (2000 years) under the current climatic conditions. It can be seen from Figure 3 that the simulated length and area of glaciers are consistent with their initial values. In fact, the glaciers in the Tien Shan have been retreating since the 1950s. The model has somewhat overestimated the glacier size in modern climate conditions. The mass-balance and ice-flow models have been examined in UG1 (Ye and Chen, 1997). The small overestimate may be caused by (1) overestimated precipitation in the alpine area, based on the precipitation gradient in the middle and low mountains, and (2) the H_{max} which is a significant factor to steady glacier size. The simulated results consistent with the initial glacier areas and lengths show that the model is reliable for simulating glacier sizes under modern climatic conditions, at least for the mass-balance model and the representative glacier with various areas.

4.2. Schemes of climatic change

The schemes of climatic change were selected based on mean air temperature and precipitation observations from 1954 to 1997. Because future precipitation change is difficult to predict, the function of temperature change is only considered for the climate-change scenarios in the study. It was assumed that air temperature rises by 1 K, and the rates vary from 1 K per year (sudden change) to 1 K per 1000 years.

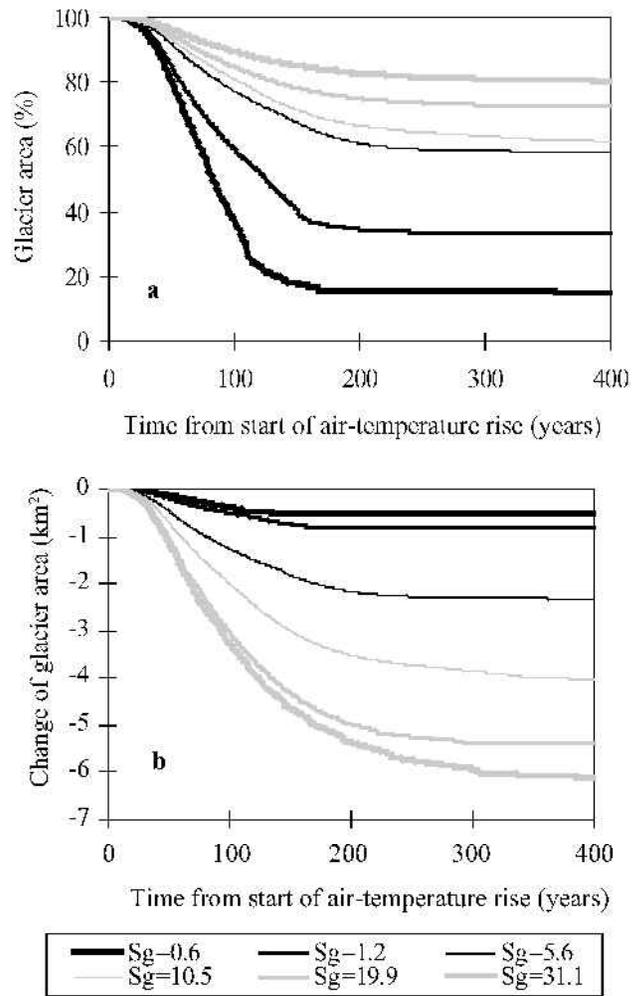


Fig. 4. The change in area of glaciers of various sizes (S_g (km²)) as air temperature rises by 1 K within 40 years: (a) the relative change; (b) the absolute change.

4.3. Simulated results

4.3.1. Processes of glacier change

The temporal changes in glacier area under different climatic scenarios are shown in Figure 4. It can be seen that there are significant differences in the sensitivity of various-sized glaciers to climatic warming, and that the larger the glacier, the faster the retreat (absolute change due to warming). However, the relative changes to the larger glaciers are rather small. This result is consistent with the comparison between two recent aerial photographs in the Ürümqi river basin (Chen and others, 1996). In addition, the time required for glaciers to reach a steady state is prolonged with size increase under a given climatic disturbance.

4.3.2. Changes in glacier runoff

Change in glacier runoff under different climatic scenarios is illustrated in Figure 5 (the runoff is relative to the average runoff under the present climate for 1954–97). In each case, there are maxima in glacier runoff which are defined as runoff peaks. It is obvious that the smaller the glacier, the more sensitive the response of glacier runoff to climatic change, the higher the runoff peak, and the faster the attenuation of runoff. The timing of the runoff peak depends on the rate of air-temperature rise (RTR (K a⁻¹)). The higher the rate, the earlier the appearance of the peak, and the higher the peak magnitude. The discrepancy

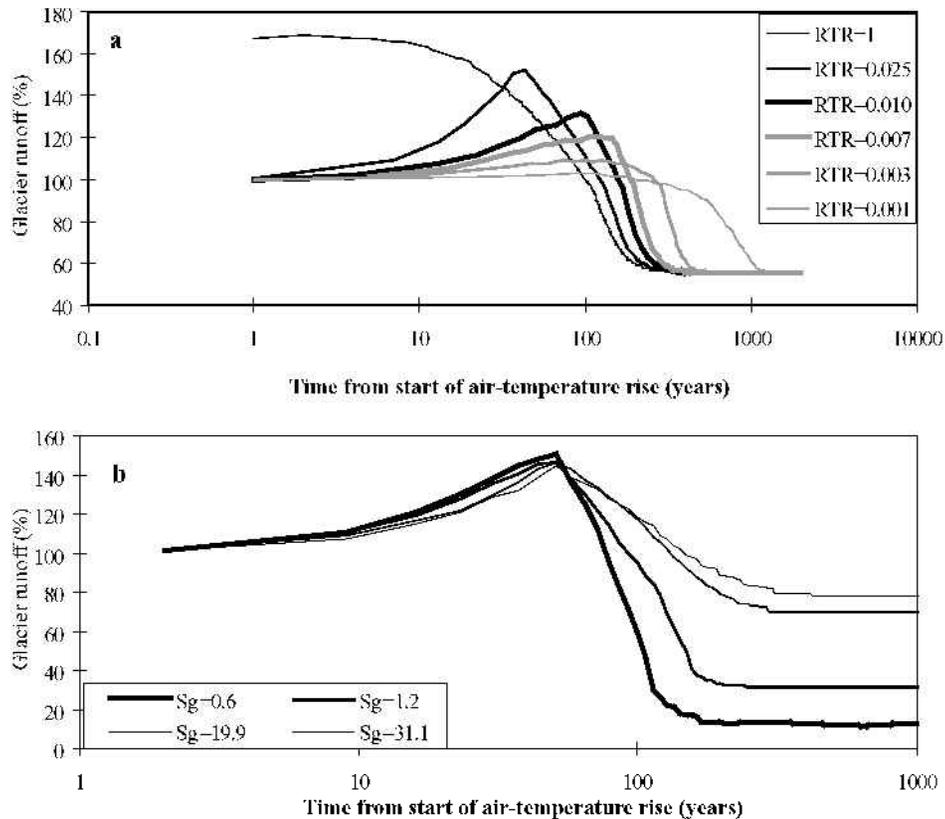


Fig. 5. Change processes of glacier runoff. (a) The processes of glacier runoff change under different rates of air-temperature rise (RTR ($K a^{-1}$)). The glacier area is $5 km^2$. (b) Runoff change as a function of glacier area (S_g (km^2)), for air temperature rising $1 K$ within 40 years.

between the changes in runoff and temperature shows hysteresis of the response of glaciers to climatic change.

4.3.3. Values of glacier runoff peaks

In the arid region of northwest China, the availability of water is of vital importance to society and the economy, and the glacier runoff forms an important part of the water resources. Accordingly, we focus on the glacier runoff change, especially on the volume and the timing of the glacier runoff peak. The dependence of runoff peaks on glacier size and different rates of air-temperature rise is shown in Figure 6. The runoff peak decreases progressively with decrease in the rate of air-temperature rise and with increase in glacier size (Fig. 6a and b). If the glacier area is large enough ($>30 km^2$) or the rate of temperature rise is slow enough ($<0.005 K a^{-1}$), the runoff peak tends to be a constant, and thus the difference between different sizes of glaciers is small, becoming significant only when climate change is rapid. Because of limitations of the model, the timing of the runoff peak was not reliably simulated when the rising rate was small and the peak was low (Fig. 7). However, the results still show a distinct tendency: if the rate of temperature rise is large, the timing of the runoff peak will stay synchronous with the occurrence of maximum air temperature; with decreasing rising rate, however, the runoff peak appears before the temperature peak reaches its maximum for small glaciers.

4.3.4. Changes of glaciers of various sizes at equilibrium state

Figure 8 illustrates the change in area, length and size of initially stable glaciers for a warming of $1 K$. It shows that the relative sensitivity to warming is larger for smaller glaciers. The relative changes in length in response to warming are smaller than the volume changes, and changes in

glacier area due to warming are smaller than changes in length under the same conditions. The relative changes are similar if the glacier size is relatively small (e.g. $<0.6 km^2$). The sensitivity of glacier area to warming exceeds that of length when the glacier area is small. This shows that changes to small glaciers are dominated by area reduction rather than length shortening under warming. This result is validated by the 1964–92 observation data from the Ürümqi river basin: changes in glacier length, area and volume of 12.4%, 13.8% and 16.8%, respectively, were measured for glaciers with an average area of $0.31 km^2$ (Liu Chaohai and others, 1996). For larger glaciers, length decreases dominate.

Figure 9 compares the simulated change in glacier area and the change measured by distributions of glacier moraine since the Little Ice Age (LIA) in the Tien Shan (Wang, 1991). Figure 10 shows the changes in glacier volume, length and area for different glacier sizes measured from the selected 66 glaciers in the upper Yili river basin using aerial photographs taken during the last 40 years. Although the climatic conditions applied to the two simulations and the degrees of glacier changes are different, the trends of glacier changes indicated by Figures 9 and 10 are consistent, suggesting that the glacier ice-flow model can simulate glacier changes with different glacier sizes in response to climatic warming.

4.3.5. Model validation

Validation of the glacier model, including the mass-balance model, has been performed on UG1 (Liu Shiyin and others, 1996; Ye and Chen, 1997). However, because observation data are lacking for processes of glacier change affecting different areas, the simulation was validated by comparing initial glacier areas and lengths with the simulation of the glacier sizes at steady state, and with the actual change of glacier

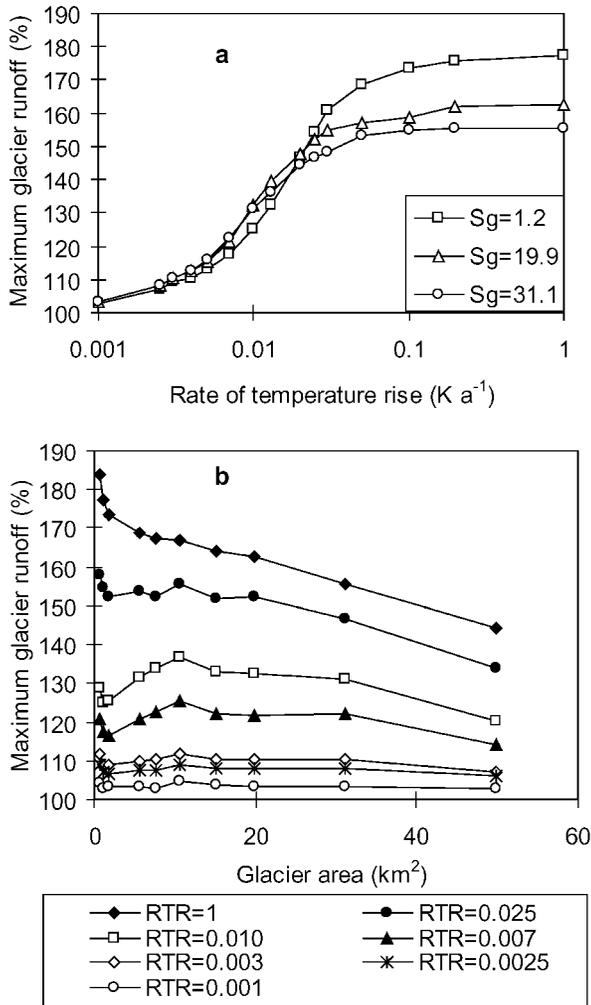


Fig. 6. Changes in glacier runoff peak for (a) different glacier sizes (S_g (km^2)) and (b) different rates of air-temperature rise (RTR (K a^{-1})).

area in the Tien Shan since the LIA. To test the simulated results, we compared them with the actual glacier changes in the Tien Shan since the LIA and during the period 1962–92. The air temperature has risen by 0.5–0.8 K on the global

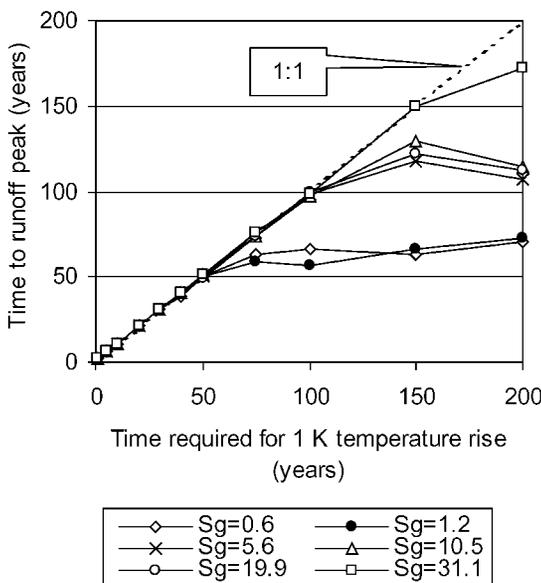


Fig. 7. The time to glacier runoff peak, with time required for 1 K temperature increase for different glacier sizes (S_g (km^2)).

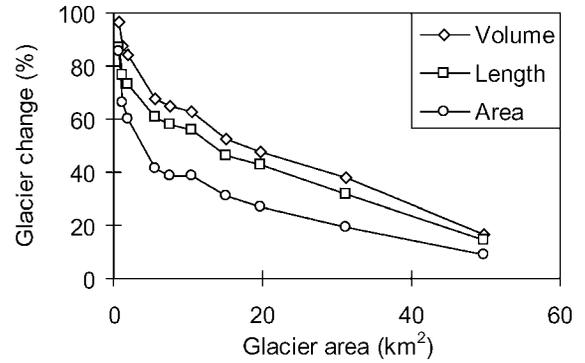


Fig. 8. Changes of initially stable glaciers with different areas for a climatic warming of 1 K.

surface over the last 150 years (Jones and others, 1999) and by 1.4 K in west China since about AD 1700 (Shi and Liu, 2000). According to meteorological data from 97 stations above 200 m altitude in west China, the summer temperature rise is about 0.008 K a^{-1} and the annual temperature rise 0.013 K a^{-1} during the period 1955–95. Considering the difference between annual and summer temperature, and excluding the rise over the last 40 years, the change in summer temperature in northwest China is about 0.5 K between the Little Ice Age and the 1950s. The area changes for a selected 15 km^2 glacier are listed in Table 2. The simulated change in glacier area with a warming of 0.5 K within 250 years is very close to the change in glacier area since the LIA. However, the glacier change during the period 1962–89 is not consistent with the simulated result. The reason is related to differences in initial conditions: glacier retreat in the Tien Shan has been ongoing since the 1950s, but the simulated initial condition is a stable one, so the simulated result is less than the actual change.

5. CONCLUSIONS

The following conclusions are drawn:

- (1) The glacier ice-flow model can simulate glacier changes as functions of glacier size in response to climatic warming.
- (2) The larger the glacier, the faster the retreat (absolute change due to warming). However, the relative changes of larger glaciers are rather small.
- (3) Compared to glacier length and area, glacier volume undergoes the most pronounced change with warming.

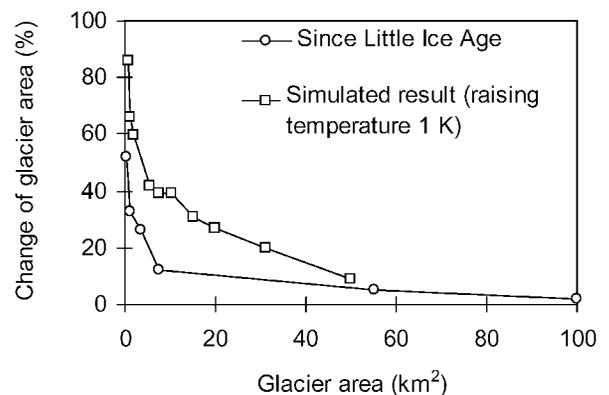


Fig. 9. Comparison between the simulated changes of different glacier areas with warming of 1 K and the measured changes since the LIA in the Tien Shan.

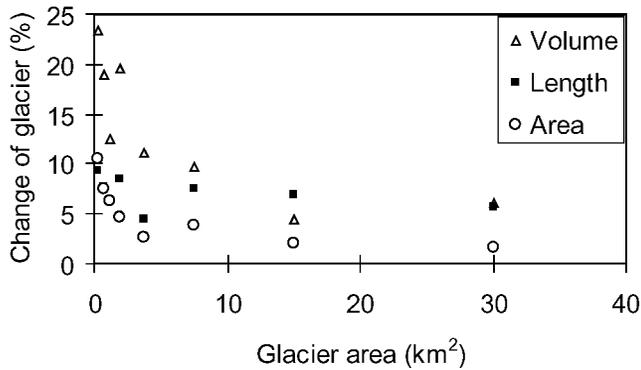


Fig. 10. Changes in glacier volume, length and area with different glacier sizes in the upper Yili river basin, 1962–89.

Table 2. Comparison of the simulated results with the actual changes of a selected 15 km² glacier in the Tien Shan since the Little Ice Age and during 1962–92

	Period	
	Little Ice Age (1700–1955)	1962–89
Change of summer temperature (K)	0.5	0.2
Rate of summer temperature change (K a ⁻¹)	0.002	0.008
Observed change of glacier		
Area (%)	-11	-2.0
Length (%)		-4.4
Volume (%)		-6.9
Time after starting rising (years)	250	27
Simulated change of glacier		
Area (%)	12	1
Length (%)	15	2
Volume (%)	25	2

For larger glaciers, the change in length (retreat) is more significant than the change in area; for smaller glaciers (<0.6 km²), the opposite is the case.

- (4) Under climatic warming, smaller glaciers with higher runoff peaks tend not only to vary more in runoff, but also to retreat more quickly than larger glaciers.
- (5) The magnitude and appearance time of runoff peaks depend not only on glacier size but also on the rising rate of air temperature. The faster the air temperature rises, the higher the peaks, and the earlier the appearance time of peaks.

ACKNOWLEDGEMENTS

This research project was supported by grants from the Innovation project of the Chinese Academy of Sciences (KZCX1-10-06, KZCX2-301) and the Chinese National Scientific Fund (49971022). We thank T. S. Clarke, R. J. Braithwaite and W. D. Harrison for their valuable comments and suggestions, and J. W. Glen, the Scientific Editor. We also thank Zhang Xinping and Yang Daqing for suggestions.

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MS received 6 April 2000 and accepted in revised form 12 November 2002