Simulated features of the air-hydrate formation process in the Antarctic ice sheet at Vostok

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ABSTRACT. A recently developed theory of post-nucleation conversion of an air bubble to air-hydrate crystal in ice is applied to simulate two different types of air-hydrate formation in polar ice sheets. The work is focused on interpretation of the Vostok (Antarctica) ice-core data. The hydrostatic compression of bubbles is the rate-limiting step of the phase transformation which is additionally influenced by selective diffusion of the gas components from neighboring air bubbles. The latter process leads to the gas fractionation resulting in lower (higher) N₂/O₂ ratios in air hydrates (coexisting bubbles) with respect to atmospheric air. The typical time of the post-nucleation conversion decreases at Vostok from 1300–200 a at the beginning to 50-3 a at the end of the transition zone. The model of the diffusive transport of the air constituents from air bubbles to hydrate crystals is constrained by the data of Raman spectra measurements. The oxygen and nitrogen self-diffusion (permeation) coefficients in ice are determined at 220 K as 4.5×10^{-8} and 9.5×10^{-8} mm² a⁻¹, respectively, while the activation energy is estimated to be about 50 kJ mol⁻¹. The gas-fractionation time-scale at Vostok, $\tau_F \sim 300$ a, appears to be two orders of magnitude less than the typical time of the air-hydrate nucleation. air-hydrate nucleation, $\tau_{\rm Z}\sim 30-35$ ka, and thus the condition for the extreme gas fractionation, $\tau_{\rm F} \ll \tau_{\rm Z}$ is satisfied. Application of the theory to the GRIP and GISP2 ice cores shows that, on average, a significant gas fractionation cannot be expected for air hydrates in central Greenland. However, a noticeable (statistically valid) nitrogen enrichment might be observed in the last air bubbles at the end of the transition.

1. INTRODUCTION

Clathrate air-hydrate crystals, substituting for air bubbles in the deeper layers of polar ice sheets at high load pressures and low temperatures, were first predicted by Miller (1969), and then observed by Shoji and Langway (1982, 1987) in available ice cores from Antarctica (Byrd) and Greenland (Dye-3, Camp Century). Understanding of the unique natural phenomenon of the air-phase-state transformations in ice remains one of the key objectives of paleoclimatic interpretations of atmospheric air-content and gas-composition records obtained in deep-ice-core studies.

Further detailed optical-microscope investigations of the air bubbles and air hydrates were performed on fresh ice cores from Vostok station, East Antarctica (Barkov and Lipenkov, 1984; Lipenkov, 1989; Lipenkov and Salamatin, 1989; Uchida and others, 1994a), and continued in laboratory experiments (Hondoh, 1989; Hondoh and others, 1990; Uchida and others, 1992, 1994b; Ikeda and others, 1993; Hondoh, 1996). The new data were examined on the basis of mathematical modelling and scale analysis in Salamatin and others (1998b). It was shown that the rate-limiting step of the conversion of air bubbles, occluded in ice, to air hydrates was the nucleation of the hydrate crystals. The latter process is primarily responsible for a large (several hundred meters thick) transition zone where pre-existing air bubbles and clathrate air-hydrate crystals coexist in polar ice sheets.

For example, first air-hydrate crystals at Vostok are found at 550 m depth where the bubble supersaturation (the difference between the bubble pressure and the hydrate dissociation pressure) is about 1.2 MPa. The entire transformation of air bubbles to air hydrates takes the time period $\tau_{\rm Z} \sim 30\,{\rm ka}$ and proceeds to 1250 m depth, where the last bubbles disappear at the supersaturation of about 6.2 MPa.

The model simulations in Salamatin and others (1998b) are restricted to the case when air hydrate, after nucleation, rapidly coats the bubble wall and then grows as a spherical hydrate shell, filling up the bubble. This type of conversion, denoted in Figure 1 as type A, was dominant in the laboratory observations of secondary air-hydrate growth in air cavities formed due to the decomposition of the initial hydrate crystals after ice-core recovery (Uchida and others 1992, 1994b). The following two counterparts of the transformation have been described mathematically: (1) the diffusive air- and water-mass transfer through the hydrate layer in opposite directions, and (2) hydrostatic compression of the bubble confined to the hydrate shell and surrounding ice, both plastically deformed under the excess load pressure. The model constrained by the laboratory experiments allows us to estimate the typical time-scales of these processes (hereafter denoted as τ_D and τ_C , respectively), which can be of the same order of magnitude at relatively high laboratory temperatures. However, extension of these results to the extreme conditions (low temperatures) of central

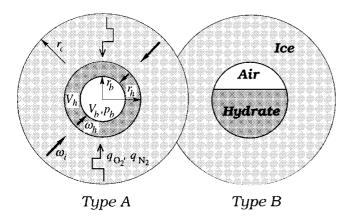


Fig. 1. Two types of air-bubble—air-hydrate transformation. Here r_c is the radius of a spherical ice cell influenced by nitrogen (q_{N_2}) and oxygen (q_{O_2}) mass fluxes from neighbouring air bubbles and air hydrates, r_b is the equivalent-sphere radius of the air bubble, and r_h is the radius of the bubble—hydrate complex; V_b and V_h are the bubble and hydrate volumes, respectively.

Antarctica leads to the following ratios between the timescales downward in the transition zone:

$$\tau_{\rm D}/\tau_{\rm C} \sim 10^{-5} \ {\rm to} \ 10^{-3}, \qquad \tau_{\rm C}/\tau_{\rm Z} \sim 10^{-2} \ {\rm to} \ 10^{-4} \, .$$

Another type, B, of post-nucleation conversion of air bubbles to air hydrates was also observed by Uchida and others (1992). As shown in Figure 1, in this case the air-hydrate crystal does not coat the bubble wall but instead gradually grows inward, maintaining a flattened interface with the gaseous phase. This type of transformation might be even more common for polar ice sheets, where air bubbles initially do not have the air-hydrate structure on their surface, and coating clathration would be very difficult. The absence of the hard hydrate shell (Salamatin and others, 1998b) around the bubble may reduce the compression time $\tau_{\rm C}$ by one order of magnitude. Nevertheless, for both types A and B the postnucleation conversion of an air bubble to air hydrate in polar ice sheets, being at least 2-4 orders faster than the hydrate nucleation, remains limited by the bubble compression. Only a very short stage at the very beginning of the post-nucleation transformation might be controlled by the diffusion, when, due to the high supersaturation of the bubble, a large quantity of air is abruptly converted to hydrate crystal, and the bubble pressure, initially close to the load pressure, simultaneously drops to the dissociation pressure level.

An important peculiarity of the process was revealed in Salamatin and others (1998b). The rate of air-mass diffusive transport through the hydrate layer is estimated to be 10-50 times lower than the rate of water-mass transfer. This implies that in the laboratory tests, conducted at 255–270 K, the gas diffusion is too slow to change noticeably the "frozen" distribution of the air constituents in the growing hydrate layer. As a result of the dominant clathration of oxygen, maximum concentrations of nitrogen are obtained in the central part of the hydrate at the end of clathration. By contrast, in polar ice sheets the typical time for air diffusion in hydrate crystal is still much less than $\tau_{\rm C}$, and the gas compositions in the bubble and the growing hydrate are close to thermodynamic equilibrium. The only, yet non-crucial, exception might be the B-type conversion process at the end of the transition zone, when the rates of the air diffusion in hydrate crystals become comparable with those of the bubble compression. Thus, in applications to the natural,

low-temperature conditions the mathematical model of the post-nucleation air-hydrate formation (Salamatin and others, 1998b) should be reduced to the case of compression of the quasi-equilibrium bubble—hydrate complex at the dissociation pressure and under the excess load pressure in the surrounding ice matrix.

Recent detailed measurements of Raman spectra of individual air bubbles and air-hydrate crystals in Vostok ice cores performed by Fukazawa and others (1996) and Ikeda and others (1999) confirm significant changes in N₂/O₂ ratios in both groups of inclusions coexisting in the transition zone, as previously found by Nakahara and others (1988) in air hydrates from the Dye-3 ice cores. The N_2/O_2 ratio in the first air hydrates observed at the beginning of the transition zone at Vostok is around 2, i.e. about two times less than the present-day air value (3.7) in surrounding air bubbles. The hydrate oxygen enrichment vanishes by the end of the transition, while the N2/O2 ratio in bubbles dramatically increases to 11.7 in the last air inclusions. Hence, selective diffusion of the air constituents between the nonnucleated air bubbles and hydrate crystals (Ikeda and others, 1999) must be admitted as another process that essentially controls air-hydrate formation in polar ice sheets. The latter findings call for additional theoretical work to develop a mathematical model adequately extending that by Salamatin and others (1998b) to extreme polar-ice-sheet conditions. Such a study is attempted in this paper.

The experimental data reviewed above on the evolution of the air-bubble and air-hydrate-crystal ensembles in the transition zone at Vostok are sufficiently representative to constrain the model. Unfortunately, very important GISP2 and GRIP publications on the Greenland Summit ice cores (e.g. Pauer and others, 1996, 1997, 1999) deal mainly with the ice-core samples retrieved from the deeper part of the transition or below it and lack the necessary information on air inclusions.

2. MODEL OF AIR-HYDRATE CRYSTAL GROWTH

Basic notations, assumptions and relations

Fast post-nucleation conversion of air inclusions to air hydrates in ice sheets, especially rapid in the B-type clathration, makes the probability of finding a "semi-bubble" (an air inclusion partly transformed to air hydrate) extremely low. With this in mind, let us consider (see Fig. 1) a single initially spherical air bubble which converts to air hydrate in infinite ice matrix containing only non-nucleated air bubbles and complete air-hydrate crystals. The current volumes, $V_{\rm b}$ and $V_{\rm h}$, of the air and the hydrate for both possible types of post-nucleation conversion are linked to the equivalent-sphere radius $r_{\rm b}$ of the bubble and to the external radius $r_{\rm h}$ of the whole bubble—hydrate complex (semi-bubble):

$$V_{\rm b} = \frac{4}{3}\pi {r_{
m b}}^3 \,, \qquad V_{
m h} = \frac{4}{3}\pi ({r_{
m h}}^3 - {r_{
m b}}^3) \,.$$

At the very moment of the air-hydrate nucleation, bubble pressure is close to the load pressure $p_{\rm l}$ in ice (Lipenkov and others, 1997; Salamatin and others, 1997), but almost immediately, as an initial air-hydrate layer (or crystal) forms on the bubble wall, the pressure drops to the hydrate dissociation pressure $p_{\rm d}$ (Salamatin and others, 1998b). Based on the considerations presented in the introduction, we assume

that in the following compression stage of the conversion the free gas phase is in equilibrium with the hydrate.

Hence, in accordance with Van der Waals and Platteeuw's theory (1959)

$$p_{\rm d} = X_{\rm N_2} p_{\rm dN_2} + X_{\rm O_2} p_{\rm dO_2};$$

$$X_{\rm N_2} = \frac{(1 - \lambda) Z_{\rm N_2}}{1 - \lambda Z_{\rm N_2}}, \quad X_{\rm O_2} = \frac{Z_{\rm O_2}}{1 - \lambda Z_{\rm N_2}}, \quad \lambda = 1 - \frac{p_{\rm dO_2}}{p_{\rm dN_2}},$$

$$(1)$$

where $Z_{\rm N_2}$, $Z_{\rm O_2}$ and $X_{\rm N_2}$, $X_{\rm O_2}$ are mole fractions of nitrogen and oxygen in the air bubble and the hydrate crystal growing on its walls, $Z_{\rm N_2} + Z_{\rm O_2} \approx 1$, $X_{\rm N_2} + X_{\rm O_2} \approx 1$, and $p_{\rm dN_2}$ and $p_{\rm dO_2}$ are the respective dissociation pressures of pure N₂- and O₂-hydrates expressed in MPa after Miller (1969) as functions of temperature T (in K):

$$\log p_{\text{dN}_2} = 3.6905 - 688.9/T$$
, $\log p_{\text{dO}_2} = 3.679 - 717/T$.

The process of post-nucleation conversion of a single bubble to an air hydrate in an ice sheet is quite short, and T is considered hereafter as a constant parameter.

The air in bubbles downward along the transition zone becomes more enriched with nitrogen (Ikeda and others, 1999). As for air hydrates, even at the beginning of the transition, their N_2/O_2 ratio does not fall below 2. Natural predominance of nitrogen with its mole mass M_{N_2} close to the oxygen mole mass M_{O_2} allows us to use in mass-balance calculations the gas state equation for standard atmospheric air, disregarding the minor (3–4%) changes in its mole mass $M_a \approx M_{N_2}$ and density ρ (or pressure p) caused by the gas composition variations:

$$p = z_{\rm g} R_{\rm g} \rho T / M_{\rm a} \,,$$

where $z_{\rm g}$ and $R_{\rm g}$ are the non-ideal compressibility coefficient (depending on thermodynamic conditions) and the gas constant. For the same reasons, the densities of the air (mainly nitrogen) and water components $\rho_{\rm ha}$ and $\rho_{\rm hw}$ in the clathrate hydrate phase at the dissociation pressure are assumed to be constant and are taken after Hondoh (1989) and Hondoh and others (1990).

All the main physical characteristics and parameters used in this study, and their symbols and values, are presented in Table 1.

Mass-balance equations

The mass of nitrogen and oxygen in the air bubble and the hydrate, growing on its wall, changes due to the gas diffusive transport between the developing bubble—hydrate complex and the surrounding sources and sinks of air molecules, i.e. other air and hydrate inclusions distributed in the ice. Consequently, the equation of the total gas mass balance in the semi-bubble takes the form (normalized by the factor $M_{\rm a}/(z_{\rm g}R_{\rm g}T)$):

$$\frac{d(p_{\rm d}V_{\rm b})}{dt} + p_{\rm ha}\frac{dV_{\rm h}}{dt} = p_{\rm iw}(q_{\rm N_2} + q_{\rm O_2}),\tag{2}$$

where t is the time. The overall surface mass fluxes of nitrogen $q_{\rm N_2}$ and oxygen $q_{\rm O_2}$ from neighboring air and hydrate inclusions to the semi-bubble are normalized by the factor $M_{\rm a}\rho_{\rm i}/M_{\rm w}$ ($M_{\rm w}$ is the mole mass of water), i.e. expressed as the equivalent ice-volume flow rate of the same number of water molecules. Parameters $p_{\rm ha}$ and $p_{\rm iw}$, defined as

$$p_{\mathrm{ha}} = z_{\mathrm{g}} R_{\mathrm{g}} \rho_{\mathrm{ha}} T / M_{\mathrm{a}}, \quad p_{\mathrm{iw}} = z_{\mathrm{g}} R_{\mathrm{g}} \rho_{\mathrm{i}} T / M_{\mathrm{w}},$$

are the pressures at which the densities of air and water

Table 1. Physical properties of air-ice-hydrate system and model parameters

Parameter	Symbol	Value
Air		
Gas constant Non-ideal compressibility coefficient Mole mass of N_2 Self-diffusion coefficient of N_2 in ice Mole mass of O_2 Self-diffusion coefficient of O_2 in ice Self-diffusion activation energy	$egin{array}{l} R_{ m g} \ z_{ m g} \ M_{ m N_2} \ D_{ m N_2} \ M_{ m O_2} \ D_{ m O_2} \ Q_{ m d} \end{array}$	$8.314 \text{ J mol}^{-1} \text{ K}^{-1} \\ 0.9 - 0.95 \\ 28 \text{ g mol}^{-1} \\ 4.5 \times 10^{-8} \text{ mm}^2 \text{ a}^{-1\ddagger} \\ 32 \text{ g mol}^{-1} \\ 9.5 \times 10^{-8} \text{ mm}^2 \text{ a}^{-1\ddagger} \\ 50 \text{ kJ mol}^{-1\ddagger}$
Ice		
Density Mole mass of water Reference temperature Creep index Rheological coefficients at $T=T_{\ast}$	$egin{array}{l} ho_{ m i} \ M_{ m w} \ T_* \ lpha_{ m i} \ \mu_{ m i1} \end{array}$	920 kg m ⁻³ 18 g mol ⁻¹ 263 K 3.5 7.9 MPa a [†] 0.14 MPa ^{\alpha} a [†]
Activation energy	$Q_{ m i}$	$60 \text{ kJ mol}^{-1},^{\dagger} T < T_*$

Air hydrate (Stackelberg's structure II)

Air density	$ ho_{ m ha}$	$180 \mathrm{kg m}^{-3}$
Water density	$ ho_{ m hw}$	$800 \mathrm{kg} \mathrm{m}^{-3}$
Creep index	$lpha_{ m h}$	3.5
Rheological coefficients at $T = T_*$	$\mu_{ m h1}$	79 MPa a [†]
	$\mu_{ m h2}$	$1.4~\mathrm{MP}^{lpha}\mathrm{a}^{\dagger}$
Activation energy	$Q_{ m h}$	$60 \mathrm{kJ} \mathrm{mol}^{-1}, T < T_*$
Relative air-mass transfer coefficient	$d_{ m ha}$	$\sim 0.05^{\dagger}$

The estimates are deduced in Lipenkov and others (1997) and Salamatin and others (1998b) through model constraining by the experimental data.

molecules in free gaseous phases are equal to those in air hydrate (ρ_{ha}) and in ice (ρ_i) , respectively.

Correspondingly, the total mass balance of nitrogen is described by the relation:

$$\frac{d(p_{d}Z_{N_{2}}V_{b})}{dt} + p_{ha}\frac{d(V_{h}X_{N_{2}})}{dt} = p_{iw}q_{N_{2}}.$$
 (3)

The outer fluxes of the air constituents are consumed on the hydrate interfaces with ice and air by the clathration process for which the surrounding ice serves as an infinite source of water molecules. The volume deformation rate (divergence) of the ice, ω_i , at the contact with the bubble—hydrate complex is determined by the ice mass-balance equation:

$$\omega_{\rm i} = -\left[\frac{\mathrm{d}V_{\rm b}}{\mathrm{d}t} + \left(1 - \frac{\rho_{\rm hw}}{\rho_{\rm i}}\right)\frac{\mathrm{d}V_{\rm h}}{\mathrm{d}t}\right] / (V_{\rm b} + V_{\rm h}). \tag{4a}$$

The above consideration does not depend on the actual form of the growing hydrate and its location in (or around) the bubble. In the A-type conversion process, however, water molecules have to move through the hydrate shell toward the bubble (see Fig. 1), and the bubble air diffuses in the opposite direction toward the ice to form new quantities of air hydrate at both phase boundaries. As a result, the diver-

[‡] The estimates are deduced in this paper through fitting of the model predictions to experimental data for $T\sim 220$ K.

gence of the spherical hydrate layer, ω_h , differs from ω_i , and the bubble-air mass-balance equation gives:

$$\omega_{\rm h} = -\left[\frac{\mathrm{d}V_{\rm b}}{\mathrm{d}t} - \frac{1 - d_{\rm ha}}{p_{\rm ha}} \frac{\mathrm{d}(p_{\rm d}V_{\rm b})}{\mathrm{d}t}\right] / (V_{\rm b} + V_{\rm h}), \quad (4b)$$

where parameter $d_{\rm ha}$, introduced by Salamatin and others (1998b), can be interpreted as the mass fraction of the air hydrate formed of the initial bubble air at the interface with the ice due to the diffusion of the air through the hydrate shell. The value $1-d_{\rm ha}$ is the relative quantity of the air hydrate formed at the interface with the gas phase due to the diffusion of water. In the case of the B-type conversion the hydrate crystal is a continuum incompressible structure without any cavities, and $\omega_{\rm h}=0$.

Equations (2)–(4) generalize the earlier developed model (Salamatin and others, 1998b) of the conversion of an air bubble to clathrate air-hydrate crystal in ice under the basic assumption that the gas components in the bubble–hydrate system evolving under polar-ice-sheet conditions are in thermodynamic equilibrium, and the bubble pressure after nucleation is equal to the hydrate dissociation pressure.

Air-constituents diffusion through ice

Nitrogen- and oxygen-mass exchange between coexisting air bubbles and hydrates in ice sheets is the diffusive mass transfer (Ikeda and others, 1999), resulting in considerable fractionation of the air components. The driving forces are the gradients of mole concentrations of nitrogen and oxygen in the ice matrix. At the phase boundaries their values are proportional to the corresponding partial pressures of the equilibrium gaseous (vapor) phases. Thus, at the ice-hydrate interface the concentrations of the air constituents dissolved in the ice are determined by the dissociation pressures p_{dN_2} and p_{dO_2} multiplied by the mole fractions of the respective gas components in the hydrate crystal, while at the air-ice interface the concentrations are related to the corresponding partial fractions of the bubble pressure. These concentrations are the same in the vicinity of semi-bubbles undergoing different types of conversion, provided that the air pressure in them is equal to the dissociation pressure $p_{\rm d}$. In nonnucleated bubbles the pressure is identified with the load pressure $p_{\rm l}$ which in the transition zone is much higher than the dissociation pressure, thus causing the air diffusion.

Actually we have also to distinguish the gas composition $(Z_{\rm N_2},\,Z_{\rm O_2})$, and $X_{\rm N_2},\,X_{\rm O_2})$ of the reference bubble–hydrate system from the mean gas compositions of the surrounding non-nucleated bubbles $(\bar{Z}_{\rm N_2},\,\bar{Z}_{\rm O_2})$ and coexisting completely formed hydrate crystals $(\bar{X}_{\rm N_2},\,\bar{X}_{\rm O_2})$, which fractions in the total inclusion number concentration N_0 are $n_{\rm b}$ and $1-n_{\rm b}$, respectively. Hence, for instance, the background mole concentration of nitrogen in ice is determined by the averaged partial pressure induced by both groups of inclusions:

$$\bar{p}_{\mathrm{N}_2} = \gamma p_{\mathrm{l}} \bar{Z}_{\mathrm{N}_2} + (1 - \gamma) p_{\mathrm{dN}_2} \bar{X}_{\mathrm{N}_2} ,$$

where the averaging parameter γ ranges from 0 to 1, following the value $n_{\rm b}$.

The difference between the latter value and the equilibrium "nitrogen-vapor" pressure at the external surface of the growing hydrate crystal $p_{\rm dN_2}X_{\rm N_2}$ is the driving force of the nitrogen mass transfer. The same considerations are valid for the pressure $\bar{p}_{\rm O_2}$ in the case of oxygen.

The choice of parameter γ is not obvious and will be discussed in section 4. Here, at the stage of simulating the conversion of a single reference bubble to air-hydrate crystal,

the pressures \bar{p}_{N_2} and \bar{p}_{O_2} should be regarded as given model parameters. Thus, γ just links them to the averaged gas compositions of neighboring air bubbles and hydrates, so its particular value is not important. As a reasonable approximation we take $\gamma \approx n_b$.

To evaluate the diffusive mass fluxes, we use the conventional cell-model approximation for diluted multiphase media illustrated in Figure 1. A spherical semi-bubble of type A or B with growing air hydrate is confined to a spherical ice cell of a specific volume related to one inclusion, that is of radius

$$r_{\rm c} = (4\pi N_0/3)^{-\frac{1}{3}}$$
.

The averaged, background concentrations are assumed on the cell boundary, at $r=r_{\rm c}$. Gas solubility in ice is very low, and the total amount of air dissolved in the ice is negligibly small (Ikeda and others, 1999). For the latter reason, the nitrogen and oxygen diffusion through the spherical ice layer toward the developing bubble—hydrate complex is a quasistationary, spherically symmetric process. The obvious solution of the corresponding boundary-value cell problem yields:

$$q_{\rm N_2} = 4\pi D_{\rm N_2} \left[\gamma \frac{p_{\rm l}}{p_{\rm dN_2}} \bar{Z}_{\rm N_2} + (1 - \gamma) \bar{X}_{\rm N_2} - X_{\rm N_2} \right] \frac{r_{\rm c} r_{\rm h}}{r_{\rm c} - r_{\rm h}},$$

$$q_{\rm O_2} = 4\pi D_{\rm O_2} \frac{M_{\rm O_2}}{M_{\rm N_2}} \left[\gamma \frac{p_{\rm l}}{p_{\rm dO_2}} \bar{Z}_{\rm O_2} + (1 - \gamma) \bar{X}_{\rm O_2} - X_{\rm O_2} \right] \frac{r_{\rm c} r_{\rm h}}{r_{\rm c} - r_{\rm h}}.$$
(5)

Here, by definition, $D_{\rm N_2}$ and $D_{\rm O_2}$ are the self-diffusion (permeation) coefficients of pure nitrogen and oxygen in ice at a given (fixed) temperature T and dissociation pressures $p_{\rm dN_2}$ and $p_{\rm dO_2}$, respectively.

It is also worth noting that volume concentrations of bubbles and hydrates within transition zones of ice sheets are very small and $r_{\rm b}$, $r_{\rm h} \ll r_{\rm c}$. In such a case the cell-model approach is not crucial: the diffusive fluxes in Equations (5) and their analogues practically do not depend on the cell size.

Hydrostatic compression

After air-hydrate nucleation, the pressure in the bubble abruptly decreases to the dissociation pressure $p_{\rm d}$. The difference between the load pressure in the ice matrix $p_{\rm l}$ and $p_{\rm d}$ is resolved in plastic compressive deformations of the ice and the hydrate around the bubble. A mathematical description of non-linear creep flow and pressure relaxation in bubbly media (Salamatin and Duval, 1997) allowed us to construct an approximate model for hydrostatic compression (or decompression) of the air bubble converting to hydrate crystal (Salamatin and others, 1998b) in case of the Atype transformation.

The ice and clathrate air hydrate are described as non-linear viscous isotropic materials with similar polynomial flow laws relating effective strain rates e_0 and deviatoric stresses τ_0 :

$$2e_0 = \frac{\tau_0}{M_{\rm s1}} + \frac{\tau_0^{\alpha_{\rm s}}}{M_{\rm s2}}, \quad M_{\rm sj} = \mu_{\rm sj} = \exp\left[\frac{Q_{\rm s}}{R_{\rm g}} \left(\frac{1}{T} - \frac{1}{T_*}\right)\right],$$
(6)

where $\alpha_{\rm s}$ and $\mu_{\rm s1}$, $\mu_{\rm s2}$ are the exponent (creep index) and the rheological coefficients (constants) at the reference temperature T_* , and $Q_{\rm s}$ is the activation energy. Subscript "s" corresponds to ice (s = i) or to hydrate (s = h).

As a final result, the ice and hydrate volume deforma-

tion rates, ω_i and ω_h , introduced in Equations (4), are linked to the pressure drop $p_1 - p_d$ by the following relation:

$$p_{\rm l} - p_{\rm d} = \Psi_{\rm h} \left(\frac{r_{\rm h}^3}{r_{\rm b}^3} \omega_{\rm h} \right) - \Psi_{\rm h}(\omega_{\rm h}) + \Psi_{\rm i}(\omega_{\rm i}). \tag{7}$$

The integrals $\Psi_s(\omega)$, s=i, h, are approximately evaluated and written in the form:

$$\begin{split} \Psi_{\rm s}(\omega) &= {\rm sign}\,(\omega) \frac{2}{\sqrt{3}} \\ \begin{cases} &\frac{2}{\sqrt{3}} \, M_{\rm s1} |\omega|, & \frac{2}{\sqrt{3}} \, M_{\rm s1} |\omega| < \left(\frac{M_{\rm s2}}{M_{\rm s1}}\right)^{\frac{1}{\alpha_{\rm s}-1}}, \\ &\alpha_{\rm s} \left(\frac{2}{\sqrt{3}} \, M_{\rm s2} |\omega|\right)^{\frac{1}{\alpha_{\rm s}}} - (\alpha_{\rm s}-1) \left(\frac{M_{\rm s2}}{M_{\rm s1}}\right)^{\frac{1}{\alpha_{\rm s}-1}}, \\ &\frac{2}{\sqrt{3}} \, M_{\rm s1} |\omega| \geq \left(\frac{M_{\rm s2}}{M_{\rm s1}}\right)^{\frac{1}{\alpha_{\rm s}-1}} \end{split}$$

The ice flow law (Equation (6)) was confirmed in special studies of the bubbly-ice densification process in polar ice sheets (Lipenkov and others, 1997; Salamatin and others, 1997). In mechanical tests (Duval and Castelnau, 1995) and in laboratory experiments on the air-hydrate formation (Salamatin and others, 1998b) performed at relatively high temperatures, ice appeared to be somewhat softer than in natural polar conditions. We use here, however, the in situ ice rheology as determined by Lipenkov and others (1997) for the Vostok region. In accordance with Salamatin and others (1998b), air hydrate, when treated as a plastic material, was found to be at least one order harder than ice. This is in good agreement with the direct experimental measurements by Stern and others (1996) performed for methane clathrate hydrates. Plausible values of the rheological parameters in Equations (6) and (7) estimated by Lipenkov and others (1997) and Salamatin and others (1998b) are given in Table 1.

Equations (4) and (7) for the idealized hard spherical hydrate shell around the bubble in the A-type conversion process represent the limiting case of the lowest rates of the bubble compression and, hence, the bubble-to-hydrate transformation. At the same time, taking $\omega_h=0$, instead of Equation (4b) for the B-type conversion, we assume that the growing hydrate crystal is freely squeezed into the bubble and does not hinder the bubble-compression and ice-deformation processes. Thus, we come to the upper bound of the conversion rates.

Initial conditions

The system of simultaneous Equations (1)-(7) needs to be supplemented with additional relations which determine the initial values of characteristics describing the conversion of a reference bubble to clathrate air hydrate after the hydrate-crystal nucleation on the bubble wall at t = 0. Let us designate by subscript "0" the bubble volume $V_{\rm b0}$ (bubble radius $r_{\mathrm{b0}})$ and the bubble (load) pressure p_{l0} just before the nucleation; the gas composition is identified with \bar{Z}_{N_2} , \bar{Z}_{O_2} . Due to relatively high rates of air and water diffusion through clathrate hydrate almost immediately after nucleation, the hydrate crystal, growing on the bubble wall, reaches the size at which the initial supersaturation is removed and the bubble pressure drops from p_{10} to the dissociation pressure $p_{\rm d}$. Gas composition of the bubble also changes from $\bar{Z}_{N_2}, \bar{Z}_{O_2}$ to Z_{N_2}, Z_{O_2} . This momentary process is too fast to be noticeably influenced by the air diffusion from neighboring inclusions and compressive deformation of the ice. Thus, the mass-conservation law for the bubble air (Salamatin and others, 1998b) determines the initial volumes of the air bubble and the hydrate crystal after its nucleation:

$$V_{b|t=0} = V_{b0} \left[\frac{p_{ha} - p_{l0} \left(1 - \frac{\rho_{hw}}{\rho_{l}} \right)}{p_{ha} - p_{d} \left(1 - \frac{\rho_{hw}}{\rho_{l}} \right)} \right],$$

$$V_{h|t=0} = V_{b0} \left[\frac{p_{l0} - p_{d}}{p_{ha} - p_{d} \left(1 - \frac{\rho_{hw}}{\rho_{l}} \right)} \right],$$
(8)

where $p_{\rm d}$ corresponds to the initial bubble-air composition $Z_{\rm N_2}, Z_{\rm O_2}$ which, being in equilibrium with the hydrate crystal (see Equations (l)), satisfies the following transcendental equation:

$$Z_{N_{2}} - \frac{\lambda Z_{N_{2}}(1 - Z_{N_{2}})}{1 - \lambda Z_{N_{2}}} \left\{ 1 - \frac{p_{d}}{p_{l0}} \left[\frac{p_{ha} - p_{l0} \left(1 - \frac{\rho_{hw}}{\rho_{i}} \right)}{p_{ha} - p_{d} \left(1 - \frac{\rho_{hw}}{\rho_{i}} \right)} \right] \right\} = \bar{Z}_{N_{2}}.$$

$$(9)$$

The load pressure in the ice matrix does not remain constant as the transforming bubble—hydrate complex sinks into the ice-sheet thickness:

$$p_{\rm l} = p_{\rm l0} + L_{\rm p}t. {10}$$

The rate of loading $L_{\rm p}$ is proportional to the ice accumulation rate b, that is $L_{\rm p} \sim g \rho_{\rm i} b$ (g is the gravity acceleration), but should be corrected to account for the thinning of the overlying ice stratum in the vertical direction due to global ice-sheet dynamics (e.g. Salamatin and others, 1997).

3. RESULTS OF SIMULATIONS

Finite-difference and iteration methods were employed to solve non-linear differential Equations (1)–(10) numerically. A special interactive computer system has been developed in the DELPHI visual programming medium to perform computational experiments and to study the process of the conversion of an air bubble to air-hydrate crystal in transition zones of ice sheets. This software is used here to simulate the air-hydrate formation process in Antarctica at Vostok station.

Preliminary notes on model parameters

The most uncertain but principal parameters of the model (Equations (1–10)) are the permeation (self-diffusion) coefficients of nitrogen and oxygen in ice. There are as yet no reliable data on their values reported and available from direct measurements, especially at the extreme conditions typical of polar regions. However, preliminary estimations can be made. The mechanism of the diffusion in ice is thought to be an interstitial one and for water molecules was studied by Goto and others (1986). Additional experiments were conducted to measure the diffusion coefficients of hydrogen (Strauss and others, 1994) and noble gases (Satoh and others, 1996). Ikeda and others (1999) extrapolated these data to N_2 and O₂ at 263 K by calculating the potential barriers of the gas-water molecular interactions, which are the proxy for the activation energy of the gas molecule jumps in ice lattice. They also estimated the concentrations of N_2 and O_2 in ice from the Van der Waals diameters of the gas molecules using the gas solubility measurements by Satoh and others (1996). Combining these results, we arrive at a rough prediction of

Table 2. Present-day initial environmental conditions of airhydrate formation within transition zone in Antarctic ice sheet at Vostok station

Parameter	Location in transition zone			
	I. Beginning	II. Middle	III. End	
H (m)	600	800	1100	
T (K)	220	222	225	
p_{10} (MPa)	5.1	6.9	9.6	
$L_{\rm p}~({ m MPa~a}^{-1})$	0.0002	0.00019	0.00018	
$r_{ m b0}~({ m mm})$	0.02	0.045	0.05	
$V_{ m b}~(10^4{ m mm}^3)$	0.34	3.8	5.2	
$n_{ m b}$	0.95	0.45	0.05	
$ar{Z}_{ ext{N}_2}$	0.79	0.84	0.92	
$ar{X}_{ ext{N}_2}$	0.67	0.75	0.79	
$z_{ m g}$	0.95	0.92	0.9	
$ au_{ m C}({ m a})^*$	1300	400	50	
	(200)	(30)	(3)	
$\tau_{\rm E} ({ m ka})$	0.5	2.3	5.0	

^{*} The first line represents the compression time-scale in the conversion of type A; the second line (figures in parentheses) corresponds to the conversion of type B.

the diffusive permeation coefficients of N_2 and O_2 in ice at 263 K for dissociation pressures $p_{\rm dN_2}=11.8$ MPa and $p_{\rm dO_2}=8.9$ MPa, respectively: $D_{\rm N_2}\sim 1.0\times 10^{-5}$ mm² a⁻¹ (3.4 × 10⁻¹⁹ m² s⁻¹) and $D_{\rm O_2}\sim 4.0\times 10^{-5}$ mm²a⁻¹ (1.3 × 10⁻¹⁸ m² s⁻¹). Thus $D_{\rm O_2}$ is noticeably greater than $D_{\rm N_2}$. The in situ diffusive transport of air molecules in ice was indirectly estimated by Uchida and others (1994c) from the growth rate of air-hydrate crystals in the Antarctic ice sheet. They found the air permeation coefficient to be of the order of 10^{-7} to 10^{-6} mm² a⁻¹ ($\sim 10^{-20}$ to 10^{-19} m² s⁻¹) at 233 K and 10 MPa. This agrees with Ikeda and others' (1999) data if the difference in temperature is taken into account.

Recent observations of the gas fractionation in Vostok ice cores (Ikeda and others, 1999) imply that the typical time $\tau_{\rm E}$ of the diffusive gas-mass exchange between the air bubble transforming to air-hydrate crystal and its neighbors, coexisting bubbles and hydrates, at the beginning of the transition zone at 220 K could be comparable with the compression (air-hydrate formation) time $\tau_{\rm C}$. Hence, for $n_{\rm b} \sim 1$ and for the time-scale ratios discussed in the introduction, at the beginning of the transition, $\tau_{\rm E}$ should be 10^5 times larger than the diffusion time $\tau_{\rm D}$ in air hydrate. The gas-mass exchange time-scale $\tau_{\rm E}$ for an air-hydrate crystal can be derived from Equations (3) and (5), as

$$\tau_{\rm E} \sim \frac{{r_{\rm b0}}^2 p_{\rm l0} p_{\rm dN_2}}{3 p_{\rm iw} D_{\rm N_2} [n_{\rm b} (p_{\rm l0} - p_{\rm dN_2}) + p_{\rm dN_2} | \bar{Z}_{\rm N_2} - \bar{X}_{\rm N_2}]]} \ . \ \ (11)$$

In accordance with Salamatin and others (1998b),

$$au_{
m D} \sim rac{{r_{
m b0}}^2 {p_{
m l0}}^2}{3 p_{
m ba} D (p_{
m l0} - p_{
m dN_2})} \ ,$$

where the diffusive mass-transfer coefficient in air hydrate D for the Vostok transition zone at 220 K is about $10^{-2} \,\mathrm{mm^2\,a^{-1}}$. Thus, the corresponding values of the self-diffusion coefficients of the air constituents in ice should be of the order of $10^{-7} \,\mathrm{mm^2\,a^{-1}}$ ($\sim 10^{-21} \,\mathrm{m^2\,s^{-1}}$). The latter estimate is consistent with the above predictions by Uchida and others (1994c) and Ikeda and others (1999) and is confirmed below (see Table 1) by model constraining.

The present-day environmental conditions of the air-hydrate crystal growth on bubble wall after its nucleation at different depth levels (h) at the beginning, in the middle and at the end of the transition zone at Vostok are presented in Table 2. Direct optical-microscope observations of the Vostok ice cores by Lipenkov (1989) showed that, in spite of the hydrostatic compression, the mean radius $\bar{r}_{\rm b}$ of air bubbles within the transition zone remains substantially constant, slightly varying from 0.06-0.065 mm in the upper part to 0.045-0.05 mm at the end. This becomes possible due to the preferential, selective clathration of bubbles of minimal, "critical" size: $r_{\rm b} \sim 0.02-0.025$ mm. The number fraction of such bubbles rapidly decreases with depth, thus increasing the initial dimensions of air inclusions involved in clathration. Our choice of the initial bubble radii (r_{b0}) in Table 2 follows this tendency.

The rate of loading $L_{\rm p}$ has been estimated in accordance with the mean ice-accumulation rate at Vostok station, $b\approx 24$ mm a⁻¹, determined over the past 22 years (Barkov and Lipenkov, 1996).

The number concentration of inclusions N_0 is taken equal to $0.8~{\rm mm}^{-3}~(r_{\rm c}\sim 0.67~{\rm mm})$ in all simulations.

Computational experiments and discussion

The time-scale of the gas-mass exchange, $\tau_{\rm E}$, given by Equation (11), depends on the bubble number fraction n_b and is proportional to the squared radius of the air bubble converting to air-hydrate crystal. It has minimal values in the upper part of the transition zone, where the air-hydrate formation (compression) time $\tau_{\rm C}$ reaches its maximum and where air bubbles have initial atmospheric gas composition and dominate in the inclusion ensemble ($n_b \approx 1$). Accordingly, first computational tests showed that at the beginning of the transition zone the initial gas composition of a growing hydrate, determined by Equations (8) and (9), rapidly changes (due to the selective diffusion of oxygen from the neighboring bubbles) to a certain new one, distinguished as $\bar{X}_{N_2}, \bar{X}_{O_2}$, which further remains constant during the formation and development of the crystal unless the air composition in the neighboring bubbles itself is changed. At the end of the transformation, when the amount of air in the bubble becomes small, the ratio between the righthand side flux terms in Equations (2) and (3) is equal to \bar{X}_{N_2} :

$$q_{\rm N_2} = \bar{X}_{\rm N_2} (q_{\rm N_2} + q_{\rm O_2}) \,. \label{eq:N_2}$$

Substituting \bar{X}_{N_2} and \bar{X}_{O_2} for X_{N_2} and X_{O_2} in Equations (5), we obtain a theoretical estimate for the permeation-coefficients ratio valid at the beginning of the transition:

$$\frac{D_{\rm O_2}}{D_{\rm N_2}} = \frac{M_{\rm N_2}}{M_{\rm O_2}} \left(\frac{p_1 \bar{Z}_{\rm N_2}}{p_{\rm dN_2} \bar{X}_{\rm N_2}} - 1 \right) / \left(\frac{p_1 \bar{Z}_{\rm O_2}}{p_{\rm dO_2} \bar{X}_{\rm O_2}} - 1 \right). \quad (12$$

For present-day conditions at Vostok station, at about 650 m depth the load pressure is $p_{\rm l}\approx 5.6$ MPa, and the dissociation pressures at temperature $T\approx 220\,\rm K$ are $p_{\rm dN_2}\approx 3.6$ MPa and $p_{\rm dO_2}\approx 2.6$ MPa. For atmospheric air trapped in bubbles $\bar{Z}_{\rm N_2}/\bar{Z}_{\rm O_2}\approx 3.7$, while, in accordance with Ikeda and others (1999), the N₂/O₂ ratio in air hydrates is $\bar{X}_{\rm N_2}/\bar{X}_{\rm O_2}\approx 2.0$. Therefore, Equation (12) predicts

$$D_{\rm O_2}/D_{\rm N_2} \approx 2.1$$
.

This relationship is hereinafter fixed in all computer simulations. It is additionally validated in section 4. However, it should be noted that this estimate is rather sensitive to feasible changes in depth (load pressure) and N_2/O_2

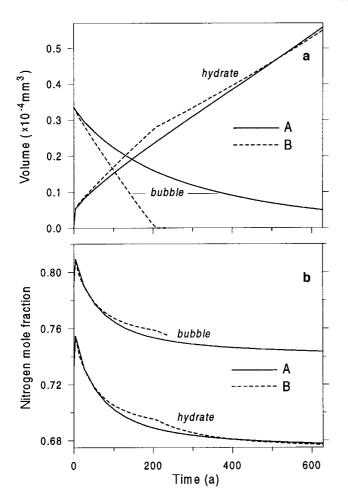


Fig. 2. Air-bubble and air-hydrate characteristics vs time simulated for the beginning of the transition zone at Vostok (600 m depth). (a) Volumes, $V_{\rm b}, V_{\rm h}$. (b) Nitrogen mole fractions, $Z_{\rm N_2}, X_{\rm N_2}$. A and B indicate type of bubble-to-clathrate conversion.

ratios. For instance, at the 600 m level, where $p_{\rm l}\approx 5.1$ MPa, the $D_{\rm O_2}/D_{\rm N_2}$ ratio would be 2.5 for the same degree of the fractionation and would range from 1.8 to 2.6 if $\bar{X}_{\rm N_2}/\bar{X}_{\rm O_2}$ varies within $\pm 5\%$ limits.

The post-nucleation transformation of an air bubble to air-hydrate crystal in polar ice sheets, being mainly controlled by the bubble compression, does not noticeably depend on the gas-mass exchange between the semi-bubble and the neighboring air and hydrate inclusions. On the other hand, the latter process is primarily responsible for the total size and the growth rate of the air hydrates after the conversion. Approximately, at the beginning of the transition, where $n_{\rm b} \approx 1$, the bulk air-mass flux from bubbles to hydrates is determined by the initial supersaturation, $p_{\rm l} - p_{\rm d}$, and the mean size of the air hydrates is related to their mean age. Ice-core analysis shows that the corresponding radius, $r_{\rm h}$, of the hydrate crystals at 700 m depth at Vostok is about $0.036 \,\mathrm{mm} \, (V_{\rm h} = 1.95 \times 10^{-4} \,\mathrm{mm}^3)$. They are mainly formed below 620 m, and their mean age can be estimated as 1.5-2 ka at the present-day accumulation rate of about 24 mm a⁻¹. The diffusive permeation coefficients of nitrogen and oxygen presented in Table 1 are obtained (with accuracy not worse than $\pm 10\%$) to satisfy the latter constraint: $D_{\rm N_2} \approx 4.5 \times 10^{-8} \, {\rm mm^2 \, a^{-1}} \, (1.4 \times 10^{-21} \, {\rm m^2 \, s^{-1}}), \ D_{\rm O_2} \approx 9.5 \times 10^{-8} \, {\rm mm^2 \, a^{-1}} \, (3.0 \times 10^{-21} \, {\rm m^2 \, s^{-1}}),$ corresponding to a temperature of 220 K (dissociation pressures $p_{\rm d\,N_2} \approx 3.6\,{\rm MPa}$ and $p_{\rm d\,O_2} \approx 2.6$ MPa). Figure 2 shows the described process of

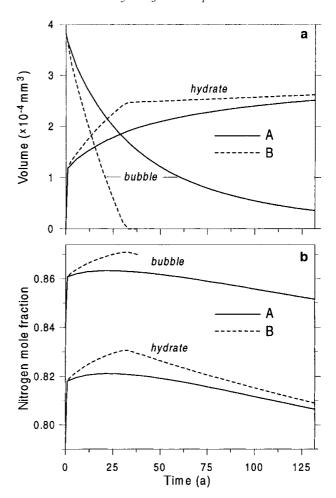


Fig. 3. Air-bubble and air-hydrate characteristics vs time simulated for the middle of the transition zone at Vostok (800 m depth). (a) Volumes, $V_{\rm b}, V_{\rm h}$. (b) Nitrogen mole fractions, $Z_{\rm N_2}, X_{\rm N_2}$. A and B indicate type of bubble-to-clathrate conversion.

air-hydrate crystal growth and the temporal changes in the gas composition of the developing bubble—hydrate complex at the beginning of the transition zone at Vostok. The limiting difference between types A and B of the post-nucleation transformation of an air bubble to clathrate air hydrate can be clearly seen.

The deduced estimates of the self-diffusion coefficients of the air components in ice agree well with the preliminary ones discussed in the previous subsection. Based on these results obtained for 220 K as well as on the predictive calculations performed by Ikeda and others (1999) for 263 K, we can attempt to evaluate the self-diffusion activation energy $Q_{\rm d}$ defined by the conventional relation:

$$D_{\rm s} = D_{\rm s}^* \exp \left[\frac{Q_{\rm d}}{R_{\rm g}} \left(\frac{1}{T_*} - \frac{1}{T} \right) \right],$$

where subscript "s" designates either oxygen (s = O_2) or nitrogen (s = N_2), and permeation coefficient D_s^* corresponds to the reference temperature T_* and linearly depends on pressure (gas concentration). In general, we should have assumed different activation energies for the air components, but limited confidence in the extrapolation procedures of Ikeda and others (1999) at 263 K inclines us not to do this. Finally, on average, taking into account the difference in dissociation pressures at different temperatures, we obtain $Q_d = 50 \pm 3 \, \text{kJ} \, \text{mol}^{-1}$, which is very close

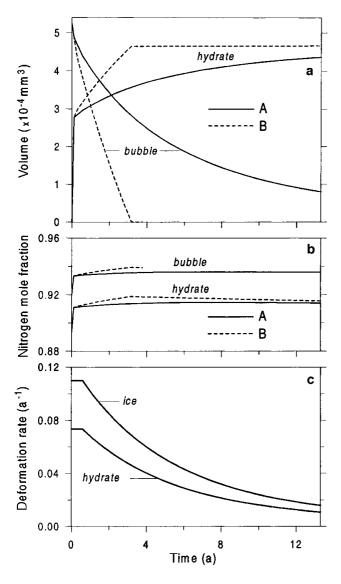


Fig. 4. Air-bubble and air-hydrate characteristics vs time simulated for the end of the transition zone at Vostok (1100 m depth). (a) Volumes, $V_{\rm b}, V_{\rm h}$. (b) Nitrogen mole fractions, $Z_{\rm N_2}, X_{\rm N_2}$. A and B indicate type of bubble-to-clathrate conversion. (c) Compressive deformation rates of the air-hydrate coat $(\omega_{\rm h})$ and surrounding ice $(\omega_{\rm i})$ in case A.

to the self-diffusion activation energy of water interstitial in ice (Goto and others, 1986). This estimate is sufficiently reliable to account for relatively small temperature variations within the transition zones, for instance, 220–225 K at Vostok. In the case of Uchida and others (1994c), at 233 K and 10 MPa, the N₂- and O₂-permeation coefficients would be 5.7×10^{-7} mm² a⁻¹ (1.8×10^{-20} m² s⁻¹) and 1.6×10^{-6} mm² a⁻¹ (5.2×10^{-20} m² s⁻¹), respectively, which corresponds to the lower bound of the range estimated in the cited study.

Figures 3 and 4 present the principal features of the airhydrate formation process in the middle and at the end of the transition zone for present-day (Holocene) climatic conditions (see Table 2). From Salamatin and others (1998b) the rate of bubble shrinking increases with depth (see Figs 2a–4a) following the increase in the initial relative supersaturation of bubbles, $p_{10}/p_{\rm d}$, from 1.5 to 2.3. The values of the typical compression time $\tau_{\rm C}$ given in Table 2 refer to the moment at which the volume of the disappearing air bubble becomes 100 times smaller than that of the growing hydrate. The time-scale of the air-hydrate formation decreases from

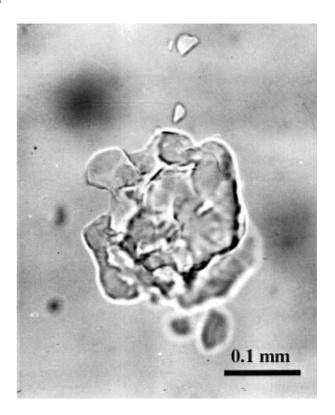


Fig. 5. Clathrate air-hydrate inclusion composed of several splinter-like pieces in the fresh Vostok ice core recovered from 850 m depth.

1300 a (or 200 a) at the beginning to 50 a (or 3 a) at the end of the transition zone for the conversion of type A (or B). On the other hand, the typical time $\tau_{\rm E}$ for the gas-composition variation in a growing air hydrate, calculated in Table 2 in accordance with Equation (11), increases considerably with depth from 500 to 5000 a. As mentioned, this is for two reasons: (1) larger bubbles transform to air hydrates at greater depths, and (2) the decrease in bubble number fraction reduces the background concentration of air constituents dissolved in the ice. As a result, first air hydrates which appear at the beginning of the transition at Vostok acquire a large quantity of air from surrounding bubbles and completely change their gas composition due to the selective diffusion of oxygen during the period of their formation (see Fig. 2b). However, even in the middle of the transition zone (Fig. 3b), and especially at its end (Fig. 4b), the gas composition of the growing air-hydrate crystal remains practically constant in the course of the transformation, while the main changes in the composition of air hydrates formed in the middle of the transition take place in the post-conversion period. The continuous gas-mass exchange between the air hydrates and coexisting bubbles along with nucleation of new air hydrates play the principal role in the gas fractionation (Ikeda and others, 1999) within the transition zone. This phenomenon is discussed in the next section.

Another peculiarity of the post-nucleation conversion of air bubbles to air hydrates can be distinguished in Figures 2a–4a. Because of the high supersaturation of bubbles, a large quantity (30–60%) of air in them almost immediately after nucleation is converted to hydrate crystals. Figure 4c shows that for the A-type transformation the compressive deformation rates of the ice and the hydrate layers, surrounding the bubbles, reach their maximum values at this moment, these values being especially high in the deeper part of the trans-

ition zone. This may cause destruction of the hydrate shells, followed by further recrystallization of different pieces. At the same time, at high supersaturation the conversion of type B can also start with simultaneous nucleation of several hydrate crystals in a single air bubble. Thus, the probability of finding such "broken" (split into separate parts) air-hydrate crystals is proportional both to the local supersaturation of bubbles and to the rate of the hydrate nucleation in a unit of ice volume. The latter tends to zero as the number of bubbles diminishes at the end of the transition zone, decreasing the above probability. This may explain the experimental observation that air-hydrate crystals of several similar-sized splinter-like pieces (see Fig. 5) are common for the Vostok ice cores mainly in the middle of the transition zone.

4. GAS FRACTIONATION IN THE TRANSITION ZONE

Simplified mass-balance model

The averaged nitrogen and oxygen mass fluxes through the ice matrix toward air hydrates $(q_{\mathrm{N}_2}^{(\mathrm{h})}, q_{\mathrm{O}_2}^{(\mathrm{h})})$ and bubbles $(q_{\mathrm{N}_2}^{(\mathrm{b})}, q_{\mathrm{O}_2}^{(\mathrm{b})})$ are direct analogues of Equations (5):

$$\begin{split} q_{\mathrm{N}_{2}}^{(\mathrm{h})} &= 4\pi \gamma \bar{r}_{\mathrm{h}} D_{\mathrm{N}_{2}} \left(\frac{p_{\mathrm{l}}}{p_{\mathrm{d}\,\mathrm{N}_{2}}} \bar{Z}_{\mathrm{N}_{2}} - \bar{X}_{\mathrm{N}_{2}} \right), \\ q_{\mathrm{O}_{2}}^{(\mathrm{h})} &= 4\pi \gamma \bar{r}_{\mathrm{h}} D_{\mathrm{O}_{2}} \frac{M_{\mathrm{O}_{2}}}{M_{\mathrm{N}_{2}}} \left(\frac{p_{\mathrm{l}}}{p_{\mathrm{d}\,\mathrm{O}_{2}}} \bar{Z}_{\mathrm{O}_{2}} - \bar{X}_{\mathrm{O}_{2}} \right), \\ q_{\mathrm{N}_{2}}^{(\mathrm{b})} &= -4\pi (1 - \gamma) \bar{r}_{\mathrm{b}} D_{\mathrm{N}_{2}} \left(\frac{p_{\mathrm{l}}}{p_{\mathrm{d}\,\mathrm{N}_{2}}} \bar{Z}_{\mathrm{N}_{2}} - \bar{X}_{\mathrm{N}_{2}} \right), \\ q_{\mathrm{O}_{2}}^{(\mathrm{b})} &= -4\pi (1 - \gamma) \bar{r}_{\mathrm{b}} D_{\mathrm{O}_{2}} \frac{M_{\mathrm{O}_{2}}}{M_{\mathrm{N}_{2}}} \left(\frac{p_{\mathrm{l}}}{p_{\mathrm{d}\,\mathrm{O}_{2}}} \bar{Z}_{\mathrm{O}_{2}} - \bar{X}_{\mathrm{O}_{2}} \right), \end{split}$$
(13)

where $\bar{r}_{\rm h}$ and $\bar{r}_{\rm b}$ are the mean radii of air-hydrate crystals and bubbles, respectively, assumed to be much less than the cell radius $r_{\rm c}$ (see Fig. 1).

The mass conservation of air components implies that

$$n_{\rm b}q_{\rm N_2}^{(\rm b)} + (1-n_{\rm b})q_{\rm N_2}^{(\rm h)} = 0, \quad n_{\rm b}q_{\rm O_2}^{(\rm b)} + (1-n_{\rm b})q_{\rm O_2}^{(\rm h)} = 0$$

and determines the parameter γ as

$$\frac{\gamma}{1-\gamma} = \frac{\bar{r}_{\rm b}}{r_{\rm h}} \frac{n_{\rm b}}{1-n_{\rm b}} \ .$$

For the transition zone at Vostok the ratio $\bar{r}_{\rm b}/\bar{r}_{\rm h} \approx 1.5 \pm 0.3$ and does not differ much from unity. Hence, the approximation $\gamma \approx n_{\rm b}$ used in the previous section seems reasonable.

It is important to remember that the typical time $\tau_{\rm E}$ of the gas-composition variations in a single air-hydrate crystal significantly exceeds the time-scale of the bubble-to-hydrate conversion ($\tau_{\rm C}$) throughout the transition zone, except maybe for its beginning at Vostok (see Table 2). This means that the gas composition of a newly formed air hydrate ($X_{\rm N_2}, X_{\rm O_2}$), at least in the deeper part of the transition zone, is initially close to that of the air bubble ($\bar{Z}_{\rm N_2}, \bar{Z}_{\rm O_2}$).

Thus, the mass-balance equation for nitrogen in gaseous (bubble) phase can be written in the following form:

$$\frac{\mathrm{d}}{\mathrm{d}t}(n_{\rm b}p_{\rm l}V_{\rm b}\bar{Z}_{\rm N_2}) = n_{\rm b}p_{\rm iw}q_{\rm N_2}^{\rm (b)} + p_{\rm l}V_{\rm b}\bar{Z}_{\rm N_2}\frac{\mathrm{d}n_{\rm b}}{\mathrm{d}t},$$

which yields

$$\frac{\mathrm{d}}{\mathrm{d}t}(p_{\mathrm{l}}V_{\mathrm{b}}\bar{Z}_{\mathrm{N}_{2}}) = p_{\mathrm{iw}}q_{\mathrm{N}_{2}}^{(\mathrm{b})}.$$

Combining this equation with that written for oxygen, we obtain the principal relation which determines the rate

of the bubble-gas composition changes (gas fractionation) in the transition zone:

$$\frac{p_{\rm l}V_{\rm b}}{p_{\rm iw}}\frac{{\rm d}\bar{Z}_{\rm N_2}}{{\rm d}t} = \bar{Z}_{\rm O_2}q_{\rm N_2}^{\rm (b)} - \bar{Z}_{\rm N_2}q_{\rm O_2}^{\rm (b)}.$$
 (14)

To construct a complete model of the gas fractionation, Equation (14) should be considered together with the analogous one for \bar{X}_{N_2} which would include the additional gasmass exchange term proportional to the rate of air-hydrate nucleation dn_b/dt . To solve this system of simultaneous equations, we would need to know the kinetics of the nucleation itself. The latter problem is beyond the scope of this paper, although its solution would allow us to constrain the gas-fractionation model by the direct Raman spectra measurements (e.g. Ikeda and others, 1999) and to infer more valid estimates of the self-diffusion coefficients D_{N_2} , D_{O_2} . It is proposed that these questions be studied in future. Nevertheless, even at the present stage of our knowledge it is useful to examine Equations (13) and (14) on the basis of scale analysis to derive the typical time τ_{F} of the bubble-gas fractionation in transition zones of ice sheets:

$$\tau_{\rm F} \sim \frac{\bar{r}_{\rm b}^2 p_{\rm l} p_{\rm dO_2} M_{\rm N_2}}{3 p_{\rm iw} D_{\rm O_2} M_{\rm O_2} (p_{\rm l} - p_{\rm dO_2})} \ . \tag{15}$$

Naturally it has the same structure and is of the same order as τ_E at the beginning of the transition.

Let τ_Z be the typical time of the hydrate nucleation covered by the transition zone. The principal conclusion can be deduced at this stage: a noticeable gas fractionation within the transition zone in an ice sheet takes place only if $\tau_F \ll \tau_Z$, i.e. when the rate of the air-hydrate nucleation is much less than the gas-fractionation rate.

Model validation on Vostok data

We can easily estimate $\tau_{\rm F}$ from Equation (15) for conditions in the transition zone at Vostok (see Tables 1 and 2). For the depth range 800–1100 m the gas-fractionation time for bubbles $\tau_{\rm F}\sim300$ a. Further, in accordance with Salamatin and others

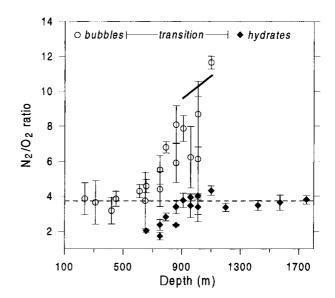


Fig. 6. Comparison of direct measurements of N_2/O_2 ratios in air bubbles and air hydrates in the Vostok ice core (Ikeda and others, 1999), with theoretical prediction of the N_2/O_2 ratio in air bubbles at the end of the transition zone (bold line). Error bars correspond to the standard deviations of the measurements performed in the different inclusions of the same ice sample. Dashed line indiates atmospheric N_2/O_2 ratio (3.7).

(1998a), the ice age is 28 ka at the beginning of the transition zone (550 m) and 94 ka at the end (1250 m). This 700 m stratum was formed in the cold glacial period when ice-accumulation rate was approximately half the present rate. Hence, the age of the ice layer that has now reached the end of the transition zone was about 60 ka at the beginning. Soon after that (approximately 10 ka), the Holocene warming started, with increased ice-accumulation rates, and the conversion of all bubbles to air hydrates took about 30–35 ka. This estimate of $\tau_{\rm Z}$ for central Antarctica is much larger than $\tau_{\rm E}$ and is two orders of magnitude larger than that of $\tau_{\rm F}$.

Thus, at Vostok, the bubble-gas fractionation in the deeper part of the transition zone, as $n_{\rm b}$ decreases, becomes a quasistationary process. Its principal limiting step is the nucleation of air hydrates. It determines the rate of the mean air-hydrate gas-composition evolution from its initial oxygen-enriched state to that close to atmospheric air. The gas composition in air bubbles simply follows the changing load (bubble) pressure to correspond with the gas composition of air hydrates and would be constant if the latter two factors remained unchanged. Mathematically this means that the lefthand side of Equation (14) becomes negligibly small compared with the gas-mass fluxes $q_{\rm N_2}^{\rm (b)}$ and $q_{\rm O_2}^{\rm (b)}$.

Therefore,

$$ar{Z}_{{
m O}_2} q_{{
m N}_2}^{({
m b})} - ar{Z}_{{
m N}_2} q_{{
m O}_2}^{({
m b})} pprox 0 \,,$$

and we come directly to the following relation:

$$\frac{D_{\rm O_2}}{D_{\rm N_2}} = \frac{M_{\rm N_2}}{M_{\rm O_2}} \left(\frac{p_{\rm l}}{p_{\rm dN_2}} - \frac{\bar{X}_{\rm N_2}}{\bar{Z}_{\rm N_2}} \right) / \left(\frac{p_{\rm l}}{p_{\rm dO_2}} - \frac{\bar{X}_{\rm O_2}}{\bar{Z}_{\rm O_2}} \right), \tag{16}$$

which is an analogue of Equation (12) at the end of the transition zone.

Laboratory Raman spectroscopic studies by Ikeda and others (1999) showed that below 850 m the gas composition of air hydrates in the Vostok ice cores is close to atmospheric: $\bar{X}_{\rm N_2}/\bar{X}_{\rm O_2}\approx 3.7$. Thus, if we fix the self-diffusion coefficients ratio $D_{\rm O_2}/D_{\rm N_2}\approx 2.1$, as determined before, then it is possible to use Equation (16) to evaluate the N₂/O₂ ratios in air bubbles. In the depth range 900–1100 m, the load pressure varies from 7.8 to 9.6 MPa, while the dissociation pressures are $p_{\rm dN_2}\approx 4.0$ –4.25 MPa and $p_{\rm dO_2}\approx 2.9$ –3.1 MPa. This leads to an N₂/O₂ ratio in bubbles of 9.6–10.9. The direct measurements by Ikeda and others (1999) give $\bar{Z}_{\rm N_2}/\bar{Z}_{\rm O_2}\approx 8.7$ –11.6. The obvious agreement between the theoretical estimates and the experimental data (see Fig. 6) tends to support the validity of the developed model.

Discussion: application to Greenland ice-sheet conditions

It might be interesting to apply the above theory to the analysis of air-hydrate formation conditions in the Greenland ice sheet, studied through the GRIP and GISP2 projects. The transition zone in the Greenland ice cores is found at 1000–1500 m depth (Pauer and others, 1999) with ice ages of about 5.3–9.4 ka (Meese and others, 1997). It covers the Holocene period, with rather stable temperatures around 240 K and ice-accumulation rates close to 250 mm a $^{-1}$ (Cuffey and Clow, 1997). Thus, the duration of the total phase transition from air bubbles to air hydrates (the typical time of nucleation) is $\tau_{\rm Z} \sim 4$ ka, i.e. one order of magnitude less than in the Vostok region in Antarctica.

To understand whether a noticeable gas fractionation could occur in central Greenland, we should estimate the corresponding time-scale τ_F , using Equation (15). The depth profiles of the

hydrate number concentration and total gas-volume concentration along the GRIP ice core (Pauer and others, 1997, 1999) allow us to calculate the mean bubble radius $\bar{r}_{\rm b} \sim 0.1$ –0.15 mm. The dissociation pressure $p_{\rm dO_2} \approx 4.9$ MPa, the self-diffusion coefficient $D_{\rm O_2} \approx 1.7 \times 10^{-6} \ \rm mm^2 \, a^{-1}$, and for load pressures $p_{\rm l}\sim 10$ MPa we get $\tau_{\rm F}\sim 200$ –400 a. Thus, the gas-fractionation rates (time-scales $\tau_{\rm F}$ and $\tau_{\rm E}$) in central Greenland for present-day (Holocene) climatic conditions are comparable with those at Vostok, but at much (10 times) higher nucleation rates. As a result the number of oxygen- enriched hydrates and the mean degree of gas fractionation sharply decrease at the beginning of the transition zone. The variance of the gas composition $(N_2/O_2 \text{ ratios})$ in the air hydrates increases as τ_E becomes comparable with $\tau_{\rm Z}$ in the deeper part of the transition zone. Therefore, we come to the following conclusion. A significant gas fractionation, on average, is ruled out for air hydrates in the Greenland ice cores and might be detected only (1) as oxygen enrichment in rare hydrate crystals formed at the very beginning of the transition, or (2) as nitrogen enrichment in rare hydrate crystals newly formed at the end of the transition zone. Indeed, N₂/O₂ ratios as low as 2.63 and as high as 4.49 were observed in the air hydrates by Pauer and others (1997). More evident (systematic and statistically valid) nitrogen enrichment might be expected in the air bubbles in the deepest part of the transition zone, but such data are so far not available.

5. CONCLUSION

On the basis of previous theoretical studies (Salamatin and others, 1998b), a mathematical model of the post-nucleation conversion of air bubbles to clathrate air-hydrate crystals is elaborated in application to polar ice-sheet conditions. The limiting step of the phase transformation is the hydrostatic compression of the ice-hydrate-air system. Two possible types, A and B, of hydrate-crystal growth on the bubble wall, schematically depicted in Figure 1, are considered and represent the limiting (lower and upper) bounds of the transformation rates. Special emphasis is put on modelling the gasmass exchange between coexisting air bubbles and air hydrates within the transition zones. All simulations are aimed at analysis and interpretation of the Vostok ice-core data.

The typical time for the post-nucleation conversion decreases along the transition zone at Vostok from 1300 a (or 200 a) at the beginning to 50 a (or 3 a) at the end, depending on the type of hydrate growth (A or B). Because of the high initial supersaturation of bubbles, a large quantity (30-60%) of air in them is converted to hydrate crystals almost immediately after nucleation. The compressive deformation rates of the ice and the hydrate layers, coating the bubble walls in the A-type conversion, reach their maximum values at this moment, with especially high values in the deeper part of the transition zone. This may cause destruction of the hydrates. In the B-type conversion, at high supersaturation of bubbles, several air-hydrate crystals can simultaneously nucleate on the wall of a single bubble. Both situations may equally explain the experimental observation that air-hydrate crystals of several similar-sized splinter-like pieces are common for the Vostok ice cores in the middle of the transition zone, where the relative rate of the nucleation is maximal.

The model of the selective diffusive transport of the air constituents from air bubbles to hydrate crystals through the ice matrix has been constrained by the data of optical-micro-

scope observations of the bubble and hydrate ensembles (Lipenkov, 1989), as well as by the Raman spectroscopic measurements of their N₂/O₂ ratios (Ikeda and others, 1999). The ratio between the diffusive permeation coefficients of oxygen and nitrogen is found to be $D_{\rm O_2}/D_{\rm N_2}\approx 2.1$, while the values of the coefficients themselves at the Vostok temperature of about 220 K are determined as $D_{\rm N_2} \approx 4.5 \times 10^{-8} \, {\rm mm}^2 \, {\rm a}^{-1}$ $(1.4 \times 10^{-21} \, {\rm m}^2 \, {\rm s}^{-1})$ and $D_{\rm O_2} \approx 9.5 \times 10^{-8} \, {\rm mm}^2 \, {\rm a}^{-1}$ $(3.0 \times 10^{-21} \, {\rm m}^2 \, {\rm s}^{-1})$ m² s⁻¹). The air-permeation (self-diffusion) activation energy is estimated to be $Q_{\rm d} \approx 50\,{\rm kJ~mol}^{-1}$. The gas-fractionation time-scale at Vostok, $\tau_{\rm F} \sim 300$ a, appears to be two orders of magnitude less than the typical time of the air-hydrate nucleation $\tau_{\rm Z} \sim 30{\text -}35$ ka. The condition for the extreme gas fractionation, $\tau_{\rm F} \ll \tau_{\rm Z}$, is satisfied, and a simplified model of a quasistationary gas-mass flux from air bubbles to air hydrates can be used to predict the total N₂/O₂ ratios in the last bubbles at the end of the transition zone at Vostok. Good agreement between the theoretical calculations and the Raman spectra data confirms the validity of the model. Application of the developed theory to the GRIP and GISP2 ice cores shows that significant gas fractionation, on average, is ruled out for air hydrates in central Greenland. A noticeable (statistically valid) nitrogen enrichment might be observed there only in the last air bubbles at the end of the transition zone.

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