CORRIGENDA

Roll-spun knots

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K. Motegi has kindly pointed out that the Lemma in Section 4 of the paper is incorrect. (The assertion in Case 1 on p. 95 that the sewing map of E(K) is periodic is false.) Hence Theorem 6 is unproven. However, we have a weaker result.

Theorem 6'. Let K be a knot in S^3 , and suppose that K is not a torus knot. For any non-zero integer m, the m-roll spun knot $\rho^m K$ of K cannot be obtained as $\tau^n K$ for any integer n.

Proof. Suppose that $\rho^m K \sim \tau^n K$ for some n. We may assume that $n \geq 0$. By Theorem 3, we have $n \neq 0$. Also, by Theorem 2, $n \neq 1$. The argument given in the paper shows that K(0) is a Seifert fibred manifold with orientable orbit manifold. From the argument in the paper we then obtain that K is a fibred knot whose closed monodromy is isotopic to a periodic homeomorphism. Let F be a fibre of K. Then by Proposition 2, $\rho^m K$ is a fibred knot with fibre W (see Section 2). Note that the closed fibre \hat{W} is a Haken Seifert fibred manifold and $H_1(\hat{W}; Z) \cong Z^{2g(F)}$. Let $\Sigma_n(K)$ be the n-fold cyclic branched cover of K. Since $\pi_1(S^4 - \rho^m K) \cong \pi_1(S^4 - \tau^n K)$, we have $\pi_1(\hat{W}) \cong \pi_1(\Sigma_n(K))$ by considering the commutator subgroup of both sides. Also, $\Sigma_n(K)$ is irreducible since $\pi_1(\hat{W})$ is indecomposable relative to free products. Hence, by [2], corollary 6.5, $\hat{W} \cong \Sigma_n(K)$.

Now we have n>2, since $H_1(\hat{W};Z)\cong Z^{2g(F)}$. From the tables of Dunbar[1], if the n-fold cyclic branched cover of a knot is a Seifert fibred manifold for some n>2 then either the knot is a torus knot or it is the figure-eight knot and n=3. But $H_1(\Sigma_3(\text{figure-eight});Z)\cong Z_4\oplus Z_4$. Hence, K would be a torus knot, contradicting our assumption.

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REFERENCES

- [1] W. Dunbar. Geometric orbifolds. Rev. Mat. U. Complutense Mad. 1 (1988), 67-99.
- [2] F. Waldhausen. On irreducible 3-manifolds which are sufficiently large. Ann. of Math. 87 (1968), 56-88.