

Ion motion effects on the generation of short-cycle relativistic laser pulses during radiation pressure acceleration

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Abstract

The effects of ion motion on the generation of short-cycle relativistic laser pulses during radiation pressure acceleration are investigated by analytical modeling and particle-in-cell simulations. Studies show that the rear part of the transmitted pulse modulated by ion motion is sharper compared with the case of the electron shutter only. In this study, the ions further modulate the short-cycle pulses transmitted. A 3.9 fs laser pulse with an intensity of $1.33 \times 10^{21} \text{ W cm}^{-2}$ is generated by properly controlling the motions of the electron and ion in the simulations. The short-cycle laser pulse source proposed can be applied in the generation of single attosecond pulses and electron acceleration in a small bubble regime.

Keywords: radiation pressure acceleration; short-cycle pulses; particle-in-cell simulations.

With the rapid development of laser technology^[1–3], the use of ultra-intense laser irradiation on ultra-thin foils has been studied for various fields ranging from fast ignition for inertial confinement fusion^[4, 5], medical therapy^[6, 7], and laboratory astrophysics^[8], to the generation of high-energy particle sources^[1]. However, prepulses or laser pulses with slowly increasing fronts may lead to premature ionization of the target, and significant expansion of the plasma sheet occurs before the amplitude peak of the pulse arrives^[9, 10]. These events jeopardize the relativistic interaction of the ultra-thin target. Thus, high-contrast^[9–20] and short-duration laser pulses^[21, 22] are needed.

Plasma mirrors may be a feasible method by which to solve these problems. Using a double plasma mirror^[23], the laser contrast may be improved to $\sim 10^{-12}$ at the picosecond time scale^[12]. A 30 nm thick carbon foil irradiated by such a high-contrast laser at an intensity of $\sim 7 \times 10^{19} \text{ W cm}^{-2}$ can produce a 185 MeV carbon ion beam. A few-cycle laser pulse with an intensity up to $3 \times 10^{20} \text{ W cm}^{-2}$ may also be generated when a laser irradiates an ultra-thin foil^[22]. In this method, the pulse duration and intensity mainly depend on the laser profile and foil conditions. Generally, the intensity

of few-cycle laser pulses is limited in conventional optical methods^[21] because of the relatively low damage threshold of the optical components and other problems. However, no laser intensity due to material damage would be limited by this method, because this process only involves laser–plasma interactions, like the plasma grating^[24].

Ref. [22] discusses the generation of a short-cycle laser pulse. It is also necessary to discuss an explicit explanation of the difference and the progress. Ref. [22] considers in detail the transmission of the incident laser pulse in constant conditions. There the electron layer is assumed to be at rest, and the ion motion effects are not considered. In fact the ion motion can significantly modulate the transmission of the laser. For example, the Doppler effect on the mirror is enhanced because the velocities of the ions initially in the middle of the foil are higher than that of the compressed electron layer (CEL) during the hole-boring stage. The rear part of the incident laser pulse can be reflected in this case.

In this letter, the effects of ion motion on the generation of short-cycle relativistic laser pulses are investigated by analytical modeling and particle-in-cell (PIC) simulations. The generation of a near single-cycle laser pulse has been obtained in the simulations, and the corresponding theoretical analysis has been discussed^[22]. However, all the solutions are based on static conditions, where the motions of the CEL and ions are not included. In fact the ion motion can

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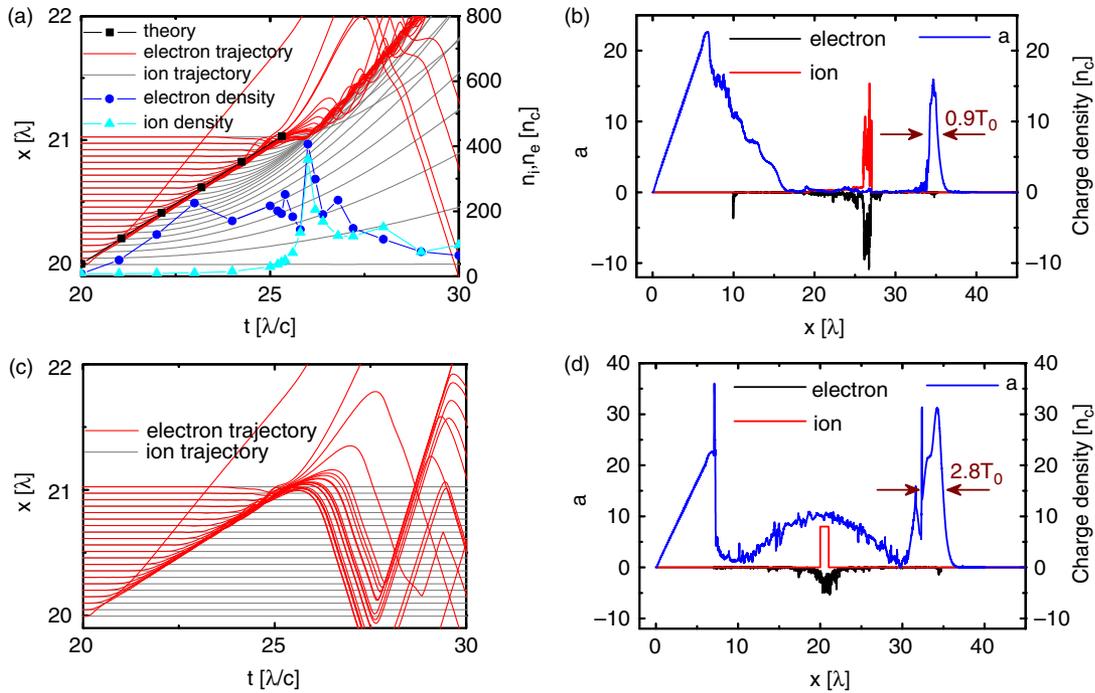


Figure 2. 1D PIC simulation results for $a_0/t_{\text{up}} = 7.35$ ($a_0 = 30$ and $t_{\text{up}} = 4.08T_0$), $n_0 = 8n_c$, and $l_0 = 1.03\lambda$. (a) Electron and proton trajectories and their density peaks versus time. (b) Laser profile (blue solid line) and charge density of electrons (black solid line) and ions (red solid line) at $t = 40T_0$ for the case of moving ions. (c) Electron and proton trajectories and (d) laser profile (blue solid line) and charge density of electrons (black solid line) and ions (red solid line) at $t = 40T_0$ for the case of ions at rest.

at this point [Figure 2d]. Compared with Figures 2b and 2d, the ion motion has an important role in modulating the rear part of the incident laser pulse.

The simulations above show that the ion motion is important for the generation of short-cycle laser pulses. The main reason is that the re-entering of the ions into the CEL at the back side of the foil can further reflect the rear part of the laser pulse. In the case of Figure 2a, the laser pulse begins to transmit the foil as the CEL slightly disperses at the back side of the foil. Then the ions re-enter into the CEL, and a double-layer reflecting mirror is produced. In this stage, the Doppler effect on the mirror is enhanced because the velocities of the ions initially in the middle of the foil are higher than that of the CEL during the hole-boring stage. At the end, the rear part of the incident laser pulse is reflected.

The dynamics of the electrons and ions are investigated to obtain insights into the generation of short-cycle lasers. The action of the electric field in the CEL E_{x2} (Figure 1) is initially neglected for ion acceleration because the velocity of the CEL is large^[35]. Moreover, the ions do not catch the CEL when this layer arrives at the back side of the target^[35]. Here, the unrelativistic interaction of the laser pulse with the linearly increasing front in the hole-boring stage is considered to simplify our study. A time-dependent theory model can be used to deal with the relativistic interaction of the laser with any pulse profile in Ref. [38].

For electrons, a uniform velocity of the CEL can be obtained for a laser with a linearly increasing front in

simulations^[35]. The electrons are first accelerated by the ponderomotive force of the CP laser pulse within a very short time, and then a balance between the laser pressure and the electrostatic forces appears. Then the swept electrons pile up to form a dense skin-depth layer by the laser pressure and electrostatic forces. We define this skin-depth layer as the CEL. The equation of motion of a perfectly reflecting mirror, $dp/dt = P d\sigma$, can be used to describe the motion of the CEL, where p is the momentum of the mirror element, $d\sigma$ is the element of area of the mirror and normal to the mirror surface, and P is the radiation pressure^[39]. In this paper, we focus on the case that the ions move after the electrons during the hole-boring stage because the laser-pulse front is very sharp. The laser energy is largely contained in the charge separation field during this stage. The velocities of the electron layer and ions are not relativistic. Simulations have shown that the surface of the CEL moves roughly at a constant velocity; if the laser-pulse front is linearly increasing and short enough, there must be a balance between the electrostatic force and the laser pressure force^[35],

$$2(\pi n_0 v_{\text{CEL}} t)^2 = 2a^2 \frac{1 - v_{\text{CEL}}}{1 + v_{\text{CEL}}}, \quad (1)$$

where the normalized amplitude of the laser on the moving CEL surface $a = (a_0/t_{\text{up}})(t - v_{\text{CEL}}t)$, and $l = v_{\text{CEL}}t$. Here, v_{CEL} , t_{up} , and n_0 are normalized by c , λ/c , and $n_c = \omega_L^2 m_e / 4\pi e^2$, respectively. Although the linear amplitude

increases, a part of the electrons is moving while another part is stationary; most electrons move around a averaged velocity during the hole-boring stage. Such averaged velocity of the skin-depth reflecting mirror has been verified in the simulations^[38]. Equation (1) describes the velocity of the CEL for the case that the laser is totally reflected by the plasma. The transmission of the laser pulse is not considered during the hole-boring stage in our case. Based on Equation (1), a uniform velocity of the CEL ($v_{\text{CEL}} \approx 0.194c$) is obtained for $a_0 = 30$, $t_{\text{up}} = 4.08T_0$, $n_0 = 8n_c$, and $l_0 = 1.03\lambda$, which is consistent with the simulation result in Figure 2a.

For ions, the velocity for the ion initially at rest at x_{10} ($0 < x_{10} < d$) can be approximated by^[35]

$$v_{i1} = \frac{2\pi q_i E_0 x_{10}}{m_i d} t_1, \quad (2)$$

where x_{10} , x_{i1} , and d are normalized by λ , and the ion mass m_i and charge q_i are normalized by m_e and e , respectively. In addition, the action time t_1 is normalized by λ/c . $E_0 = 2\pi n_0 d$ is the maximum electrostatic field of charge depletion, which is normalized by $e/m_e \omega_L c$. $E_0 = 2\pi n_0 l_0$ is obtained when the CEL is assumed to be superthin ($d \approx l_0$)^[35]. For the case shown in Figure 2a, $E_0 \approx 52$ for $n_0 = 8n_c$, and $l_0 = 1.03\lambda$.

The velocity of the ions initially at rest in the middle of the foil ($x_{10} = d/2$) $v_{i1} \sim 0.24c$ is obtained using Equation (2). Here, $t_1 \sim 0.5d/v_{\text{CEL}}$ is used. Ions initially resting in the middle of the foil run fast during the sharp-front laser interaction at the end of the hole-boring stage^[35]. The CEL quickly catches up to these ions after the hole-boring stage because the electron mass is much smaller than the ion mass. Therefore, we can assume that $v_{\text{CEL}} \sim 0.24c$ at this point, which is larger than the velocity of the CEL ($\sim 0.194c$) during the hole-boring stage. The Doppler effect parameter $(c - v_{\text{CEL}})/(c + v_{\text{CEL}})$ is thus reduced by the ion motion. Moreover, the reflection of the laser pulse is enhanced. The rear part of the transmitted pulse can be further modulated by the ion motion compared with the case of the electron shutter only, which is verified by the simulations in Figures 2a–2d.

From the discussion above, two conditions are required for the generation of an intense short-cycle transmitted pulse. First, the peak of the incident pulse must arrive at the back surface when the CEL disperses, thereby generating a short-duration transmitted pulse with higher amplitude. This condition is simply an approximation because the exact amplitude of the transmitted pulse is not considered. Second, the ions must not catch up to the CEL during the hole-boring stage. Otherwise all of the laser pulses may be reflected.

For the first condition, the laser and foil parameters are as follows:

$$a_{\text{open}} > \frac{a_0}{t_{\text{up}}} \left(\frac{l_0}{v_{\text{CEL}}} - l_0 \right), \quad (3)$$

where a_{open} is the peak amplitude of the incident laser pulse that may open the electron shutter. For a certain laser amplitude $a_{\text{open}} = a_0$ and gradient a_0/t_{up} , the incident laser

can transmit if $l_0 < t_{\text{up}} \cdot v_{\text{CEL}}/(1 - v_{\text{CEL}})$ according to Equation (3). Here, v_{CEL} is calculated using Equation (1). The laser peak cannot reach the back side of the target when $l_0 \gg t_{\text{up}} \cdot v_{\text{CEL}}/(1 - v_{\text{CEL}})$. In this case, the incident laser is completely reflected, and no transmitted laser pulse can be generated. For the case shown in Figure 2, $l_0 < 0.98\lambda$ is obtained for $a_0/t_{\text{up}} = 7.35$ ($a_0 = 30$ and $t_{\text{up}} = 4.08T_0$), and $n_0 = 8n_c$, which is consistent with the simulation results (Figure 3). Figure 3 shows that the transmitted laser pulse with $a_0 > 30$ is generated for $l_0 < 0.98\lambda$. A nearly single-cycle laser pulse is generated for $l_0 = 1.03\lambda$, as shown in Figure 3.

For the second condition, the laser and foil parameters are^[35]

$$l_0 < \frac{1}{\pi} \sqrt{\frac{2m_i}{q_i n_0}} v_{\text{CEL}}, \quad (4)$$

where $l_0 = \sqrt{2m_i/q_i n_0} v_{\text{CEL}}/\pi$ corresponds to the case where ions are initially in the middle of the foil and the CEL reaches the back surface of the foil at the same time. The incident laser is completely reflected if $l_0 \geq \sqrt{2m_i/q_i n_0} v_{\text{CEL}}/\pi$ ^[35], which is verified by the simulation results in Figure 3. $l_0 \geq 1.32\lambda$ is obtained for $a_0/t_{\text{up}} = 7.35$ ($a_0 = 40.4$ and $t_{\text{up}} = 5.5T_0$), and $n_0 = 8n_c$. Figure 3b shows that no transmitted laser pulse is generated for $l_0 = 1.32\lambda$. A thinner foil ($l_0 = 1.2\lambda$) is simulated for the same laser and foil parameters to verify the condition of Equation (4). Figure 3c shows that a quasi-single-cycle transmitted pulse is generated, where the ions do not catch up the CEL as the CEL leaves the back surface of the foil. This indicates that ion motion indeed affects the transmitting of the laser pulse. Here, a higher density ($n_0 = 200n_c$) of the foil is also theoretically estimated. The velocity of the CEL $v_{\text{CEL}} \sim 0.07c$ is obtained for an ultra-intense laser pulse ($a_0/t_{\text{up}} \sim 54$) based on Equation (1). Then $l_0 < 0.1\lambda$ can be obtained according to Equation (4). And $a_{\text{open}} > 57.4$ is obtained for $l_0 = 0.08\lambda$ according to Equation (3). In Figure 3c, the duration of the transmitted pulse is much shorter than the laser period when the foil thickness further increases ($l_0 > 1\lambda$). The frequency broadening should be taken into account when the duration of the transmitted pulse is much shorter than the laser period, which is not considered in this paper.

Different simulations of carbon ions are also performed to verify the theory. The velocity of the CEL $v_{\text{CEL}} \sim 0.2c$ is obtained for $a_0/t_{\text{up}} \sim 15$ and $n_0 = 15n_c$ according to Equation (1). $l_0 < 1.4\lambda$ is calculated based on Equation (4) for C^{6+} ions, where $m_i = 12$ and $q_i = 6$. Here, the foil thickness $l_0 \sim 1.25\lambda$ is used in the simulation. And $a_0 = 80$ is chosen to satisfy the condition $a_{\text{open}} > 75$ according to Equation (3). Figure 4 shows that a near single-cycle laser pulse is generated, indicating that the conditions [Equations (3) and (4)] can be used to deal with different ion masses. However, a smaller value of m_i/q_i is suggested for the generation of a short-cycle transmitted laser pulse. The

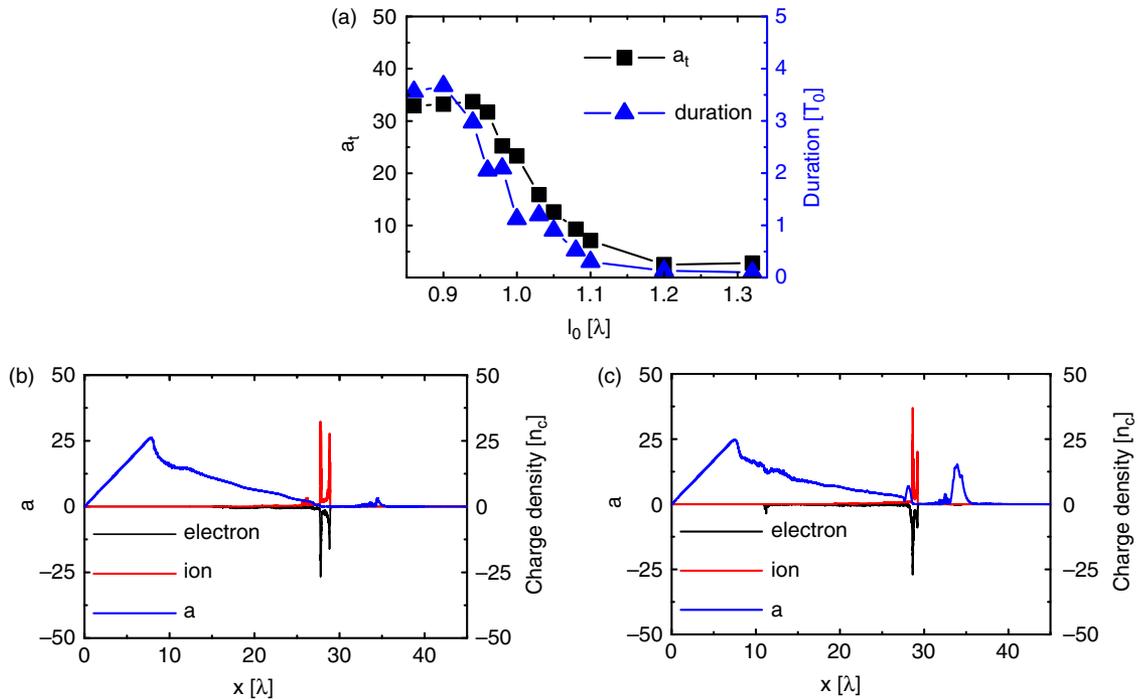


Figure 3. (a) Amplitude peak a_t (black square) and duration (blue triangle) of transmitted pulses versus foil thickness l_0 . For the incident laser, $a_0/t_{up} = 7.35$ ($a_0 = 30$ and $t_{up} = 4.08T_0$). The foil density is $n_0 = 8n_c$. Laser profile (blue solid line) and charge density of electrons (black solid line) and ions (red solid line) for $a_0/t_{up} = 7.35$ ($a_0 = 40.4$ and $t_{up} = 5.5T_0$) and (b) $l_0 = 1.32\lambda$, (c) 1.2λ .

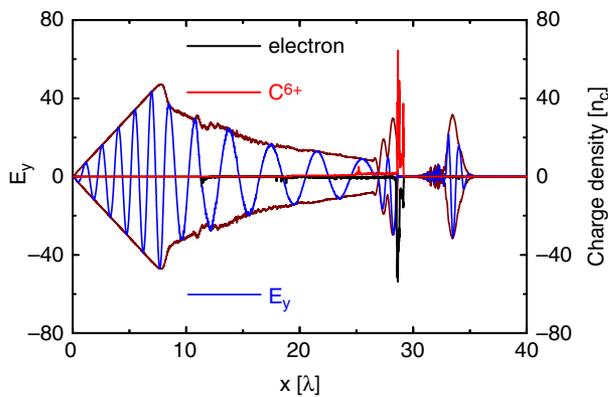


Figure 4. Laser profile E_y (blue solid line) and charge density of electrons (black solid line) and C^{6+} ions (red solid line) for $a_0/t_{up} = 15$ ($a_0 = 80$ and $t_{up} = 6T_0$). The foil density is $n_0 = 15n_c$, and the foil thickness is $l_0 = 1.25\lambda$.

main reason is that a thinner foil is obtained according to Equation (4), and some multidimensional effects and instabilities can be reduced to a certain extent for a thinner foil.

A clean laser pulse is used to simplify the model in this work. In fact, the effect of a laser prepulse is always critical for a thin foil and it may alter the conditions [see Equations (3) and (4)]. A density gradient at the front or back side of the foil produced by the prepulse must be considered if the laser contrast is not ultra-high^[9, 10]; such a condition is not considered in this work.

To verify our theoretical model, we also carried out 2D PIC simulations. The same parameters as in the 1D PIC simulations [see Figures 2a and 2b], which include $a_0 = 30$, $t_{up} = 4.08T_0$, $n_0 = 8n_c$, and $l_0 = 1.03\lambda$, are used in the 2D case. The laser pulse has a trapezoidal shape profile ($4.08T_0 - 1.5T_0 - 4.08T_0$) in time and is a transverse four-order super Gaussian, $I \sim \exp[-(r/r_0)^4]$, where $r_0 = 10\lambda$. The simulation region is a $50\lambda \times 50\lambda$ box (3000 cells along the laser axis x , and 3000 cells transversely along axis y). The plasma foil occupies the region from $x = 20\lambda$ to 21.03λ and from $x = -22.5\lambda$ to 22.5λ . Ten macroparticles are available in each cell. Absorbing boundaries are used for both electromagnetic waves and macroparticles.

Figure 5 shows the electron and ion distributions and the laser profile in the (x, y) plane at $t = 40T_0$. From the laser axial profiles at $y = 0\lambda$, a nearly single-cycle transmitted pulse is produced. The laser duration is about 3.9 fs (FWHM), and the amplitude peak is $a_t \sim 22$ ($I_0 = 2a_t^2 \times 1.37 \times 10^{18} \text{ W cm}^{-2} = 1.33 \times 10^{21} \text{ W cm}^{-2}$). Compared with the results from 1D simulations in Figure 2b, the duration and amplitude peak are larger in the 2D case, which is mainly attributed to foil deformation and self-focusing of the laser in the ‘hole-boring’ stage. Figure 5 shows that the transmitted laser amplitude decreases sharply from its peak because ions catch the slightly dispersed electron layer at the end of the hole-boring stage. Here, the ion motion further modulates the rear part of the incident laser pulse. In addition, the transverse width is also reduced when the

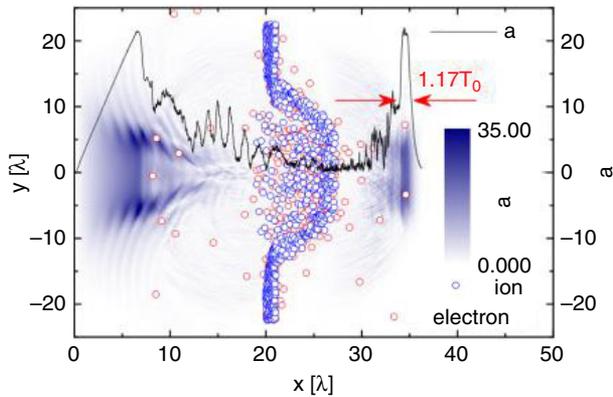


Figure 5. Electron (red circle) and ion (blue circle) distribution and the laser profiles in the (x, y) plane for foils with $n_0 = 8n_c$ and $l_0 = 1.03$ irradiated by CP laser pulses with $a_0/t_{\text{up}} = 7.35$ ($a_0 = 30$ and $t_{\text{up}} = 4.08T_0$) at $t = 40T_0$. The axial laser profiles at $y = 0$ are denoted by the black solid lines.

laser mainly passes through the foil. Figure 4 further shows that the transverse width is reduced from 10λ (FWHM) to about 6λ (FWHM). The front and back portions of the pulse are reflected after laser–foil interaction. About 92% of the energy of the incident laser pulse is reflected, as shown in Figure 5.

In conclusion, the effects of ion motion on the generation of a short-cycle relativistic laser pulse are investigated by analytical modeling and PIC simulations. 1D PIC simulations show that the ion shutter can further modulate the transmitted short-cycle pulse compared with the case of the electron shutter only. Two conditions are theoretically proposed to generate short-cycle transmitted laser pulses, which are proven by the simulations. A near single-cycle (3.9 fs) laser pulse with an intensity of $1.33 \times 10^{21} \text{ W cm}^{-2}$ is generated by properly controlling the electron and ion shutters in 2D PIC simulations.

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