

Character tables of certain finite simple groups

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$M(22)$ is the sporadic simple group discovered by Fischer in 1969. The character tables of $M(22)$ and the simple groups $PSU(5, 2)$, $PSU(6, 2)$, $PS\Omega^+(6, 3)$ and $PS\Omega(7, 3)$ are presented. Only a brief description of the methods used to determine the tables is given.

1. Notation

$O(n, q)$ is the group of orthogonal $n \times n$ matrices over the field $GF(q)$. The exponent + or - distinguishes between the two orthogonal forms when n is even. + denotes the group of maximal Witt index $n/2$.

$\Omega(n, q)$ denotes the kernel of the spinorial norm on the orthogonal group $O(n, q)$.

$U(n, q)$ is the group of unitary $n \times n$ matrices over the field $GF(q)$.

As usual S denotes special and P projective. Hence $PS\Omega^+(6, 3)$ is a simple group of order $2^7 \cdot 3^6 \cdot 5 \cdot 13$.

Let

$$\chi_i^{(5)}, i = 1, \dots, 47; \left(\begin{array}{l} \chi_i^{(6)}, i = 1, \dots, 46; \beta_i, i = 1, \dots, 29; \\ \chi_i^{(7)}, i = 1, \dots, 58; \chi_i^{(22)}, i = 1, \dots, 65 \end{array} \right)$$

be the irreducible characters of

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$PSU(5, 2)$ ($PSU(6, 2)$; $PS\Omega^+(6, 3)$; $PS\Omega(7, 3)$; $M(22)$) .

$M(22)$ is the sporadic simple group of order $2^{17} \cdot 3^9 \cdot 5^2 \cdot 7 \cdot 11 \cdot 13$ discovered and described by Fischer [1]. D denotes the conjugacy class of 3-transpositions in $M(22)$, [1].

$P^* = C_{M(22)}(d)$ where d is a given element in D .

$P^*/\langle d \rangle \cong PSU(6, 2)$, [1].

2. Conjugacy classes in the classical groups

The conjugacy classes of $U(5, 2)$, $U(6, 2)$, $O^+(6, 3)$ and $O(7, 3)$ were determined directly from the main theorems in the paper of Wall [2] on the conjugacy classes in the unitary, symplectic and orthogonal groups. The restriction to the associated simple groups was easy in the case of the unitary groups. Some difficulties were encountered in dealing with the orthogonal groups as it was necessary to calculate the spinorial norm of the elements in each centralizer.

3. The character tables

The character tables of the five groups were determined following the steps (1) to (3).

(1) Several permutation characters of representations on subgroups of small index were found. The associated irreducible characters were found by restricting the permutation characters to subgroups with known character tables and decomposing into irreducible characters on these subgroups.

(2) A large number of generalized characters were found by inducing characters from subgroups with known character tables and forming tensor products of the irreducibles already found.

(3) A matrix of the character scalar products was formed (using an Elliot 4100 computer). The known irreducibles were stripped off the generalized characters. The scalar products naturally led to sets of linear equations which were solved to yield the other irreducible characters.

The following representations and subgroups were used in (1) and (2).

Group	Subgroup	degree	Representation	Character
$PSU(5, 2)$	$PSU(4, 2) \times C$	176	Isotropic points in $PG(5, 4)$	$\chi_1^{(5)} + \chi_5^{(5)} + \chi_{16}^{(5)}$
		165	Non-isotropic points in $PG(5, 4)$	$\chi_1^{(5)} + \chi_6^{(5)} + \chi_{16}^{(5)}$
		297	Totally isotropic points in $PG(5, 4)$	$\chi_1^{(5)} + \chi_{18}^{(5)} + \chi_{16}^{(5)}$
$PSU(6, 2)$	$PSU(5, 2)$	672	Non-isotropic points in $PG(6, 4)$	$\chi_1^{(6)} + \chi_3^{(6)} + \chi_6^{(6)}$
		693	Isotropic points in $PG(6, 4)$	$\chi_1^{(6)} + \chi_4^{(6)} + \chi_6^{(6)}$
	$PSU(4, 9) \cong P\Omega^-(6, 3)$	2816		$\chi_1^{(6)} + \chi_2^{(6)} + \chi_4^{(6)} + \chi_{11}^{(6)} + \chi_{14}^{(6)}$
$P\Omega^+(6, 3) \cong PSL(4, 3)$		40	Points in $PG(4, 3)$	$\beta_1 + \beta_4$
		130	Lines in $PG(4, 3)$	$\beta_1 + \beta_4 + \beta_8$
	$P\Omega(5, 3)$	234		$\beta_1 + \beta_2 + \beta_8 + \beta_5 + \beta_6$
$P\Omega(7, 3)$	$\Omega^-(6, 3)$	351	Points of length 1 in $PG(7, 3)$	$\chi_1^{(7)} + \chi_5^{(7)} + \chi_6^{(7)}$
	$S\Omega^-(6, 3)$	702		$\chi_1^{(7)} + \chi_5^{(7)} + \chi_6^{(7)} + \chi_2^{(7)} + \chi_{10}^{(7)}$
	$\Omega^+(6, 3)$	378	Points of length 2 in $PG(7, 3)$	$\chi_1^{(7)} + \chi_6^{(7)} + \chi_7^{(7)}$
	$S\Omega^+(6, 3)$	756		$\chi_1^{(7)} + \chi_6^{(7)} + \chi_7^{(7)} + \chi_4^{(7)} + \chi_{10}^{(7)}$
	$PSp(6, 2)$	3159		$\chi_1^{(7)} + \chi_5^{(7)} + \chi_8^{(7)} + \chi_{25}^{(7)}$
$M(22)$	P^*	3510	The conjugacy class D	$\chi_1^{(22)} + \chi_3^{(22)} + \chi_7^{(22)}$
	$P\Omega(7, 3)$	14080		$\chi_1^{(22)} + \chi_3^{(22)} + \chi_9^{(22)}$

4. Conjugacy classes in $M(22)$

$PSU(6, 2)$ is a factor group of P^* by a central involution. Hence characters χ of $M(22)$ may be restricted to P^* and determine an associated character $\bar{\chi}$ of $PSU(6, 2)$. The restrictions to $PS\Omega(7, 3)$ and $PSU(6, 2)$ of the permutation representations of $M(22)$ of degrees 3510 and 14080 were found. From this information the fusion of elements represented in P^* and $PS\Omega(7, 3)$ was determined. This determined the conjugacy classes up to a few alternatives which were decided while calculating the characters.

References

- [1] Bernd Fischer, "Finite groups generated by 3-transpositions", (to appear).
- [2] G.E. Wall, "On the conjugacy classes in the unitary, symplectic and orthogonal groups", *J. Austral. Math. Soc.* 3 (1963), 1-62.

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Appendix: The tables

The following symbols are used for complex integers:

$$\begin{aligned}
 \omega & \quad \omega^3 = 1 \\
 \gamma & \quad \gamma^2 = -5 \\
 \sigma & \quad \sigma^2 = -8 \\
 \rho & \quad \rho = 3 + 6\omega \\
 \alpha & \quad \alpha^2 + \alpha = 3 \\
 & \quad \alpha^* = \alpha + 1 \\
 \beta & \quad \beta + \bar{\beta} = -1 \\
 & \quad \beta\bar{\beta} = 3 \\
 \lambda_1 & \quad \lambda_1 = \epsilon + \epsilon^3 + \epsilon^9 \\
 \lambda_2 & \quad \lambda_2 = \epsilon^{10} + \epsilon^{12} + \epsilon^4 \\
 \lambda_3 & \quad \lambda_3 = \epsilon^2 + \epsilon^5 + \epsilon^6 \\
 \lambda_4 & \quad \lambda_4 = \epsilon^{11} + \epsilon^7 + \epsilon^8
 \end{aligned}
 \left. \right\} \text{where } \epsilon^{13} = 1 .$$

Each character table extends over several pages. In the first four such tables, with characters of $PSU(5, 2)$, $PSU(6, 2)$, $PS\Omega^+(6, 3)$, and $PS\Omega(7, 3)$, the columns are headed by the order of an element in the relevant conjugacy class and the order of its centralizer. In the last table, for $M(22)$, this information is listed separately at the end.

Order of centralizer												
	$2^{10} \cdot 3^5 \cdot 5 \cdot 11$	$2^{10} \cdot 3^4$	$2^9 \cdot 3^2$	$2^7 \cdot 3^2$	$2^7 \cdot 3$	$2^5 \cdot 3$	2^4	$2^6 \cdot 3^5 \cdot 5$	$2^6 \cdot 3^5$	$2^6 \cdot 3^3$	$2^6 \cdot 3^3$	$2^5 \cdot 3^2$
el.	1	2	2	4	4	4	8	3	3	6	6	6
$\chi_i^{(5)}$	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}	c_{11}	c_{12}
χ_1	1	1	1	1	1	1	1	1	1	1	1	1
χ_2	10	-6	2	2	-2	-2	0	-5	-5	3	3	-1
χ_3	11	-5	3	3	-1	-1	1	-1-6ω	5+6ω	-1+2ω	-3-2ω	-1-2ω
χ_4	11	-5	3	3	-1	-1	1	5+6ω	-1-6ω	-3-2ω	-1+2ω	1+2ω
χ_5	44	12	-4	4	4	0	0	14	14	6	6	2
χ_6	55	23	7	-1	-1	3	-1	10	10	2	2	-2
χ_7	55	7	-1	7	3	-1	1	-20-15ω	-5+15ω	-4-7ω	3+7ω	-4-3ω
χ_8	55	7	-1	7	3	-1	1	-5+15ω	-20-15ω	3+7ω	-4-7ω	-1+3ω
χ_9	66	18	10	2	-2	2	0	-15-9ω	-6+9ω	1-ω	2+ω	1+3ω
χ_{10}	66	18	10	2	-2	2	0	-6+9ω	-15-9ω	2+ω	1-ω	-2-3ω
χ_{11}	110	-2	-10	6	-6	2	0	-25	-25	7	7	-1
χ_{12}	110	30	6	6	2	2	0	-25-30ω	5+30ω	-9-6ω	-3+6ω	-1-2ω
χ_{13}	110	30	6	6	2	2	0	5+30ω	-25-30ω	-3+6ω	-9-6ω	1+2ω
χ_{14}	110	-34	6	-2	2	-2	0	-10-15ω	5+15ω	-2+ω	-3-ω	2+ω
χ_{15}	110	-34	6	-2	2	-2	0	5+15ω	-10-15ω	-3-ω	-2+ω	1-ω
χ_{16}	120	24	8	8	0	0	0	30	30	6	6	2
χ_{17}	165	-27	5	5	5	-3	1	30	30	6	6	2
χ_{18}	176	-16	16	0	0	0	0	-4	-4	-4	-4	4
χ_{19}	220	-36	-4	4	-4	0	0	40+30ω	10-30ω	-8-10ω	2+10ω	2ω
χ_{20}	220	-36	-4	4	-4	0	0	10-30ω	40+30ω	2+10ω	-8-10ω	-2-2ω
χ_{21}	220	-4	12	4	4	0	0	10+30ω	-20-30ω	2+6ω	-4-6ω	-2+2ω
χ_{22}	220	-4	12	4	4	0	0	-20-30ω	10+30ω	-4-6ω	2+6ω	-4-2ω
χ_{23}	264	-24	-8	8	0	0	0	-24-54ω	30+54ω	-8+2ω	-10-2ω	-2ω
χ_{24}	264	-24	-8	8	0	0	0	30+54ω	-24-54ω	-10-2ω	-8+2ω	2+2ω

Table 1, Part 1: Characters of $PSU(5, 2)$

el.	Order of centralizer	2 ¹⁰ .3 ⁵ .5.11	2 ¹⁰ .3 ⁴	2 ⁹ .3 ²	2 ⁷ .3 ²	2 ⁷ .3	2 ⁵ .3	2 ⁴	2 ⁶ .3 ⁵ .5	2 ⁶ .3 ⁵	2 ⁶ .3 ³	2 ⁶ .3 ³	2 ⁵ .3 ²	
		1	2	2	4	4	4	4	3	3	6	6	6	
$\chi_i^{(5)}$		c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}	c_{11}	c_{12}	
χ_{25}		320	-64	0	0	0	0	0	-40	-40	8	8	0	
χ_{26}		330	-6	2	10	-2	2	0	$60+45\omega$	$15-45\omega$	$-4-11\omega$	$7+11\omega$	$4+\omega$	
χ_{27}		330	-6	2	10	-2	2	0	$15-45\omega$	$60+45\omega$	$7+11\omega$	$-4-11\omega$	$3-\omega$	
χ_{28}		440	88	8	-8	0	0	0	-10	-10	-2	-2	2	
χ_{29}		440	-40	8	8	0	0	0	$-40+30\omega$	$-70-30\omega$	$8+6\omega$	$2-6\omega$	2ω	
χ_{30}		440	-40	8	8	0	0	0	$-70-30\omega$	$-40+30\omega$	$2-6\omega$	$8+6\omega$	$-2-2\omega$	
χ_{31}		495	-81	15	-1	-1	-1	-1	-45\omega	$45+45\omega$	3\omega	$-3-3\omega$	3ω	
χ_{32}		495	-81	15	-1	-1	-1	-1	$45+45\omega$	-45\omega	$-3-3\omega$	3ω	$-3-3\omega$	
χ_{33}		495	63	-9	-1	-5	-1	1	$45+45\omega$	-45\omega	$-3-3\omega$	3ω	$-3-3\omega$	
χ_{34}		495	63	-9	-1	-5	-1	1	-45\omega	$45+45\omega$	3\omega	$-3-3\omega$	3ω	
χ_{35}		660	84	20	-4	4	0	0	30	30	6	6	2	
χ_{36}		704	64	0	0	0	0	0	$-64-24\omega$	$-40+24\omega$	-8\omega	$8+8\omega$	0	
χ_{37}		704	64	0	0	0	0	0	$-40+24\omega$	$-64-24\omega$	$8+8\omega$	-8\omega	0	
χ_{38}		880	48	16	0	0	0	0	$40+60\omega$	$-20-60\omega$	$-8-4\omega$	$-4+4\omega$	4ω	
χ_{39}		880	48	16	0	0	0	0	$-20-60\omega$	$40+60\omega$	$-4+4\omega$	$-8-4\omega$	$-4-4\omega$	
χ_{40}		891	27	-21	3	3	-1	-1	81	81	9	9	-3	
χ_{41}		891	27	-21	3	3	-1	-1	$-81-81\omega$	81ω	$-9-9\omega$	9ω	$3+3\omega$	
χ_{42}		891	27	-21	3	3	-1	-1	81\omega	$-81-81\omega$	9\omega	$-9-9\omega$	-3ω	
χ_{43}		990	-18	6	-2	-6	-2	0	$-45-45\omega$	45\omega	$3+3\omega$	-3ω	$3+3\omega$	
χ_{44}		990	-18	6	-2	-6	-2	0	45\omega	$-45-45\omega$	-3\omega	$3+3\omega$	-3ω	
χ_{45}		1024	0	0	0	0	0	0	64	64	0	0	0	
χ_{46}		1215	-81	-9	-9	3	3	1	0	0	0	0	0	
χ_{47}		1215	-81	-9	-9	3	3	1	0	0	0	0	0	

Table 1, Part 2: Characters of $PSU(5, 2)$

Order of centralizer	$2^5 \cdot 3^2$	$2^4 \cdot 3^2$	$2^4 \cdot 3^2$	$2^3 \cdot 3$	$2^3 \cdot 3$	$2^4 \cdot 3^5$	$2^4 \cdot 3^5$	$2^4 \cdot 3^4$	$2^4 \cdot 3^4$	$2^4 \cdot 3^3$	$2^4 \cdot 3^3$	$2^4 \cdot 3^3$
	el.	6	12	12	12	12	3	3	6	6	6	6
$\chi_i^{(5)}$	c_{13}	c_{14}	c_{15}	c_{16}	c_{17}	c_{18}	c_{19}	c_{20}	c_{21}	c_{22}	c_{23}	
χ_1	1	1	1	1	1	1	1	1	1	1	1	1
χ_2	-1	-1	-1	1	1	1	1	3	3	-3	-3	
χ_3	$1+2\omega$	$-1-2\omega$	$1+2\omega$	-1	-1	$-1+3\omega$	$-4-3\omega$	$1+3\omega$	$-2-3\omega$	$-1-\omega$	ω	
χ_4	$-1-2\omega$	$1+2\omega$	$-1-2\omega$	-1	-1	$-4-3\omega$	$-1+3\omega$	$-2-3\omega$	$1+3\omega$	ω	$-1-\omega$	
χ_5	2	-2	-2	0	0	-1	-1	3	3	3	3	
χ_6	-2	2	2	0	0	1	1	5	5	5	5	
χ_7	$-1+3\omega$	ω	$-1-\omega$	$-\omega$	$1+\omega$	$-2-6\omega$	$4+6\omega$	-2	-2	$2+2\omega$	-2ω	
χ_8	$-4-3\omega$	$-1-\omega$	ω	$1+\omega$	$-\omega$	$4+6\omega$	$-2-6\omega$	-2	-2	-2ω	$2+2\omega$	
χ_9	$-2-3\omega$	$-3-\omega$	$-2+\omega$	$1+\omega$	$-\omega$	$-6-9\omega$	$3+9\omega$	$-6-3\omega$	$-3+3\omega$	$-2-\omega$	$-1+\omega$	
χ_{10}	$1+3\omega$	$-2+\omega$	$-3-\omega$	$-\omega$	$1+\omega$	$3+9\omega$	$-6-9\omega$	$-3+3\omega$	$-6-3\omega$	$-1+\omega$	$-2-\omega$	
χ_{11}	-1	3	3	-1	-1	2	2	-2	-2	-2	-2	
χ_{12}	$1+2\omega$	$-1-2\omega$	$1+2\omega$	-1	-1	$-4-3\omega$	$-1+3\omega$	$-6-9\omega$	$3+9\omega$	-3ω	$3+3\omega$	
χ_{13}	$-1-2\omega$	$1+2\omega$	$-1-2\omega$	-1	-1	$-1+3\omega$	$-4-3\omega$	$3+9\omega$	$-6-9\omega$	$3+3\omega$	-3ω	
χ_{14}	$1-\omega$	$-2-3\omega$	$1+3\omega$	ω	$-1-\omega$	$-1-6\omega$	$5+6\omega$	$5+6\omega$	$-1-6\omega$	$-5-2\omega$	$-3+2\omega$	
χ_{15}	$2+\omega$	$1+3\omega$	$-2-3\omega$	$-1-\omega$	ω	$5+6\omega$	$-1-6\omega$	$-1-6\omega$	$5+6\omega$	$-3+2\omega$	$-5-2\omega$	
χ_{16}	2	2	2	0	0	12	12	6	6	0	0	
χ_{17}	2	2	2	0	0	3	3	-9	-9	3	3	
χ_{18}	4	0	0	0	0	14	14	2	2	2	2	
χ_{19}	$-2-2\omega$	-2ω	$2+2\omega$	0	0	$10+3\omega$	$7-3\omega$	$-6-3\omega$	$-3+3\omega$	$-2-\omega$	$-1+\omega$	
χ_{20}	2ω	$2+2\omega$	-2ω	0	0	$7-3\omega$	$10+3\omega$	$-3+3\omega$	$-6-3\omega$	$-1+\omega$	$-2-\omega$	
χ_{21}	$-4-2\omega$	$2+2\omega$	-2ω	0	0	$-17-15\omega$	$-2+15\omega$	$-1-3\omega$	$2+3\omega$	$-1-3\omega$	$2+3\omega$	
χ_{22}	$-2+2\omega$	-2ω	$2+2\omega$	0	0	$-2+15\omega$	$-17-15\omega$	$2+3\omega$	$-1-3\omega$	$2+3\omega$	$-1-3\omega$	
χ_{23}	$2+2\omega$	2ω	$-2-2\omega$	0	0	-6	-6	$6+6\omega$	-6ω	$-2-4\omega$	$2+4\omega$	
χ_{24}	-2ω	$-2-2\omega$	2ω	0	0	-6	-6	-6ω	$6+6\omega$	$2+4\omega$	$-2-4\omega$	

Table 1, Part 3: Characters of $PSU(5, 2)$

Order of centralizer	$2^5 \cdot 3^2$	$2^4 \cdot 3^2$	$2^4 \cdot 3^2$	$2^3 \cdot 3$	$2^3 \cdot 3$	$2^4 \cdot 3^5$	$2^4 \cdot 3^5$	$2^4 \cdot 3^4$	$2^4 \cdot 3^4$	$2^4 \cdot 3^3$	$2^4 \cdot 3^3$
e1.	6	12	12	12	12	3	3	6	6	6	6
$\chi_i^{(5)}$	c_{13}	c_{14}	c_{15}	c_{16}	c_{17}	c_{18}	c_{19}	c_{20}	c_{21}	c_{22}	c_{23}
X25	0	0	0	0	0	-4	-4	8	8	-4	-4
X26	$3-\omega$	ω	$-1-\omega$	$-\omega$	$1+\omega$	$-12-9\omega$	$-3+9\omega$	3ω	$-3-3\omega$	$-4-5\omega$	$1+5\omega$
X27	$4+\omega$	$-1-\omega$	ω	$1+\omega$	$-\omega$	$-3+9\omega$	$-12-9\omega$	$-3-3\omega$	3ω	$1+5\omega$	$-4-5\omega$
X28	2	-2	-2	0	0	8	8	-2	-2	4	4
X29	$-2-2\omega$	2ω	$-2-2\omega$	0	0	$14+12\omega$	$2-12\omega$	$2-6\omega$	$8+6\omega$	2	2
X30	2ω	$-2-2\omega$	2ω	0	0	$2-12\omega$	$4+12\omega$	$8+6\omega$	$2-6\omega$	2	2
X31	$-3-3\omega$	$-\omega$	$1+\omega$	$-\omega$	$1+\omega$	9 ω	$-9-9\omega$	9 ω	$-9-9\omega$	-3ω	$3+3\omega$
X32	3ω	$1+\omega$	$-\omega$	$1+\omega$	$-\omega$	$-9-9\omega$	9 ω	$-9-9\omega$	9 ω	$3+3\omega$	-3ω
X33	3ω	$1+\omega$	$-\omega$	$1+\omega$	$-\omega$	$-9-9\omega$	9 ω	$9+9\omega$	-9ω	$3+3\omega$	-3ω
X34	$-3-3\omega$	$-\omega$	$1+\omega$	$-\omega$	$1+\omega$	9 ω	$-9-9\omega$	-9ω	$9+9\omega$	-3ω	$3+3\omega$
X35	2	2	2	0	0	-15	-15	3	3	-3	-3
X36	0	0	0	0	0	$8+12\omega$	$-4-12\omega$	-8	-8	4ω	$-4-4\omega$
X37	0	0	0	0	0	$-4-12\omega$	$8+12\omega$	-8	-8	$-4-4\omega$	4ω
X38	$-4-4\omega$	0	0	0	0	$10+6\omega$	$4-6\omega$	$6+6\omega$	-6ω	$-2+2\omega$	$-4-2\omega$
X39	4ω	0	0	0	0	$4-6\omega$	$10+6\omega$	-6 ω	$6+6\omega$	$-4-2\omega$	$-2+2\omega$
X40	-3	-3	-3	-1	-1	0	0	0	0	0	0
X41	-3ω	$3+3\omega$	-3ω	$1+\omega$	$-\omega$	0	0	0	0	0	0
X42	$3+3\omega$	-3ω	$3+3\omega$	$-\omega$	$1+\omega$	0	0	0	0	0	0
X43	-3ω	$-1-\omega$	ω	$-1-\omega$	ω	$-18-18\omega$	18ω	0	0	$6+6\omega$	-6ω
X44	$3+3\omega$	ω	$-1-\omega$	ω	$-1-\omega$	18ω	$-18-18\omega$	0	0	-6ω	$6+6\omega$
X45	0	0	0	0	0	16	16	0	0	0	0
X46	0	0	0	0	0	0	0	0	0	0	0
X47	0	0	0	0	0	0	0	0	0	0	0

Table 1, Part 4: Characters of $PSU(5, 2)$

Order of centralizer e1.	$2^4 \cdot 3^2$	$2^4 \cdot 3^2$	$2^3 \cdot 3^2$	$2^3 \cdot 3^2$	$2^3 \cdot 3$	$2^3 \cdot 3$	$2^3 \cdot 3^5$	$2^3 \cdot 3^3$	$2^2 \cdot 3^2$	$2^2 \cdot 3^2$	$2^2 \cdot 3^3$	$2^2 \cdot 3^3$	$2^2 \cdot 3^4$
	6	6	12	12	12	12	3	6	12	6	6	6	3
$\chi_i^{(5)}$	C_{24}	C_{25}	C_{26}	C_{27}	C_{28}	C_{29}	C_{30}	C_{31}	C_{32}	C_{33}	C_{34}	C_{35}	C_{36}
χ_1	1	1	1	1	1	1	1	1	1	1	1	1	1
χ_2	-1	-1	-1	-1	1	1	4	0	2	2	0	0	-2
χ_3	$1-\omega$	$2+\omega$	$-1+\omega$	$-2-\omega$	$1+\omega$	$-\omega$	2	-2	0	0	$2+2\omega$	-2ω	2
χ_4	$2+\omega$	$1-\omega$	$-2-\omega$	$-1+\omega$	$-\omega$	$1+\omega$	2	-2	0	0	-2ω	$2+2\omega$	2
χ_5	-1	-1	1	1	1	1	5	-3	1	2	0	0	2
χ_6	1	1	-1	-1	-1	-1	10	2	2	1	-1	-1	1
χ_7	2	2	-2ω	$2+2\omega$	0	0	1	1	1	-1	$-1+2\omega$	$-3-2\omega$	1
χ_8	2	2	$2+2\omega$	-2ω	0	0	1	1	1	-1	$-3-2\omega$	$-1+2\omega$	1
χ_9	$-2-3\omega$	$1+3\omega$	$-\omega$	$1+\omega$	ω	$-1-\omega$	3	3	-1	1	$1+2\omega$	$-1-2\omega$	3
χ_{10}	$1+3\omega$	$-2-3\omega$	$1+\omega$	$-\omega$	$-1-\omega$	ω	3	3	-1	1	$-1-2\omega$	$1+2\omega$	3
χ_{11}	2	2	0	0	0	0	2	-2	0	2	-2	-2	2
χ_{12}	$-2-\omega$	$-1+\omega$	$2+\omega$	$1-\omega$	$-\omega$	$1+\omega$	8	0	0	0	0	0	-4
χ_{13}	$-1+\omega$	$-2-\omega$	$1-\omega$	$2+\omega$	$1+\omega$	$-\omega$	8	0	0	0	0	0	-4
χ_{14}	$1+2\omega$	$-1-2\omega$	1	1	-1	-1	11	-1	1	0	$-2-2\omega$	2ω	2
χ_{15}	$-1-2\omega$	$1+2\omega$	1	1	-1	-1	11	-1	1	0	2ω	$-2-2\omega$	2
χ_{16}	2	2	2	2	0	0	3	3	-1	-1	3	3	3
χ_{17}	-1	-1	-1	-1	-1	-1	3	3	-1	2	0	0	-6
χ_{18}	-2	-2	0	0	0	0	-4	-4	0	1	-1	-1	5
χ_{19}	$-2+\omega$	$-3-\omega$	ω	$-1-\omega$	$-\omega$	$1+\omega$	7	3	1	-1	$1+2\omega$	$-1-2\omega$	1
χ_{20}	$-3-\omega$	$-2+\omega$	$-1-\omega$	ω	$1+\omega$	$-\omega$	7	3	1	-1	$-1-2\omega$	$1+2\omega$	1
χ_{21}	$-1+\omega$	$-2-\omega$	$-1-\omega$	ω	$-1-\omega$	ω	-5	-1	1	0	2	2	4
χ_{22}	$-2-\omega$	$-1+\omega$	ω	$-1-\omega$	ω	$-1-\omega$	-5	-1	1	0	2	2	4
χ_{23}	$2+2\omega$	-2ω	2ω	$-2-2\omega$	0	0	3	3	-1	1	$1+2\omega$	$-1-2\omega$	3
χ_{24}	-2ω	$2+2\omega$	$-2-2\omega$	2ω	0	0	3	3	-1	1	$-1-2\omega$	$1+2\omega$	3

Table 1, Part 5: Characters of $PSU(5, 2)$

Order of centralizer	$2^4 \cdot 3^2$	$2^4 \cdot 3^2$	$2^3 \cdot 3^2$	$2^3 \cdot 3^2$	$2^3 \cdot 3$	$2^3 \cdot 3$	$2^3 \cdot 3^5$	$2^3 \cdot 3^3$	$2^2 \cdot 3^2$	$2^2 \cdot 3^3$	$2^2 \cdot 3^3$	$2^2 \cdot 3^4$	
el.	6	6	12	12	12	12	3	6	12	6	6	3	
$\chi_i^{(5)}$	c_{24}	c_{25}	c_{26}	c_{27}	c_{28}	c_{29}	c_{30}	c_{31}	c_{32}	c_{33}	c_{34}	c_{35}	c_{36}
χ_{25}	0	0	0	0	0	0	14	2	0	0	2	2	-4
χ_{26}	$-\omega$	$1+\omega$	ω	$-1-\omega$	$\omega -1-\omega$	-3	-3	1	-1	$-1-2\omega$	$1+2\omega$	-3	
χ_{27}	$1+\omega$	$-\omega$	$-1-\omega$	$\omega -1-\omega$	$\omega -3$	-3	1	-1	$1+2\omega$	$-1-2\omega$	-3		
χ_{28}	2	2	-2	-2	0	0	17	1	1	-1	1	1	-1
χ_{29}	$-2-2\omega$	2ω	2ω	$-2-2\omega$	0	0	-1	-1	-1	-1	-1	-1	-1
χ_{30}	2ω	$-2-2\omega$	$-2-2\omega$	2ω	0	0	-1	-1	-1	-1	-1	-1	-1
χ_{31}	-3ω	$3+3\omega$	$-\omega$	$1+\omega$	$-\omega$	$1+\omega$	9	-3	-1	0	0	0	0
χ_{32}	$3+3\omega$	-3ω	$1+\omega$	$-\omega$	$1+\omega$	$-\omega$	9	-3	-1	0	0	0	0
χ_{33}	$-3-3\omega$	3ω	$1+\omega$	$-\omega$	$-1-\omega$	ω	9	-3	-1	0	0	0	0
χ_{34}	3ω	$-3-3\omega$	$-\omega$	$1+\omega$	$\omega -1-\omega$	9	-3	-1	0	0	0	0	0
χ_{35}	-1	-1	-1	-1	1	1	3	3	-1	-1	-3	-3	3
χ_{36}	0	0	0	0	0	0	2	-2	0	0	-2ω	$2+2\omega$	2
χ_{37}	0	0	0	0	0	0	2	-2	0	0	$2+2\omega$	-2ω	2
χ_{38}	$2+2\omega$	-2ω	0	0	0	0	-8	0	0	1	$1+2\omega$	$-1-2\omega$	-5
χ_{39}	-2ω	$2+2\omega$	0	0	0	0	-8	0	0	1	$-1-2\omega$	$1+2\omega$	-5
χ_{40}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{41}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{42}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{43}	0	0	$2+2\omega$	-2ω	0	0	-9	3	1	0	0	0	0
χ_{44}	0	0	-2ω	$2+2\omega$	0	0	-9	3	1	0	0	0	0
χ_{45}	0	0	0	0	0	0	-8	0	0	0	0	0	4
χ_{46}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{47}	0	0	0	0	0	0	0	0	0	0	0	0	0

Table 1, Part 6: Characters of $PSU(5, 2)$

$\chi_i^{(5)}$	el.	Order of centralizer											
		2.3 ³	2.3 ³	2.3 ²	2.3 ²	3 ³	3 ³	3.5	3.5	3.5	11	11	11
χ_1		1	1	1	1	1	1	1	1	1	1	1	1
χ_2		-2	-2	0	0	1	1	0	0	0	-1	-1	-1
χ_3		$-\omega$	$1+\omega$	ω	$-1-\omega$	$-\omega$	$1+\omega$	1	ω	$-1-\omega$	0	0	0
χ_4		$1+\omega$	$-\omega$	$-1-\omega$	ω	$1+\omega$	$-\omega$	1	$-1-\omega$	ω	0	0	0
χ_5		2	2	0	0	-1	-1	-1	-1	-1	0	0	0
χ_6		1	1	-1	-1	1	1	0	0	0	0	0	0
χ_7		$-1-\omega$	ω	$-1-\omega$	ω	$-1-\omega$	ω	0	0	0	0	0	0
χ_8		ω	$-1-\omega$	ω	$-1-\omega$	ω	$-1-\omega$	0	0	0	0	0	0
χ_9		0	0	0	0	0	0	1	$-1-\omega$	ω	0	0	0
χ_{10}		0	0	0	0	0	0	1	ω	$-1-\omega$	0	0	0
χ_{11}		-1	-1	1	1	-1	-1	0	0	0	0	0	0
χ_{12}		$-2-2\omega$	2ω	0	0	$1+\omega$	$-\omega$	0	0	0	0	0	0
χ_{13}		2ω	$-2-2\omega$	0	0	$-\omega$	$1+\omega$	0	0	0	0	0	0
χ_{14}		$-\omega$	$1+\omega$	$-\omega$	$1+\omega$	$-\omega$	$1+\omega$	0	0	0	0	0	0
χ_{15}		$1+\omega$	$-\omega$	$1+\omega$	$-\omega$	$1+\omega$	$-\omega$	0	0	0	0	0	0
χ_{16}		0	0	0	0	0	0	0	0	0	-1	-1	-1
χ_{17}		0	0	0	0	0	0	0	0	0	0	0	0
χ_{18}		-1	-1	-1	-1	-1	-1	1	1	1	0	0	0
χ_{19}		$2+2\omega$	-2ω	0	0	$-1-\omega$	ω	0	0	0	0	0	0
χ_{20}		-2ω	$2+2\omega$	0	0	ω	$-1-\omega$	0	0	0	0	0	0
χ_{21}		$-1-\omega$	ω	$1+\omega$	$-\omega$	$-1-\omega$	ω	0	0	0	0	0	0
χ_{22}		ω	$-1-\omega$	$-\omega$	$1+\omega$	ω	$-1-\omega$	0	0	0	0	0	0
χ_{23}		0	0	0	0	0	0	-1	$-\omega$	$1+\omega$	0	0	0
χ_{24}		0	0	0	0	0	-1	$1+\omega$	$-\omega$	0	0	0	0

Table 1, Part 7: Characters of $PSU(5, 2)$

Order of centralizer												
	2.3 ³	2.3 ³	2.3 ²	2.3 ²	3 ³	3 ³	3.5	3.5	3.5	11	11	11
el.	9	9	18	18	9	9	5	15	15	11	11	11
$\chi_i^{(5)}$	c_{37}	c_{38}	c_{39}	c_{40}	c_{41}	c_{42}	c_{43}	c_{44}	c_{45}	c_{46}	c_{47}	
X_{25}	-1	-1	-1	-1	-1	-1	0	0	0	1	1	
X_{26}	0	0	0	0	0	0	0	0	0	0	0	
X_{27}	0	0	0	0	0	0	0	0	0	0	0	
X_{28}	-1	-1	1	1	-1	-1	0	0	0	0	0	
X_{29}	$-\omega$	$1+\omega$	$-\omega$	$1+\omega$	$-\omega$	$1+\omega$	0	0	0	0	0	
X_{30}	$1+\omega$	$-\omega$	$1+\omega$	$-\omega$	$1+\omega$	$-\omega$	0	0	0	0	0	
X_{31}	0	0	0	0	0	0	0	0	0	0	0	
X_{32}	0	0	0	0	0	0	0	0	0	0	0	
X_{33}	0	0	0	0	0	0	0	0	0	0	0	
X_{34}	0	0	0	0	0	0	0	0	0	0	0	
X_{35}	0	0	0	0	0	0	0	0	0	0	0	
X_{36}	$-\omega$	$1+\omega$	ω	$-1-\omega$	$-\omega$	$1+\omega$	-1	$-\omega$	$1+\omega$	0	0	
X_{37}	$1+\omega$	$-\omega$	$-1-\omega$	ω	$1+\omega$	$-\omega$	-1	$1+\omega$	$-\omega$	0	0	
X_{38}	-2ω	$2+2\omega$	0	0	ω	$-1-\omega$	0	0	0	0	0	
X_{39}	$2+2\omega$	-2ω	0	0	$-1-\omega$	ω	0	0	0	0	0	
X_{40}	0	0	0	0	0	0	1	1	1	0	0	
X_{41}	0	0	0	0	0	0	1	ω	$-1-\omega$	0	0	
X_{42}	0	0	0	0	0	0	1	$-1-\omega$	ω	0	0	
X_{43}	0	0	0	0	0	0	0	0	0	0	0	
X_{44}	0	0	0	0	0	0	0	0	0	0	0	
X_{45}	-2	-2	0	0	1	1	-1	-1	-1	1	1	
X_{46}	0	0	0	0	0	0	0	0	0	β	$\bar{\beta}$	
X_{47}	0	0	0	0	0	0	0	0	0	$\bar{\beta}$	β	

Table 1, Part 8: Characters of $PSU(5, 2)$

el.	Order of centralizer	2 ¹⁵ .3 ⁶ .5.7.11	2 ¹⁵ .3 ⁴ .5	2 ¹⁴ .3 ²	2 ¹² .3 ²	2 ¹¹ .3 ³	2 ¹¹ .3	2 ⁹ .3	2 ⁹ .3	2 ⁹ .3	2 ⁸ .3	2 ⁸	2 ⁶
		1	2	2	2	4	4	4	4	4	4	4	4
$\chi_i^{(6)}$		c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}	c_{11}	c_{12}
χ_1		1	1	1	1	1	1	1	1	1	1	1	1
χ_2		22	-10	6	-2	6	-2	2	2	2	-2	2	2
χ_3		231	39	7	-9	23	7	-1	-1	-1	-1	-1	3
χ_4		252	60	28	12	12	-4	4	4	4	4	4	0
χ_5		385	-95	17	-7	1	9	5	5	5	-7	-3	1
χ_6		440	120	24	8	24	8	0	0	0	8	0	0
χ_7		560	-80	-16	16	16	-16	0	0	0	0	0	0
χ_8		616	-24	40	8	8	8	8	8	8	0	0	0
χ_9		770	-30	-14	10	34	-6	-2	-2	-2	2	-2	2
χ_{10}		770	-30	-14	10	34	-6	-2	-2	-2	2	-2	2
χ_{11}		1155	195	35	19	-13	3	11	-5	-5	3	3	-1
χ_{12}		1155	195	35	19	-13	3	-5	11	-5	3	3	-1
χ_{13}		1155	195	35	19	-13	3	-5	-5	11	3	3	-1
χ_{14}		1386	-246	58	-30	-6	2	-2	-2	-2	-6	6	-2
χ_{15}		1540	260	4	-28	-12	-12	4	4	4	4	-4	0
χ_{16}		3080	-440	40	-8	40	-8	0	0	0	-8	0	0
χ_{17}		3080	-440	40	-8	40	-8	0	0	0	-8	0	0
χ_{18}		3520	-320	64	0	64	0	0	0	0	0	0	0
χ_{19}		4620	-180	44	-36	28	-20	4	4	4	-4	-4	0
χ_{20}		4928	320	64	64	0	0	0	0	0	0	0	0
χ_{21}		5544	-24	-56	24	72	24	0	0	0	-8	0	0
χ_{22}		6160	400	-48	-16	48	16	0	0	0	0	0	0
χ_{23}		6160	400	-48	-16	48	16	0	0	0	0	0	0

Table 2, Part 1: Characters of $PSU(6, 2)$

el.	Order of centralizer	2 ¹⁵ .3 ⁶ .5.7.11	2 ¹⁵ .3 ⁴ .5	2 ¹⁴ .3 ²	2 ¹² .3 ²	2 ¹¹ .3 ³	2 ¹¹ .3	2 ⁹ .3	2 ⁹ .3	2 ⁹ .3	2 ⁸ .3	2 ⁸	2 ⁶
		1	2	2	2	4	4	4	4	4	4	4	8
$\chi_i^{(6)}$	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}	c_{11}	c_{12}	
X ₂₄	6930	690	98	42	18	-6	6	6	6	10	-2	2	
X ₂₅	8064	384	128	0	0	0	0	0	0	0	0	0	
X ₂₆	9240	-360	88	-8	-8	-8	24	-8	-8	0	0	0	
X ₂₇	9240	-360	88	-8	-8	-8	-8	24	-8	0	0	0	
X ₂₈	9240	-360	88	-8	-8	-8	-8	-8	24	0	0	0	
X ₂₉	10395	315	-21	-45	75	-13	-1	-1	-1	3	-1	-1	
X ₃₀	10395	315	-21	-45	75	-13	-1	-1	-1	3	-1	-1	
X ₃₁	10395	315	-21	-45	-21	19	15	-1	-1	3	-1	-1	
X ₃₂	10395	315	-21	-45	-21	19	-1	15	-1	3	-1	-1	
X ₃₃	10395	315	-21	-45	-21	19	-1	-1	15	3	-1	-1	
X ₃₄	11264	1024	0	0	0	0	0	0	0	0	0	0	
X ₃₅	13860	420	100	36	84	20	4	4	4	-4	4	0	
X ₃₆	14784	-1344	64	0	-64	0	0	0	0	0	0	0	
X ₃₇	18711	-1161	-57	63	-9	15	3	3	3	-1	-5	-1	
X ₃₈	18711	1431	87	-9	-9	-9	-9	-9	-9	-1	-1	-1	
X ₃₉	20790	-810	6	-18	6	14	-6	-6	-6	6	2	2	
X ₄₀	20790	-810	6	-18	6	14	-6	-6	-6	6	2	2	
X ₄₁	24640	-960	64	-64	0	0	0	0	0	0	0	0	
X ₄₂	25515	-405	-117	27	27	-21	3	3	3	3	3	-1	
X ₄₃	25515	-405	-117	27	27	-21	3	3	3	3	3	-1	
X ₄₄	32768	0	0	0	0	0	0	0	0	0	0	0	
X ₄₅	37422	270	30	54	-18	6	-6	-6	-6	-2	-6	-2	
X ₄₆	40095	1215	-81	-9	-81	-9	3	3	3	-9	3	3	

Table 2, Part 2: Characters of $PSU(6, 2)$

Order of centralizer												
	2^5	2^5	2^5	$2^6 \cdot 3^5 \cdot 5$	$2^6 \cdot 3^3$	$2^5 \cdot 3^2$	$2^4 \cdot 3^2$	$2^3 \cdot 3$	$2^6 \cdot 3^6$	$2^6 \cdot 3^4$	$2^6 \cdot 3^4$	$2^6 \cdot 3^2$
el.	8	8	8	3	6	6	12	12	3	6	6	6
$\chi_i^{(6)}$	C_{13}	C_{14}	C_{15}	C_{16}	C_{17}	C_{18}	C_{19}	C_{20}	C_{21}	C_{22}	C_{23}	C_{24}
χ_1	1	1	1	1	1	1	1	1	1	1	1	1
χ_2	0	0	0	4	-4	0	0	-2	-5	-1	-1	3
χ_3	-1	-1	-1	6	6	-2	2	2	15	3	3	7
χ_4	0	0	0	9	9	1	-3	1	9	-3	-3	1
χ_5	-1	-1	-1	25	1	5	1	-1	7	-5	-5	-1
χ_6	0	0	0	35	3	3	3	-1	8	12	12	0
χ_7	0	0	0	20	4	-4	4	0	20	-8	-8	-4
χ_8	0	0	0	-14	-6	-2	2	0	-5	3	3	-5
χ_9	0	0	0	5	-3	1	1	-1	-13	$3+12\omega$	$-9-12\omega$	7
χ_{10}	0	0	0	5	-3	1	1	-1	-13	$-9-12\omega$	$3+12\omega$	7
χ_{11}	3	-1	-1	30	6	2	2	0	-6	6	6	2
χ_{12}	-1	3	-1	30	6	2	2	0	-6	6	6	2
χ_{13}	-1	-1	3	30	6	2	2	0	-6	6	6	2
χ_{14}	0	0	0	36	-12	4	0	0	9	-3	-3	1
χ_{15}	0	0	0	55	-1	-5	3	1	1	17	17	1
χ_{16}	0	0	0	65	1	1	1	1	2	$-2+12\omega$	$-14-12\omega$	-2
χ_{17}	0	0	0	65	1	1	1	1	2	$-14-12\omega$	$-2+12\omega$	-2
χ_{18}	0	0	0	10	-14	-2	-2	0	-44	4	4	4
χ_{19}	0	0	0	-15	9	5	1	-1	57	9	9	-7
χ_{20}	0	0	0	-4	-4	4	0	0	68	-4	-4	4
χ_{21}	0	0	0	9	9	1	-3	1	36	12	12	4
χ_{22}	0	0	0	40	-8	0	0	0	-50	$-2-12\omega$	$10+12\omega$	-6
χ_{23}	0	0	0	40	-8	0	0	0	-50	$10+12\omega$	$-2-12\omega$	-6

Table 2, Part 3: Characters of $PSU(6, 2)$

Order of centralizer												
	2^5	2^5	2^5	2^5	$2^6 \cdot 3 \cdot 5$	$2^6 \cdot 3^3$	$2^5 \cdot 3^2$	$2^4 \cdot 3^2$	$2^3 \cdot 3$	$2^6 \cdot 3^6$	$2^6 \cdot 3^4$	$2^6 \cdot 3^2$
el.	8	8	8	3	6	6	12	12	3	6	6	6
$\chi_i^{(6)}$	c_{13}	c_{14}	c_{15}	c_{16}	c_{17}	c_{18}	c_{19}	c_{20}	c_{21}	c_{22}	c_{23}	c_{24}
X_{24}	0	0	0	45	-3	5	-3	1	-36	-12	-12	-4
X_{25}	0	0	0	-36	12	-4	0	0	-36	-12	-12	-4
X_{26}	0	0	0	-30	-6	-2	-2	0	33	9	9	1
X_{27}	0	0	0	-30	-6	-2	-2	0	33	9	9	1
X_{28}	0	0	0	-30	-6	-2	-2	0	33	9	9	1
X_{29}	1	1	1	0	0	0	0	0	27	-9	-9	3
X_{30}	1	1	1	0	0	0	0	0	27	-9	-9	3
X_{31}	-3	1	1	0	0	0	0	0	27	-9	-9	3
X_{32}	1	-3	1	0	0	0	0	0	27	-9	-9	3
X_{33}	1	1	-3	0	0	0	0	0	27	-9	-9	3
X_{34}	0	0	0	104	-8	0	0	0	32	16	16	0
X_{35}	0	0	0	-45	3	-5	3	-1	9	-3	-3	1
X_{36}	0	0	0	114	-6	-2	2	0	-12	-12	-12	4
X_{37}	1	1	1	81	9	-3	-3	-1	0	0	0	0
X_{38}	-1	-1	-1	81	9	-3	-3	-1	0	0	0	0
X_{39}	0	0	0	0	0	0	0	0	54	$18+36\omega$	$-18-36\omega$	-6
X_{40}	0	0	0	0	0	0	0	0	54	$-18-36\omega$	$18+36\omega$	-6
X_{41}	0	0	0	-20	12	4	0	0	-92	12	12	4
X_{42}	-1	-1	-1	0	0	0	0	0	0	0	0	0
X_{43}	-1	-1	-1	0	0	0	0	0	0	0	0	0
X_{44}	0	0	0	-64	0	0	0	0	-64	0	0	0
X_{45}	0	0	0	-81	-9	3	3	1	0	0	0	0
X_{46}	1	1	1	0	0	0	0	0	0	0	0	0

Table 2, Part 4: Characters of $PSU(6, 2)$

Order of centralizer	C_{25}	C_{26}	C_{27}	C_{28}	C_{29}	C_{30}	C_{31}	C_{32}	C_{33}	C_{34}	C_{35}	C_{36}
e.l.	12	12	12	12	12	12	12	12	6	6	6	3
$\chi_i^{(6)}$	1	1	1	1	1	1	1	1	1	1	1	1
χ_1	1	1	1	1	1	1	1	1	1	1	1	1
χ_2	-3	-3	1	1	-1	-1	-1	-2	0	2	4	1
χ_3	5	5	1	1	-1	-1	-1	0	-2	0	6	0
χ_4	3	3	-1	-1	1	1	1	3	1	3	9	0
χ_5	1	1	-3	-3	-1	-1	-1	2	2	-2	-2	1
χ_6	6	6	2	2	0	0	0	-1	3	3	-1	-1
χ_7	-2	-2	2	2	0	0	0	-2	2	-2	2	2
χ_8	-1	-1	-1	-1	-1	-1	-1	-1	1	3	13	-2
χ_9	$-5-6\omega$	$1+6\omega$	$-1-2\omega$	$1+2\omega$	1	1	1	1	1	-3	5	-1
χ_{10}	$1+6\omega$	$-5-6\omega$	$1+2\omega$	$-1-2\omega$	1	1	1	1	1	-3	5	-1
χ_{11}	-4	-4	0	0	2	-2	-2	1	-1	-3	3	0
χ_{12}	-4	-4	0	0	-2	2	-2	1	-1	-3	3	0
χ_{13}	-4	-4	0	0	-2	-2	2	1	-1	-3	3	0
χ_{14}	3	3	-1	-1	1	1	1	-3	1	-3	9	0
χ_{15}	-3	-3	-3	-3	1	1	1	-1	1	-1	1	1
χ_{16}	$-8-6\omega$	$-2+6\omega$	-2ω	$2+2\omega$	0	0	0	1	1	1	-7	-1
χ_{17}	$-2+6\omega$	$-8-6\omega$	$2+2\omega$	-2ω	0	0	0	1	1	1	-7	-1
χ_{18}	-8	-8	0	0	0	0	0	0	-2	4	10	1
χ_{19}	1	1	1	1	1	1	1	0	-4	0	12	0
χ_{20}	0	0	0	0	0	0	0	1	1	5	5	2
χ_{21}	0	0	0	0	0	0	0	-3	1	-3	9	0
χ_{22}	$6+6\omega$	-6ω	$2+2\omega$	-2ω	0	0	0	2	0	-2	4	1
χ_{23}	-6ω	$6+6\omega$	-2ω	$2+2\omega$	0	0	0	2	0	-2	4	1

Table 2, Part 5: Characters of $PSU(6, 2)$

el.	Order of centralizer											
	$2^5 \cdot 3^3$	$2^5 \cdot 3^3$	$2^5 \cdot 3$	$2^5 \cdot 3$	$2^4 \cdot 3$	$2^4 \cdot 3$	$2^3 \cdot 3^2$	$2^3 \cdot 3^2$	$2^3 \cdot 3^3$	$2^3 \cdot 3^5$	3^3	3^3
$\chi_i^{(6)}$	C_{25}	C_{26}	C_{27}	C_{28}	C_{29}	C_{30}	C_{31}	C_{32}	C_{33}	C_{34}	C_{35}	C_{36}
χ_{24}	0	0	0	0	0	0	0	-3	-1	-3	-9	0
χ_{25}	0	0	0	0	0	0	0	0	2	0	18	0
χ_{26}	1	1	1	1	-3	1	1	1	1	-3	-3	0
χ_{27}	1	1	1	1	1	-3	1	1	1	-3	-3	0
χ_{28}	1	1	1	1	1	1	-3	1	1	-3	-3	0
χ_{29}	$-3-12\omega$	$9+12\omega$	$1+4\omega$	$-3-4\omega$	-1	-1	-1	0	0	0	0	0
χ_{30}	$9+12\omega$	$-3-12\omega$	$-3-4\omega$	$1+4\omega$	-1	-1	-1	0	0	0	0	0
χ_{31}	-3	-3	1	1	3	-1	-1	0	0	0	0	0
χ_{32}	-3	-3	1	1	-1	3	-1	0	0	0	0	0
χ_{33}	-3	-3	1	1	-1	-1	3	0	0	0	0	0
χ_{34}	0	0	0	0	0	0	0	0	0	4	-4	-1
χ_{35}	3	3	-1	-1	1	1	1	0	-2	0	-18	0
χ_{36}	8	8	0	0	0	0	0	0	-2	0	6	0
χ_{37}	0	0	0	0	0	0	0	0	0	0	0	0
χ_{38}	0	0	0	0	0	0	0	0	0	0	0	0
χ_{39}	6ω	$-6-6\omega$	2ω	$-2-2\omega$	0	0	0	0	0	0	0	0
χ_{40}	$-6-6\omega$	-6ω	$-2-2\omega$	2ω	0	0	0	0	0	0	0	0
χ_{41}	0	0	0	0	0	0	0	-1	1	3	-11	1
χ_{42}	0	0	0	0	0	0	0	0	0	0	0	0
χ_{43}	0	0	0	0	0	0	0	0	0	0	0	0
χ_{44}	0	0	0	0	0	0	0	0	0	0	8	-1
χ_{45}	0	0	0	0	0	0	0	0	0	0	0	0
χ_{46}	0	0	0	0	0	0	0	0	0	0	0	0

Table 2, Part 6: Characters of $PSU(6, 2)$

$\chi_i^{(6)}$	Order of centralizer																	
	el.	18	$2 \cdot 3^2$	18	$2 \cdot 3^2$	9	$2 \cdot 3^3$	9	10	2.5	$2 \cdot 3 \cdot 5$	15	3.5	11	11	11	7	7
χ_1		1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
χ_2		-1	-1	1	1	0	2	-1	0	0	0	0	0	0	0	0	0	1
χ_3		0	0	0	0	-1	1	1	0	0	0	0	0	0	0	0	0	0
χ_4		0	0	0	0	0	2	-1	0	0	0	-1	-1	-1	-1	0	0	0
χ_5		1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_6		0	0	2	2	0	0	0	0	0	0	0	0	0	0	0	0	-1
χ_7		1	1	-1	-1	0	0	0	0	0	-1	-1	-1	-1	0	0	0	0
χ_8		0	0	-2	-2	1	1	1	1	0	0	0	0	0	0	0	0	0
χ_9		$1+2\omega$	$-1-2\omega$	-1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{10}		$-1-2\omega$	$1+2\omega$	-1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{11}		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{12}		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{13}		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{14}		0	0	0	0	-1	1	1	1	0	0	0	0	0	0	0	0	0
χ_{15}		-1	-1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{16}		$-1-\omega$	ω	$-1-3\omega$	$2+3\omega$	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{17}		ω	$-1-\omega$	$2+3\omega$	$-1-3\omega$	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{18}		1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	-1
χ_{19}		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{20}		-1	-1	-1	-1	0	-2	1	0	0	0	0	0	0	0	0	0	0
χ_{21}		0	0	0	0	1	-1	-1	0	0	0	0	0	0	0	0	0	0
χ_{22}		ω	$-1-\omega$	$-2-3\omega$	$1+3\omega$	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{23}		$-1-\omega$	ω	$1+3\omega$	$-2-3\omega$	0	0	0	0	0	0	0	0	0	0	0	0	0

Table 2, Part 7: Characters of $PSU(6, 2)$

Order of centralizer	el.	2.3 ²	2.3 ²	2.3 ³	2.3 ³	2.5	2.3.5	3.5	11	11	7
		C ₃₇	C ₃₈	C ₃₉	C ₄₀	C ₄₁	C ₄₂	C ₄₃	C ₄₄	C ₄₅	C ₄₆
X ₂₄		0	0	0	0	0	0	0	0	0	0
X ₂₅		0	0	0	0	-1	-1	-1	1	1	0
X ₂₆		0	0	0	0	0	0	0	0	0	0
X ₂₇		0	0	0	0	0	0	0	0	0	0
X ₂₈		0	0	0	0	0	0	0	0	0	0
X ₂₉		0	0	0	0	0	0	0	0	0	0
X ₃₀		0	0	0	0	0	0	0	0	0	0
X ₃₁		0	0	0	0	0	0	0	0	0	0
X ₃₂		0	0	0	0	0	0	0	0	0	0
X ₃₃		0	0	0	0	0	0	0	0	0	0
X ₃₄		1	1	-1	-1	-1	-1	-1	0	0	1
X ₃₅		0	0	0	0	0	0	0	0	0	0
X ₃₆		0	0	0	0	1	-1	-1	0	0	0
X ₃₇		0	0	0	0	-1	1	1	0	0	0
X ₃₈		0	0	0	0	1	1	1	0	0	0
X ₃₉		0	0	0	0	0	0	0	0	0	0
X ₄₀		0	0	0	0	0	0	0	0	0	0
X ₄₁		0	0	-2	-2	0	0	0	0	0	0
X ₄₂		0	0	0	0	0	0	0	-β	-β	0
X ₄₃		0	0	0	0	0	0	0	-β	-β	0
X ₄₄		0	0	2	2	0	-2	1	-1	-1	1
X ₄₅		0	0	0	0	0	2	-1	0	0	0
X ₄₆		0	0	0	0	0	0	0	0	0	-1

Table 2, Part 8: Characters of $PSU(6, 2)$

el. β_i	Order of centralizer															
	$2^7 \cdot 3^6 \cdot 5 \cdot 13$	$2^7 \cdot 3^2$	$2^6 \cdot 3^2 \cdot 5$	$2^5 \cdot 3$	$2^5 \cdot 3^2 \cdot 5$	2^5	2^3	$2^3 \cdot 3^6$	$2^3 \cdot 3^5$	$2^3 \cdot 3^5$	3^4	3^3	3^3	$2^3 \cdot 3^2$	$2^2 \cdot 3^2$	$2^2 \cdot 3^2$
el.	1	2	2	4	4	4	8	3	3	3	9	9	9	6	6	6
β_i	C_1	C_2	C_3	C_4	C_5	C_6	C_7	C_8	C_9	C_{10}	C_{11}	C_{12}	C_{13}	C_{14}	C_{15}	C_{16}
β_1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
β_2	26	2	6	2	4	0	0	-1	-1	8	-1	2	-1	-1	-1	2
β_3	26	2	6	2	4	0	0	-1	8	-1	-1	-1	2	-1	2	-1
β_4	39	7	-1	3	-1	-1	1	12	3	3	3	0	0	4	1	1
β_5	52	-4	8	0	-10	2	0	-2	7	7	-2	1	1	2	-1	-1
β_6	65	-7	5	1	-5	-1	-1	11	2	11	2	2	-1	-1	2	-1
β_7	65	-7	5	1	-5	-1	-1	11	11	2	2	-1	2	-1	-1	2
β_8	90	10	10	-2	10	2	0	9	9	9	0	0	0	1	1	1
β_9	234	2	14	2	-4	0	0	-9	18	-9	0	0	0	-1	2	-1
β_{10}	234	2	14	2	-4	0	0	-9	-9	18	0	0	0	-1	-1	2
β_{11}	260	-4	0	0	10	-2	0	-10	17	-1	-1	2	-1	2	-1	-1
β_{12}	260	-4	0	0	10	-2	0	-10	-1	17	-1	-1	2	2	-1	-1
β_{13}	260	4	20	4	0	0	0	17	-10	-10	-1	-1	-1	1	-2	-2
β_{14}	351	15	-9	-1	-9	-1	-1	27	0	0	0	0	0	3	0	0
β_{15}	390	-10	-10	2	10	2	0	39	3	3	3	0	0	-1	-1	-1
β_{16}	416	0	16	0	16	0	0	-16	2	2	2	-1	-1	0	0	0
β_{17}	416	0	16	0	-16	0	0	-16	2	2	2	-1	-1	0	0	0
β_{18}	416	0	-16	0	0	0	0	-16	2	2	2	-1	-1	0	0	0
β_{19}	416	0	-16	0	0	0	0	-16	2	2	2	-1	-1	0	0	0
β_{20}	468	-4	-8	0	-10	2	0	-18	9	9	0	0	0	2	-1	-1
β_{21}	585	1	5	-3	-5	-1	1	18	-9	18	0	0	0	-2	1	-2
β_{22}	585	1	5	-3	-5	-1	1	18	18	-9	0	0	0	-2	-2	1
β_{23}	640	0	0	0	0	0	0	-8	-8	-8	1	1	1	0	0	0
β_{24}	640	0	0	0	0	0	0	-8	-8	-8	1	1	1	0	0	0
β_{25}	640	0	0	0	0	0	0	-8	-8	-8	1	1	1	0	0	0
β_{26}	640	0	0	0	0	0	0	-8	-8	-8	1	1	1	0	0	0
β_{27}	729	9	9	-3	9	1	-1	0	0	0	0	0	0	0	0	0
β_{28}	780	12	-20	4	0	0	0	-3	6	6	-3	0	0	-3	0	0
β_{29}	1040	-16	0	0	0	0	0	14	-4	-4	-4	-1	-1	2	2	2

Table 3, Part 1: Characters of $PS\Omega^+(6, 3)$

β_i	Order of el. centralizer	$2^3 \cdot 3^2$												
		C_{17}	C_{18}	C_{19}	C_{20}	C_{21}	C_{22}	C_{23}	C_{24}	C_{25}	C_{26}	C_{27}	C_{28}	C_{29}
β_1	6	1	1	1	1	1	1	1	1	1	1	1	1	1
β_2	$2^3 \cdot 3^2$	3	0	-1	-2	1	1	1	-1	-1	0	0	0	0
β_3	$2^2 \cdot 3$	0	3	-1	1	-2	1	1	-1	-1	0	0	0	0
β_4	$2^2 \cdot 3^2$	-1	-1	0	-1	-1	-1	-1	-1	-1	0	0	0	0
β_5	5	-1	-1	0	-1	-1	2	-2	0	0	0	0	0	0
β_6	$2^2 \cdot 5$	2	-1	1	1	-2	0	0	0	0	0	0	0	0
β_7	10	-1	2	1	-2	1	0	0	0	0	0	0	0	0
β_8	$2^2 \cdot 5$	1	1	1	1	1	0	0	0	-1	-1	-1	-1	-1
β_9	13	2	-1	-1	-1	2	-1	-1	1	1	0	0	0	0
β_{10}	13	-1	2	-1	2	-1	-1	-1	1	1	0	0	0	0
β_{11}	13	-3	3	0	1	1	0	0	0	0	0	0	0	0
β_{12}	13	3	-3	0	1	1	0	0	0	0	0	0	0	0
β_{13}	13	2	2	1	0	0	0	0	0	0	0	0	0	0
β_{14}	13	0	0	-1	0	0	1	1	1	1	0	0	0	0
β_{15}	13	-1	-1	-1	1	1	0	0	0	0	0	0	0	0
β_{16}	13	-2	-2	0	-2	-2	1	1	1	1	0	0	0	0
β_{17}	13	-2	-2	0	2	2	1	1	-1	-1	0	0	0	0
β_{18}	13	2	2	0	0	0	1	-1	γ	$-\gamma$	0	0	0	0
β_{19}	13	2	2	0	0	0	1	-1	$-\gamma$	γ	0	0	0	0
β_{20}	13	1	1	0	-1	-1	-2	2	0	0	0	0	0	0
β_{21}	13	-1	2	0	-2	1	0	0	0	0	0	0	0	0
β_{22}	13	2	-1	0	1	-2	0	0	0	0	0	0	0	0
β_{23}	13	0	0	0	0	0	0	0	0	0	λ_1	λ_2	λ_3	λ_4
β_{24}	13	0	0	0	0	0	0	0	0	0	λ_2	λ_1	λ_4	λ_3
β_{25}	13	0	0	0	0	0	0	0	0	0	λ_3	λ_4	λ_1	λ_2
β_{26}	13	0	0	0	0	0	0	0	0	0	λ_4	λ_3	λ_2	λ_1
β_{27}	13	0	0	0	0	0	-1	-1	-1	-1	1	1	1	1
β_{28}	13	-2	-2	1	0	0	0	0	0	0	0	0	0	0
β_{29}	13	0	0	0	0	0	0	0	0	0	0	0	0	0

Table 3, Part 2: Characters of $P\Omega^+(6, 3)$

Order of centralizer el.	1	$2^9 \cdot 3^9 \cdot 5 \cdot 7 \cdot 13$	$2^9 \cdot 3^6 \cdot 5 \cdot 7$	$2^9 \cdot 3^4 \cdot 5$	$2^9 \cdot 3^3$	$2^6 \cdot 3^2 \cdot 5$	$2^7 \cdot 3^2$	$2^7 \cdot 3$	$2^6 \cdot 3^3$	2^4	2^4	$2^5 \cdot 3^9$	$2^6 \cdot 3^7$	$2^4 \cdot 3^7 \cdot 5$	$2^3 \cdot 3^7$	$2^3 \cdot 3^7$
	1	2	2	2	4	4	4	4	8	8	3	3	3	3	3	3
$X_i^{(7)}$	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}	c_{11}	c_{12}	c_{13}	c_{14}	c_{15}	
X_1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
X_2	78	-34	14	-2	-6	2	2	2	0	0	-3	6	15	-3	-3	
X_3	91	-21	11	-5	-1	3	3	-1	-1	-1	10	19	1	10	10	
X_4	105	-35	5	1	-5	5	1	-1	1	-1	24	6	15	-3	-3	
X_5	168	56	24	8	4	0	0	4	0	0	6	24	15	6	6	
X_6	182	70	22	6	10	2	2	2	0	0	20	11	29	-7	-7	
X_7	195	55	15	11	5	3	-1	1	1	-1	33	24	15	6	6	
X_8	260	20	20	4	0	4	4	0	0	0	17	-10	-10	-10	17	
X_9	260	20	20	4	0	4	4	0	0	0	17	-10	-10	17	-10	
X_{10}	273	-91	29	-7	-9	1	-3	3	-1	1	30	30	30	3	3	
X_{11}	546	154	26	2	14	6	-2	-2	0	0	-21	-12	51	6	6	
X_{12}	819	-21	-21	19	-1	7	-1	-1	1	1	90	9	9	9	9	
X_{13}	910	-210	30	-2	-10	2	2	-2	0	0	19	-17	55	-8	19	
X_{14}	910	-210	30	-2	-10	2	2	-2	0	0	19	-17	55	19	-8	
X_{15}	1092	-140	52	4	0	4	4	0	0	0	-42	30	-6	-15	-15	
X_{16}	1365	245	5	-27	5	1	1	-3	-1	-1	69	-3	60	15	15	
X_{17}	1365	-35	45	5	5	5	-3	-3	1	1	-12	87	-30	15	15	
X_{18}	1560	120	-40	-8	0	0	0	0	0	0	-60	12	30	-6	-6	
X_{19}	1560	120	-40	-8	0	0	0	0	0	0	-60	12	30	-6	-6	
X_{20}	1638	294	54	-10	6	2	2	-2	0	0	-63	18	45	-9	-9	
X_{21}	1820	140	-20	-4	0	4	4	0	0	0	-43	56	20	11	11	
X_{22}	2106	-414	66	-6	-14	6	-2	2	0	0	-81	0	81	0	0	
X_{23}	2184	56	24	-24	-4	0	0	-4	0	0	78	96	-21	24	24	
X_{24}	2457	189	21	33	-9	-7	5	3	-1	1	27	54	0	27	27	
X_{25}	2730	490	90	26	10	-2	-2	2	0	0	-24	-15	75	3	3	
X_{26}	2730	-70	10	-6	-10	6	6	-2	0	0	138	21	-15	-24	-24	
X_{27}	2835	315	75	3	-5	3	-5	3	-1	-1	-81	81	0	0	0	
X_{28}	4095	315	-45	-25	5	11	-1	1	-1	1	207	18	45	-9	-9	
X_{29}	4095	-525	75	7	5	-9	3	1	1	-1	-36	72	45	18	18	

Table 4, Part 1: Characters of $PS\Omega(7, 3)$

Order of centralizer	$2^9 \cdot 3^9 \cdot 5 \cdot 7 \cdot 13$																			
	1	2	2	2	2	4	2^6 \cdot 3^2 \cdot 5	4	4	4	8	8	2^4	3	25 \cdot 3^9	3	2^6 \cdot 3^7	3	2^4 \cdot 3^7 \cdot 5	3
$x_i^{(7)}$	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}	c_{11}	c_{12}	c_{13}	c_{14}	c_{15}					
x_{30}	4368	560	48	16	0	0	0	0	0	0	156	-24	66	-6	-6					
x_{31}	4536	-504	-24	24	-4	0	0	-4	0	0	162	0	81	0	0					
x_{32}	5265	225	-15	33	5	-3	-3	-3	-1	-1	162	81	0	0	0					
x_{33}	5460	420	100	20	0	4	4	0	0	0	33	96	-30	-21	-21					
x_{34}	5460	-700	100	-12	0	-4	-4	0	0	0	114	6	60	-21	-21					
x_{35}	5460	-140	-140	20	0	12	-4	0	0	0	-129	60	60	6	6					
x_{36}	5824	896	64	0	16	0	0	0	0	0	-8	-8	154	-8	-8					
x_{37}	5824	-896	64	0	-16	0	0	0	0	0	-8	-8	154	-8	-8					
x_{38}	6552	-504	-24	-8	4	0	0	4	0	0	234	72	45	18	18					
x_{39}	7020	540	60	12	0	4	4	0	0	0	-27	-54	0	-27	54					
x_{40}	7020	540	60	12	0	4	4	0	0	0	-27	-54	0	54	-27					
x_{41}	7280	-560	80	-16	0	0	0	0	0	0	-10	152	-10	-10	-10					
x_{42}	7280	-560	80	-16	0	0	0	0	0	0	-10	-64	-10	44	-10					
x_{43}	7280	-560	80	-16	0	0	0	0	0	0	-10	-64	-10	-10	44					
x_{44}	7371	819	51	-21	-1	-9	-1	-1	1	1	81	81	81	0	0					
x_{45}	8190	-210	30	-18	10	2	2	2	0	0	171	-45	-45	36	-45					
x_{46}	8190	-210	30	-18	10	2	2	2	0	0	171	-45	-45	-45	36					
x_{47}	11648	0	128	0	0	0	0	0	0	0	-16	-16	-124	-16	-16					
x_{48}	14742	630	102	6	-10	-6	-6	-2	0	0	162	-81	-81	0	0					
x_{49}	16380	-420	60	28	0	12	-4	0	0	0	99	-36	-90	18	18					
x_{50}	16640	1280	0	0	0	0	0	0	0	0	-208	-64	80	8	8					
x_{51}	16640	-1280	0	0	0	0	0	0	0	0	-208	-64	80	8	8					
x_{52}	17472	-896	-64	0	16	0	0	0	0	0	-24	-24	30	-24	-24					
x_{53}	17472	896	-64	0	-16	0	0	0	0	0	-24	-24	30	-24	-24					
x_{54}	17920	0	0	0	0	0	0	0	0	0	-224	64	-80	-8	-8					
x_{55}	17920	0	0	0	0	0	0	0	0	0	-224	64	-80	-8	-8					
x_{56}	19683	-729	-81	27	9	-9	3	-3	-1	1	0	0	0	0	0					
x_{57}	21840	560	-80	-48	0	0	0	0	0	0	-30	24	-30	24	24					
x_{58}	22113	189	-171	9	-9	-3	1	3	1	-1	243	0	0	0	0					

Table 4, Part 2: Characters of $PS\Omega(7, 3)$

el.	Order of centralizer	3	$2 \cdot 3^6$	3	$2^2 \cdot 3^6$	9	$2 \cdot 3^4$	9	$2^2 \cdot 3^4$	3 ³	3 ³	6	$2^5 \cdot 3^6$	6	$2^4 \cdot 3^5$	6	$2^4 \cdot 3^5$	6	$2^2 \cdot 3^4$	6	$2^5 \cdot 3^4$	6	$2^5 \cdot 3^3$	6	$2^5 \cdot 3^3$	6	$2^4 \cdot 3^3$
		(7)	c_{16}	c_{17}	c_{18}	c_{19}	c_{20}	c_{21}	c_{22}	c_{23}	c_{24}	c_{25}	c_{26}	c_{27}	c_{28}	c_{29}	c_{30}										
X ₁		1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
X ₂		-3	6	0	3	0	0	0	-7	2	-7	2	5	2	-1	1	1	1	1	1	1	1	1	1	1	1	1
X ₃		1	1	4	-2	1	1	6	-3	-3	-3	2	-1	5	-2	1	-2	1	1	1	1	1	1	1	1	1	1
X ₄		6	-3	0	3	0	0	0	-8	-8	1	1	-4	2	-1	4	1	1	1	1	1	1	1	1	1	1	1
X ₅		-3	6	3	0	0	0	0	2	2	11	2	6	0	3	2	-1	0	3	2	-1	1	1	1	1	1	1
X ₆		2	2	-1	5	-1	-1	16	7	7	-2	4	7	1	0	3	2	-1	1	0	3	2	-1	1	1	1	1
X ₇		6	-3	3	0	0	0	0	1	10	1	-1	-3	0	3	5	5	5	5	5	5	5	5	5	5	5	5
X ₈		-1	8	-1	-1	-1	2	-7	2	2	2	-7	2	2	2	1	-2	1	1	1	1	1	1	1	1	1	1
X ₉		-1	8	-1	-1	2	-1	-7	2	2	2	-7	2	2	2	1	-2	1	1	1	1	1	1	1	1	1	1
X ₁₀		3	3	3	3	0	0	0	-10	-10	-10	-1	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
X ₁₁		-3	-3	0	3	0	0	0	19	-8	1	1	-1	8	-1	-1	5	5	5	5	5	5	5	5	5	5	5
X ₁₂		9	9	0	0	0	0	0	6	-3	-3	-3	6	-3	-3	-3	10	1	1	1	1	1	1	1	1	1	1
X ₁₃		1	1	-2	4	-2	1	-21	-3	-3	-3	3	3	3	3	3	-5	1	1	1	1	1	1	1	1	1	1
X ₁₄		1	1	-2	4	1	-2	-21	-3	-3	-3	3	3	3	3	3	-5	1	1	1	1	1	1	1	1	1	1
X ₁₅		3	12	0	-3	0	0	22	4	-14	4	-2	-2	-2	-2	-2	-2	-2	-2	-2	-2	-2	-2	-2	-2	-2	
X ₁₆		6	6	0	3	0	0	0	29	11	2	2	5	5	5	5	-4	-3	-6	-3	-3	-3	-3	-3	-3	-3	
X ₁₇		-3	-3	3	0	0	0	0	-8	1	-8	1	0	3	6	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	
X ₁₈		3	3	0	-3	0	0	12	-6	-6	3	-4	8	2	4	-2	-2	-2	-2	-2	-2	-2	-2	-2	-2	-2	
X ₁₉		3	3	0	-3	0	0	12	-6	-6	3	-4	8	2	4	-2	-2	-2	-2	-2	-2	-2	-2	-2	-2	-2	
X ₂₀		0	9	0	0	0	0	0	-3	-12	15	-3	9	-6	-3	5	-1	1	1	1	1	1	1	1	1	1	
X ₂₁		-7	-7	-1	5	-1	-1	5	-4	-4	5	-11	-8	4	5	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	
X ₂₂		0	0	0	0	0	0	0	-9	18	-9	0	3	0	-3	3	3	3	3	3	3	3	3	3	3	3	
X ₂₃		6	6	3	0	0	0	0	2	2	11	2	6	0	3	-6	-3	-3	-3	-3	-3	-3	-3	-3	-3	-3	
X ₂₄		0	0	0	0	0	0	0	27	0	0	0	3	6	0	3	0	3	0	3	0	3	0	3	0	3	
X ₂₅		3	12	-3	0	0	0	4	-5	13	4	0	-3	3	-4	5	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	
X ₂₆		3	-6	0	-3	0	0	38	-7	11	2	10	1	1	1	6	3	3	3	3	3	3	3	3	3		
X ₂₇		0	0	0	0	0	0	0	-9	-9	18	0	3	-3	0	3	-6	-3	-3	-1	-1	-1	-1	-1	-1		
X ₂₈		9	0	0	0	0	0	0	-9	18	-9	0	-9	-6	-3	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1		
X ₂₉		0	9	0	0	0	0	0	-12	6	-21	-3	12	0	-3	4	-5	-5	-5	-5	-5	-5	-5	-5	-5		

Table 4, Part 3: Characters of $PS\Omega(7, 3)$

Order of centralizer el.	Order of centralizer el.														
	$2 \cdot 3^6$	$2^2 \cdot 3^6$	$2 \cdot 3^4$	$2^2 \cdot 3^4$	3^3	3^3	$2^5 \cdot 3^6$	$2^4 \cdot 3^5$	$2^4 \cdot 3^5$	$2^2 \cdot 3^4$	$2^5 \cdot 3^4$	$2^5 \cdot 3^3$	$2^4 \cdot 3^3$	$2^5 \cdot 3^3$	$2^4 \cdot 3^3$
$\chi_i^{(7)}$	c_{16}	c_{17}	c_{18}	c_{19}	c_{20}	c_{21}	c_{22}	c_{23}	c_{24}	c_{25}	c_{26}	c_{27}	c_{28}	c_{29}	c_{30}
χ_{30}	3	-6	-3	0	0	0	20	20	2	2	12	0	6	4	-2
χ_{31}	0	0	0	0	0	0	-18	-18	9	0	-6	0	-3	6	-3
χ_{32}	0	0	0	0	0	0	-18	9	-18	0	-6	-3	0	6	6
χ_{33}	-3	-3	0	-6	0	0	-39	6	6	-3	1	4	-2	-7	2
χ_{34}	6	6	-3	-3	0	0	2	-16	-16	2	10	-2	4	-6	0
χ_{35}	-3	15	-3	-3	0	0	-5	4	4	-5	-5	4	4	-1	-4
χ_{36}	-8	-8	1	1	1	1	32	-4	-4	-4	-8	4	-2	0	0
χ_{37}	-8	-8	1	1	1	1	-32	4	4	4	-8	4	-2	0	0
χ_{38}	9	0	0	0	0	0	-18	-18	9	0	-6	0	-3	-2	1
χ_{39}	0	0	0	0	0	0	-27	0	0	0	-3	-6	0	-3	0
χ_{40}	0	0	0	0	0	0	-27	0	0	0	-3	-6	0	-3	0
χ_{41}	-10	-10	-1	-1	-1	-1	34	-2	-2	-2	-10	-4	2	2	2
χ_{42}	-1	8	-1	-1	-1	2	34	-2	-2	-2	-10	-4	2	2	2
χ_{43}	-1	8	-1	-1	2	-1	34	-2	-2	-2	-10	-4	2	2	2
χ_{44}	0	0	0	0	0	0	9	9	9	0	-3	-3	-3	-3	-3
χ_{45}	0	-9	0	0	0	0	-21	-3	-3	-3	3	3	3	3	-3
χ_{46}	0	-9	0	0	0	0	-21	-3	-3	-3	3	3	3	3	-3
χ_{47}	2	20	2	2	-1	-1	0	0	0	0	-16	8	-4	0	0
χ_{48}	0	0	0	0	0	0	-18	9	9	0	-6	3	3	6	-3
χ_{49}	-9	-9	0	0	0	0	39	-6	-6	3	15	0	-6	-5	-2
χ_{50}	8	-10	2	-4	-1	-1	-16	-16	-16	2	0	0	0	0	0
χ_{51}	8	-10	2	-4	-1	-1	16	16	16	-2	0	0	0	0	0
χ_{52}	-6	12	3	3	0	0	-32	4	4	4	8	-4	2	0	0
χ_{53}	-6	12	3	3	0	0	32	-4	-4	-4	8	-4	2	0	0
χ_{54}	10	-8	-2	4	1	1	0	0	0	0	0	0	0	0	0
χ_{55}	10	-8	-2	4	1	1	0	0	0	0	0	0	0	0	0
χ_{56}	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{57}	-12	6	-3	-3	0	0	-34	2	2	2	10	4	-2	6	6
χ_{58}	0	0	0	0	0	0	27	0	0	0	-9	0	0	-9	0

Table 4, Part 4: Characters of $P\Omega(7, 3)$

Order of centralizer															
	$2^4 \cdot 3^3$	$2^6 \cdot 3^3$	$2^3 \cdot 3^3$	$2^3 \cdot 3^3$	$2 \cdot 3^3$	$2^2 \cdot 3^3$	$2^2 \cdot 3^3$	$2^3 \cdot 3^2$	$2^3 \cdot 3^2$	$2^3 \cdot 3$	$2^4 \cdot 3^2$	$2^4 \cdot 3^2$	$2^2 \cdot 3^2$	$2^2 \cdot 3^2$	$2^4 \cdot 3$
el.	6	6	6	6	6	6	12	12	12	12	12	12	12	12	12
$X_i^{(7)}$	c_{31}	c_{32}	c_{33}	c_{34}	c_{35}	c_{36}	c_{37}	c_{38}	c_{39}	c_{40}	c_{41}	c_{42}	c_{43}	c_{44}	c_{45}
X_1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
X_2	-2	-2	1	1	1	-2	-2	0	-3	-1	2	-1	-1	-1	-1
X_3	1	-5	-2	-2	1	1	1	-1	-1	-1	3	0	0	0	0
X_4	4	-2	1	1	-2	1	1	-2	1	-1	2	2	-1	-1	-2
X_5	2	8	2	2	-1	2	2	-2	1	1	0	0	0	0	0
X_6	3	3	-3	-3	0	0	0	1	1	-1	-1	2	-1	-1	2
X_7	2	8	2	2	2	-1	-1	2	-1	1	0	3	0	0	-1
X_8	-2	-2	-2	1	1	4	-2	0	0	0	-2	1	-2	1	1
X_9	-2	-2	1	-2	1	-2	4	0	0	0	-2	1	1	-2	1
X_{10}	2	-10	-1	-1	-1	-1	-1	0	0	0	-2	4	1	1	0
X_{11}	-4	-4	2	2	-1	-1	-1	2	-1	1	0	-3	0	0	1
X_{12}	1	1	1	1	1	1	1	-1	-1	-1	1	-2	1	1	2
X_{13}	1	7	4	-5	1	1	1	-1	-1	1	-1	-1	2	-1	-1
X_{14}	1	7	-5	4	1	1	1	-1	-1	1	-1	-1	-1	2	-1
X_{15}	4	-2	1	1	1	-2	-2	0	0	0	-2	-2	1	1	-2
X_{16}	3	-3	3	3	0	0	0	-1	2	0	1	1	1	1	1
X_{17}	5	-1	-1	-1	-1	-1	-1	-1	2	0	-1	-4	-1	-1	0
X_{18}	-2	4	-2	-2	1	1	1	0	0	0	0	0	0	0	0
X_{19}	-2	4	-2	-2	1	1	1	0	0	0	0	0	0	0	0
X_{20}	-4	2	-1	-1	2	-1	-1	0	3	1	2	-1	-1	-1	-1
X_{21}	-4	8	-1	-1	-1	-1	-1	0	0	0	4	1	1	1	1
X_{22}	-6	0	0	0	0	0	0	-2	1	-1	0	-3	0	0	1
X_{23}	-6	0	0	0	0	0	0	2	-1	-1	0	0	0	0	0
X_{24}	0	6	3	3	0	0	0	0	0	0	2	-1	-1	-1	-1
X_{25}	-1	-7	-1	-1	-1	2	2	1	1	-1	1	-2	1	1	-2
X_{26}	-3	-3	0	0	-3	0	0	-1	-1	1	-3	0	0	0	0
X_{27}	3	9	0	0	0	0	0	1	-2	0	-3	-3	0	0	1
X_{28}	2	2	-1	-1	-1	2	2	2	-1	1	2	-1	-1	-1	-1
X_{29}	-2	-8	-2	-2	-2	1	1	2	-1	1	0	0	0	0	0

Table 4, Part 5: Characters of $PS\Omega(7, 3)$

el.	Order of centralizer															
		C_{31}	C_{32}	C_{33}	C_{34}	C_{35}	C_{36}	C_{37}	C_{38}	C_{39}	C_{40}	C_{41}	C_{42}	C_{43}	C_{44}	
X_{30}	6	2 ⁴ .3 ³	6	2 ⁶ .3 ³	6	2 ³ .3 ³	6	2 ³ .3 ³	6	2 ² .3 ³	6	2 ² .3 ³	12	2 ³ .3 ²	12	2 ⁴ .3 ²
X_{31}	(7)	6	-8	-2	-2	1	-2	-2	0	2	-1	-1	0	0	0	0
X_{32}		6	0	0	0	0	0	0	-1	2	0	-3	0	0	0	0
X_{33}		-3	9	0	0	0	0	0	-1	2	0	4	1	1	1	1
X_{34}		2	8	-1	-1	-1	-1	-1	0	0	0	0	2	2	-1	-1
X_{35}		0	6	3	3	0	0	0	0	0	0	0	2	2	-1	2
X_{36}		0	-4	2	2	-1	-1	-1	0	0	0	0	3	0	0	-1
X_{37}		0	0	0	0	0	0	0	2	2	0	0	0	0	0	0
X_{38}		0	-2	-8	-2	-2	1	-2	-2	-2	1	1	0	0	0	0
X_{39}		0	-6	-3	6	0	0	0	0	0	0	-2	1	1	-2	1
X_{40}		0	-6	6	-3	0	0	0	0	0	0	-2	1	-2	1	1
X_{41}		2	-16	2	2	2	2	2	0	0	0	0	0	0	0	0
X_{42}		2	8	-4	2	-1	-4	2	0	0	0	0	0	0	0	0
X_{43}		2	8	2	-4	-1	2	-4	0	0	0	0	0	0	0	0
X_{44}		-3	9	0	0	0	0	0	-1	-1	-1	-3	3	0	0	-1
X_{45}		-3	3	0	3	0	3	-3	1	1	-1	-1	2	-1	-1	-1
X_{46}		-3	3	3	0	0	-3	3	1	1	-1	-1	-1	-1	2	-1
X_{47}		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{48}		-3	-9	0	0	0	0	0	-1	-1	1	3	0	0	0	0
X_{49}		-2	4	-2	-2	1	1	1	0	0	0	0	3	0	0	-1
X_{50}		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{51}		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{52}		0	0	0	0	0	0	0	-2	-2	0	0	0	0	0	0
X_{53}		0	0	0	0	0	0	0	2	2	0	0	0	0	0	0
X_{54}		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{55}		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{56}		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{57}		6	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{58}		0	0	0	0	0	0	0	0	0	0	-3	0	0	0	1

Table 4, Part 6: Characters of $PS\Omega(7, 3)$

$\chi_i^{(7)}$	el.	Order of centralizer																
		$2^2 \cdot 3^3$	$2^2 \cdot 3^3$	$2^3 \cdot 3$	$2^2 \cdot 3^2$	$2^3 \cdot 3^5$	5	10	$2^3 \cdot 5$	10	$2^2 \cdot 5$	20	15	$3 \cdot 5$	7	$2 \cdot 7$	14	13
c_{46}	c_{47}	c_{48}	c_{49}	c_{50}	c_{51}	c_{52}	c_{53}	c_{54}	c_{55}	c_{56}	c_{57}	c_{58}						
X_1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
X_2	-1	-1	2	-1	3	-1	1	-1	-1	0	1	1	0	0	0	0	0	0
X_3	0	0	0	2	1	1	-1	-1	1	0	0	0	0	0	0	0	0	0
X_4	1	1	-2	-1	0	0	0	0	0	0	0	0	0	0	0	0	1	1
X_5	2	2	-1	0	3	-1	1	-1	0	0	0	0	0	0	0	-1	-1	-1
X_6	1	1	1	1	2	2	0	0	-1	0	0	0	0	0	0	0	0	0
X_7	-2	-2	1	0	0	0	0	0	0	0	0	0	0	-1	-1	0	0	0
X_8	-1	-1	-1	-1	0	0	0	0	0	0	0	0	0	1	-1	0	0	0
X_9	-1	-1	-1	-1	0	0	0	0	0	0	0	0	0	1	-1	0	0	0
X_{10}	-1	-1	-1	-1	3	-1	-1	1	0	0	0	0	0	0	0	0	0	0
X_{11}	1	1	-2	-1	1	1	-1	-1	1	0	0	0	0	0	0	0	0	0
X_{12}	0	0	0	0	-1	-1	-1	-1	-1	0	0	0	0	0	0	0	0	0
X_{13}	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{14}	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{15}	1	1	-2	1	2	2	0	0	-1	0	0	0	0	0	0	0	0	0
X_{16}	-1	-1	2	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{17}	-2	-2	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{18}	ρ	$-\rho$	0	-1	0	0	0	0	0	0	0	0	0	-1	1	0	0	0
X_{19}	$-\rho$	ρ	0	-1	0	0	0	0	0	0	0	0	0	-1	1	0	0	0
X_{20}	0	0	0	0	3	-1	-1	1	0	0	0	0	0	0	0	0	0	0
X_{21}	-1	-1	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{22}	0	0	0	0	1	1	1	1	1	1	1	1	-1	-1	0	0	0	0
X_{23}	2	2	-1	0	-1	-1	1	1	-1	0	0	0	0	0	0	0	0	0
X_{24}	0	0	0	0	-3	1	-1	1	0	0	0	0	0	0	0	0	0	0
X_{25}	-2	-2	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{26}	-1	-1	2	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{27}	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1
X_{28}	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{29}	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Table 4, Part 7: Characters of $PS\Omega(7, 3)$

Order of el. $X_i^{(7)}$	centralizer																			
	$2^2 \cdot 3^3$	$2^2 \cdot 3^3$	$2 \cdot 3^3$	18	$2^2 \cdot 3^2$	5	$2^3 \cdot 3^5$	10	$2^3 \cdot 5$	10	$2^2 \cdot 5$	20	15	$3 \cdot 5$	7	$2 \cdot 7$	14	$2 \cdot 7$	13	13
X_{30}	2	2	-1	0	-2	-2	0	0	1	0	0	0	0	0	0	0	0	0	0	0
X_{31}	0	0	0	0	1	1	1	1	1	0	0	0	0	-1	-1	-1	-1	-1	-1	-1
X_{32}	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0
X_{33}	0	0	0	-2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{34}	-1	-1	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{35}	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{36}	-1	-1	-1	1	-1	-1	1	1	-1	0	0	0	0	0	0	0	0	0	0	0
X_{37}	1	1	1	1	-1	-1	-1	-1	-1	-1	-1	0	0	0	0	0	0	0	0	0
X_{38}	0	0	0	0	-3	1	1	-1	0	0	0	0	0	0	0	0	0	0	0	0
X_{39}	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0
X_{40}	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0
X_{41}	1	1	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{42}	1	1	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{43}	1	1	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{44}	0	0	0	0	1	1	-1	-1	1	0	0	0	0	0	0	0	0	0	0	0
X_{45}	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{46}	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{47}	0	0	0	2	-2	-2	0	0	0	1	0	0	0	0	0	0	0	0	0	0
X_{48}	0	0	0	0	2	2	0	0	0	-1	0	0	0	0	0	0	0	0	0	0
X_{49}	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{50}	2	2	2	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0
X_{51}	-2	-2	-2	0	0	0	0	0	0	0	0	0	1	1	1	0	0	0	0	0
X_{52}	1	1	1	-1	-3	1	-1	1	0	0	0	0	0	0	0	0	0	0	0	0
X_{53}	-1	-1	-1	-1	-3	1	1	-1	0	0	0	0	0	0	0	0	0	0	0	0
X_{54}	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	α	$-\alpha^*$	α	α
X_{55}	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	$-\alpha^*$	α	α	α
X_{56}	0	0	0	0	3	-1	1	-1	0	0	0	0	-1	-1	-1	-1	1	1	1	1
X_{57}	-1	-1	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{58}	0	0	0	0	3	-1	-1	1	0	0	0	0	0	0	0	0	0	0	0	0

Table 4, Part 8: Characters of $PS\Omega(7, 3)$

$x_i^{(22)}$	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}	c_{11}	c_{12}	c_{13}
x_1	1	1	1	1	1	1	1	1	1	1	1	1	1
x_2	78	-34	14	-2	0	0	1	1	-1	-1	1	1	1
x_3	429	77	45	13	0	0	0	0	0	0	2	0	-1
x_4	1001	-231	41	-7	0	0	0	0	0	0	0	0	0
x_5	1430	-154	86	6	0	0	0	0	0	0	2	0	-1
x_6	3003	539	59	-37	0	0	0	0	0	0	0	0	0
x_7	3080	615	136	40	-1	-1	0	0	0	0	0	0	0
x_8	10725	-715	165	-43	0	0	0	0	0	0	1	-1	1
x_9	13650	1330	210	114	0	0	-1	-1	-1	-1	0	0	0
x_{10}	30030	1694	526	62	0	0	0	0	0	0	0	0	0
x_{11}	32032	-2464	544	-32	0	0	0	0	0	0	0	0	0
x_{12}	43680	-4256	416	-32	0	0	-1	-1	1	1	0	0	0
x_{13}	45045	4389	309	133	0	0	0	0	0	0	0	0	0
x_{14}	48048	-1232	432	48	0	0	0	0	0	0	0	0	0
x_{15}	50050	-5390	450	-46	0	0	0	0	0	0	0	0	0
x_{16}	50050	770	130	-126	0	0	0	0	0	0	0	0	0
x_{17}	75075	1155	835	131	0	0	0	0	0	0	0	0	0
x_{18}	75075	7315	515	51	0	0	0	0	0	0	0	0	0
x_{19}	75075	-5005	-125	83	0	0	0	0	0	0	0	0	0
x_{20}	81081	3465	633	-87	0	0	0	0	0	0	0	0	0
x_{21}	114400	-8800	480	32	0	0	0	0	0	0	-1	-1	-1
x_{22}	138600	-9240	360	-24	$-\alpha$	α^*	0	0	0	0	0	0	0
x_{23}	138600	-9240	360	-24	α^*	$-\alpha$	0	0	0	0	0	0	0
x_{24}	150150	8470	70	54	0	0	0	0	0	0	0	0	0
x_{25}	205920	1056	864	160	0	0	0	0	0	0	1	-1	1
x_{26}	289575	12375	615	183	0	0	0	0	0	0	-1	-1	-1
x_{27}	300300	-7700	1420	-84	0	0	0	0	0	0	0	0	0
x_{28}	320320	14784	1344	192	0	0	0	0	0	0	0	0	0
x_{29}	360855	18711	1431	279	1	1	0	0	0	0	-2	0	1
x_{30}	370656	-15840	1248	-96	0	0	0	0	0	0	-1	1	-1
x_{31}	400400	6160	1040	16	0	0	0	0	0	0	0	0	0
x_{32}	400400	6160	1040	16	0	0	0	0	0	0	0	0	0
x_{33}	400400	-18480	-240	80	0	0	0	0	0	0	0	0	0

Table 5, Part 1: Characters of $M(22)$

$\chi_i^{(22)}$	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}	c_{11}	c_{12}	c_{13}
X34	400400	-18480	-240	80	0	0	0	0	0	0	0	0	0
X35	450450	6930	1170	-110	0	0	0	0	0	0	0	0	0
X36	450450	25410	210	-350	0	0	0	0	0	0	0	0	0
X37	576576	14784	576	-320	0	0	0	0	0	0	0	0	0
X38	577368	-21384	216	-72	-1	-1	0	0	0	0	1	1	1
X39	579150	-6930	1230	174	0	0	0	0	0	0	-2	0	1
X40	582400	-8960	-1280	256	0	0	β	$\bar{\beta}$	β	$\bar{\beta}$	0	0	0
X41	582400	-8960	-1280	256	0	0	$\bar{\beta}$	β	$\bar{\beta}$	β	0	0	0
X42	600600	9240	-1000	280	0	0	0	0	0	0	0	0	0
X43	600600	9240	-1000	280	0	0	0	0	0	0	0	0	0
X44	600600	21560	920	-136	0	0	0	0	0	0	0	0	0
X45	675675	10395	-165	411	0	0	0	0	0	0	0	0	0
X46	720720	-33264	1104	-112	0	0	0	0	0	0	0	0	0
X47	800800	-12320	800	-416	0	0	0	0	0	0	0	0	0
X48	852930	-29646	1026	18	0	0	1	1	-1	-1	1	-1	1
X49	938223	-2673	1647	207	0	0	0	0	0	0	-1	1	-1
X50	972972	-24948	1836	-180	0	0	0	0	0	0	0	0	0
X51	982800	15120	-240	-240	0	0	β	$\bar{\beta}$	$-\beta$	$-\bar{\beta}$	0	0	0
X52	982800	15120	-240	-240	0	0	$\bar{\beta}$	β	$-\bar{\beta}$	$-\beta$	0	0	0
X53	1201200	-30800	560	176	0	0	0	0	0	0	0	0	0
X54	1360800	30240	1440	288	-1	-1	1	1	1	1	0	0	0
X55	1372800	49280	640	128	0	0	0	0	0	0	2	0	-1
X56	1441792	0	0	1	1	1	0	0	0	0	2	0	-1
X57	1791153	-5103	-2511	81	0	0	1	1	1	1	0	0	0
X58	1876446	37422	-1890	-306	0	0	0	0	0	0	-2	0	1
X59	2027025	-24255	-1455	33	0	0	0	0	0	0	0	0	0
X60	2050048	0	2048	0	0	0	0	0	0	0	0	0	0
X61	2316600	-43560	-840	24	0	0	0	0	0	0	-1	1	-1
X62	2402400	12320	-160	160	0	0	0	0	0	0	0	0	0
X63	2555904	32768	0	0	0	0	-1	-1	-1	-1	1	1	1
X64	2555904	-32768	0	0	0	0	-1	-1	1	1	1	-1	1
X65	2729376	7776	-864	-288	0	0	1	1	-1	-1	-1	-1	-1

Table 5, Part 2: Characters of $M(22)$

$\chi_i^{(22)}$	c_{14}	c_{15}	c_{16}	c_{17}	c_{18}	c_{19}	c_{20}	c_{21}	c_{22}	c_{23}	c_{24}	c_{25}	c_{26}
χ_1	1	1	1	1	1	1	1	1	1	1	1	1	1
χ_2	3	1	-1	0	-1	-2	15	-7	-1	1	-3	3	-1
χ_3	4	2	0	1	0	-1	6	14	6	-2	2	-2	2
χ_4	1	-1	1	1	-1	-1	56	-6	8	2	-2	4	0
χ_5	5	1	1	-1	-1	1	-1	-19	-1	-3	-3	-1	-1
χ_6	3	-1	-1	0	1	2	105	17	-7	-7	5	5	1
χ_7	5	1	1	-1	-1	1	119	31	7	7	3	3	-1
χ_8	0	0	0	0	0	0	15	5	15	5	-3	-1	-1
χ_9	0	0	0	0	0	0	105	25	9	9	1	1	1
χ_{10}	5	-1	1	-1	1	-1	-21	29	-5	5	5	-1	-1
χ_{11}	7	1	-1	1	1	1	91	-79	-5	1	-3	-5	-1
χ_{12}	5	-1	1	-1	1	-1	399	-71	-1	1	-3	3	-1
χ_{13}	-5	-1	-1	1	1	-1	441	-21	9	19	-1	5	1
χ_{14}	-2	-2	2	1	0	1	-84	-44	12	-12	0	-4	0
χ_{15}	0	0	0	0	0	0	595	-35	3	5	1	7	3
χ_{16}	0	0	0	0	0	0	-35	5	13	-3	1	1	-3
χ_{17}	0	0	0	0	0	0	-210	30	-2	-10	-2	2	2
χ_{18}	0	0	0	0	0	0	735	25	-1	9	1	7	-1
χ_{19}	0	0	0	0	0	0	420	-10	4	-10	-6	4	0
χ_{20}	6	0	-2	0	0	0	0	90	0	-6	2	0	0
χ_{21}	0	0	0	0	0	0	685	-25	-3	-1	-1	1	1
χ_{22}	0	0	0	0	0	0	630	30	6	6	2	2	-2
χ_{23}	0	0	0	0	0	0	630	30	6	6	2	2	-2
χ_{24}	0	0	0	0	0	0	525	55	13	-9	3	5	1
χ_{25}	-5	1	-1	1	-1	1	-279	-69	9	-5	3	1	1
χ_{26}	0	0	0	0	0	0	405	-45	21	3	-1	-3	1
χ_{27}	0	0	0	0	0	0	-210	-50	-2	6	-2	2	2
χ_{28}	-5	-1	-1	1	1	-1	406	114	6	-6	-2	-6	-2
χ_{29}	5	1	1	-1	-1	1	729	81	9	9	-3	-3	1
χ_{30}	6	0	-2	0	0	0	405	-45	21	3	-1	-3	1
χ_{31}	0	0	0	0	0	0	-280	40	8	-8	0	0	0
χ_{32}	0	0	0	0	0	0	-280	40	8	-8	0	0	0
χ_{33}	0	0	0	0	0	0	980	60	-12	-4	0	4	0

Table 5, Part 3: Characters of $M(22)$

$X_i^{(22)}$	C_{14}	C_{15}	C_{16}	C_{17}	C_{18}	C_{19}	C_{20}	C_{21}	C_{22}	C_{23}	C_{24}	C_{25}	C_{26}
X_{34}	0	0	0	0	0	0	980	60	-12	-4	0	4	0
X_{35}	0	0	0	0	0	0	-315	45	21	-11	1	1	-3
X_{36}	0	0	0	0	0	0	1575	-15	-9	-23	-3	3	-1
X_{37}	1	-1	1	1	-1	-1	126	114	-18	10	2	-6	2
X_{38}	-7	1	1	-1	1	1	729	81	9	9	-3	-3	1
X_{39}	0	0	0	0	0	0	-405	-45	-21	3	-1	3	-1
X_{40}	0	0	0	0	0	0	280	40	-8	-8	0	0	0
X_{41}	0	0	0	0	0	0	280	40	-8	-8	0	0	0
X_{42}	0	0	0	0	0	0	210	-30	2	10	2	-2	-2
X_{43}	0	0	0	0	0	0	210	-30	2	10	2	-2	-2
X_{44}	0	0	0	0	0	0	525	5	-19	5	1	-3	1
X_{45}	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{46}	-5	1	-1	1	-1	1	1386	-54	-6	2	2	-2	-2
X_{47}	0	0	0	0	0	0	-245	-35	11	13	1	3	-1
X_{48}	5	-1	1	-1	1	-1	729	-81	9	-9	3	-3	1
X_{49}	-2	2	2	1	0	-1	-729	-81	-9	-9	3	3	-1
X_{50}	-3	-3	1	0	-1	0	0	0	0	0	0	0	0
X_{51}	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{52}	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{53}	0	0	0	0	0	0	420	-20	-28	-4	0	-4	0
X_{54}	0	0	0	0	0	0	0	0	0	0	0	0	0
X_{55}	0	0	0	0	0	0	1560	-40	-8	8	0	0	0
X_{56}	-8	0	0	-2	0	0	-512	0	0	0	0	0	0
X_{57}	3	-3	-1	0	-1	0	0	0	0	0	0	0	0
X_{58}	-4	2	0	-1	0	-1	729	-81	9	-9	3	-3	1
X_{59}	0	0	0	0	0	0	0	-90	0	6	-2	0	0
X_{60}	-2	0	-2	-2	0	0	-1232	0	-16	0	0	0	0
X_{61}	0	0	0	0	0	0	405	45	21	-3	1	-3	1
X_{62}	0	0	0	0	0	0	-735	35	17	-5	-1	5	1
X_{63}	4	-2	0	1	0	1	-384	-64	0	0	0	0	0
X_{64}	4	2	0	1	0	-1	-384	64	0	0	0	0	0
X_{65}	1	1	1	1	1	1	-729	81	-9	9	-3	3	-1

Table 5, Part 4: Characters of $M(22)$

$\chi_i^{(22)}$	C_{27}	C_{28}	C_{29}	C_{30}	C_{31}	C_{32}	C_{33}	C_{34}	C_{35}	C_{36}	C_{37}	C_{38}	C_{39}
χ_1	1	1	1	1	1	1	1	1	1	1	1	1	1
χ_2	-3	1	-1	-3	-7	5	1	-3	1	-1	-1	0	2
χ_3	-2	-2	-2	24	-4	0	4	4	0	2	2	3	-1
χ_4	-2	-2	0	29	-15	5	-7	1	-3	-1	-1	2	0
χ_5	5	-1	1	-28	8	-4	0	-4	0	-2	-2	-1	-1
χ_6	5	-1	-1	6	26	14	2	2	-2	0	0	0	2
χ_7	3	1	1	2	22	10	-2	6	2	0	0	-1	1
χ_8	5	3	1	114	14	-6	-10	2	-2	0	0	3	-1
χ_9	1	1	1	123	7	3	15	-5	-1	1	1	3	1
χ_{10}	-7	1	-1	-102	-34	-14	-10	2	-2	0	0	-3	-1
χ_{11}	1	-1	1	-44	20	4	4	-8	0	0	0	1	-1
χ_{12}	-3	1	-1	-60	-44	20	4	0	0	0	0	3	1
χ_{13}	-1	-1	1	90	42	-6	10	2	2	-2	-2	0	0
χ_{14}	-4	0	0	258	10	18	-6	2	2	-2	-2	3	1
χ_{15}	1	1	-1	73	-71	9	-7	1	1	1	1	-2	-2
χ_{16}	1	-1	-1	235	-13	-5	3	-5	3	3	3	1	-1
χ_{17}	2	0	0	150	-6	-2	2	2	-2	0	0	0	0
χ_{18}	1	-1	1	-93	79	11	-9	-5	-1	1	1	0	-2
χ_{19}	-2	0	2	-12	-64	28	8	4	0	2	2	-3	-1
χ_{20}	-6	0	2	162	-18	-6	6	6	2	0	0	0	0
χ_{21}	-5	-1	1	28	-52	12	-4	-8	0	0	0	-2	2
χ_{22}	2	0	0	-153	-33	-9	15	-1	-1	-1	-1	0	0
χ_{23}	2	0	0	-153	-33	-9	15	-1	-1	-1	-1	0	0
χ_{24}	-1	1	-1	57	73	25	9	-7	1	-3	-3	0	-2
χ_{25}	-5	1	-1	-144	-24	0	-8	-8	0	0	0	0	0
χ_{26}	3	1	-1	162	-18	-6	6	6	2	0	0	0	0
χ_{27}	2	0	0	-291	49	-11	9	5	1	-1	-1	-3	1
χ_{28}	6	0	0	-116	-12	12	-12	0	0	0	0	-2	0
χ_{29}	-3	-1	-1	0	0	0	0	0	0	0	0	0	0
χ_{30}	3	1	-1	324	36	-12	-12	0	0	0	0	0	0
χ_{31}	0	0	0	-307	-23	5	1	-3	1	7	-5	-1	1
χ_{32}	0	0	0	-307	-23	5	1	-3	1	-5	7	-1	1
χ_{33}	4	0	0	98	-66	-6	-10	-2	2	0	0	2	0

Table 5, Part 5: Characters of $M(22)$

$\chi_i^{(22)}$	C_{27}	C_{28}	C_{29}	C_{30}	C_{31}	C_{32}	C_{33}	C_{34}	C_{35}	C_{36}	C_{37}	C_{38}	C_{39}
χ_{34}	4	0	0	98	-66	-6	-10	-2	2	0	0	2	0
χ_{35}	1	-1	-1	-72	-36	0	4	4	0	-2	-2	0	0
χ_{36}	-3	1	-1	171	111	3	7	3	-1	1	1	0	0
χ_{37}	6	0	0	180	-12	36	4	0	0	0	0	0	0
χ_{38}	-3	-1	-1	0	0	0	0	0	0	0	0	0	0
χ_{39}	3	-1	-1	324	36	-12	-12	0	0	0	0	0	0
χ_{40}	0	0	0	172	4	-20	4	0	0	0	0	1	1
χ_{41}	0	0	0	172	4	-20	4	0	0	0	0	1	1
χ_{42}	-2	0	0	-15	33	17	1	1	1	1	1	0	0
χ_{43}	-2	0	0	-15	33	17	1	1	1	1	1	0	0
χ_{44}	-3	1	1	-96	-40	-16	8	0	0	0	0	3	-1
χ_{45}	0	0	0	135	27	15	3	3	-1	1	1	0	0
χ_{46}	-2	0	0	-18	-54	6	2	10	-2	0	0	0	0
χ_{47}	-3	-1	1	520	-8	8	-8	0	0	0	0	1	1
χ_{48}	3	-1	1	0	0	0	0	0	0	0	0	0	0
χ_{49}	3	1	1	0	0	0	0	0	0	0	0	0	0
χ_{50}	0	0	0	-243	81	-27	9	-3	1	3	3	0	0
χ_{51}	0	0	0	-135	-27	-15	-3	-3	1	-1	-1	0	0
χ_{52}	0	0	0	-135	-27	-15	-3	-3	1	-1	-1	0	0
χ_{53}	-4	0	0	-30	34	2	2	2	2	-2	-2	0	-2
χ_{54}	0	0	0	486	-54	-18	18	-6	-2	0	0	0	0
χ_{55}	0	0	0	-312	32	-8	-16	0	0	0	0	0	2
χ_{56}	0	0	0	640	0	0	0	0	0	0	0	-2	0
χ_{57}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{58}	3	-1	1	0	0	0	0	0	0	0	0	0	0
χ_{59}	6	0	-2	-324	-36	12	12	0	0	0	0	0	0
χ_{60}	0	0	0	-224	0	32	0	0	0	0	0	4	0
χ_{61}	-3	1	1	-162	18	6	-6	-6	-2	0	0	0	0
χ_{62}	-1	-1	1	-384	8	-16	-8	8	0	0	0	3	-1
χ_{63}	0	0	0	192	-64	0	0	0	0	0	0	-3	-1
χ_{64}	0	0	0	192	64	0	0	0	0	0	0	-3	-1
χ_{65}	-3	1	-1	0	0	0	0	0	0	0	0	0	0

Table 5, Part 6: Characters of $M(22)$

$\chi_i^{(22)}$	C_{40}	C_{41}	C_{42}	C_{43}	C_{44}	C_{45}	C_{46}	C_{47}	C_{48}	C_{49}	C_{50}	C_{51}	C_{52}
χ_1	1	1	1	1	1	1	1	1	1	1	1	1	1
χ_2	3	-1	-1	-1	0	-3	1	-1	6	2	2	-2	-2
χ_3	0	2	2	0	0	-3	1	-1	15	5	3	7	1
χ_4	2	0	0	2	-1	2	2	2	2	-6	2	2	2
χ_5	-1	-1	-1	-1	2	-1	3	1	26	8	2	-6	0
χ_6	3	-1	-1	-1	0	6	2	0	15	-1	-1	-1	-1
χ_7	5	1	1	1	-1	2	-2	0	20	4	4	4	4
χ_8	0	2	2	0	0	6	2	0	24	-4	0	8	-4
χ_9	0	-2	-2	0	0	15	3	1	33	7	-3	9	3
χ_{10}	-3	-1	-1	1	0	6	2	0	60	2	4	-4	2
χ_{11}	1	-1	-1	1	-2	10	-2	0	64	2	4	-8	-2
χ_{12}	3	1	1	-1	0	-6	-2	0	48	10	-4	-8	-2
χ_{13}	0	0	0	0	0	9	1	1	-18	6	6	-2	-2
χ_{14}	0	-2	-2	0	0	-12	0	-2	6	-8	6	6	0
χ_{15}	4	-2	-2	0	1	19	-1	1	10	-8	6	2	-4
χ_{16}	1	-1	-1	1	1	-8	0	0	19	5	-5	3	-3
χ_{17}	-6	0	0	-2	0	-12	-4	0	51	3	7	11	-1
χ_{18}	3	1	1	-1	0	-12	0	-2	-3	-11	5	-3	-3
χ_{19}	-3	-1	-1	1	0	15	-1	-1	42	-10	-2	2	2
χ_{20}	0	0	0	0	0	0	0	0	81	9	-3	9	-3
χ_{21}	4	2	2	0	1	-26	2	0	-8	2	0	8	2
χ_{22}	0	0	0	0	0	9	-3	-1	-45	3	3	3	3
χ_{23}	0	0	0	0	0	9	-3	-1	-45	3	3	3	3
χ_{24}	-3	1	1	1	0	-24	0	0	48	-8	-8	0	0
χ_{25}	0	0	0	0	0	18	-2	0	72	12	0	-8	4
χ_{26}	0	0	0	0	0	0	0	0	-81	9	3	-9	-3
χ_{27}	-3	1	1	1	0	-21	3	-1	114	4	-2	-6	0
χ_{28}	4	0	0	0	1	-8	0	0	64	6	0	0	6
χ_{29}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{30}	0	0	0	0	0	0	0	0	0	-18	0	0	6
χ_{31}	-1	1	1	-1	-1	17	1	1	-10	-14	2	-2	-2
χ_{32}	-1	1	1	-1	-1	17	1	1	-10	-14	2	-2	-2
χ_{33}	-4	0	0	0	-1	-10	2	0	-28	6	0	-4	2

Table 5, Part 7: Characters of $M(22)$

$\chi_i^{(22)}$	C_{40}	C_{41}	C_{42}	C_{43}	C_{44}	C_{45}	C_{46}	C_{47}	C_{48}	C_{49}	C_{50}	C_{51}	C_{52}
χ_{34}	-4	0	0	0	-1	-10	2	0	-28	6	0	-4	2
χ_{35}	0	0	0	0	0	9	1	1	9	-9	-3	1	-5
χ_{36}	0	0	0	0	0	9	1	1	-18	12	6	-2	4
χ_{37}	0	0	0	0	0	18	-2	0	72	6	0	-8	-2
χ_{38}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{39}	0	0	0	0	0	0	0	0	81	9	-3	9	-3
χ_{40}	1	1	1	1	1	10	-2	0	64	-14	4	-8	-2
χ_{41}	1	1	1	1	1	10	-2	0	64	-14	4	-8	-2
χ_{42}	-3	ρ	$-\rho$	-1	0	-15	1	1	57	-3	5	1	1
χ_{43}	-3	$-\rho$	ρ	-1	0	-15	1	1	57	-3	5	1	1
χ_{44}	3	-1	-1	-1	0	-42	2	0	12	-22	-4	-4	2
χ_{45}	0	0	0	0	0	54	6	-2	-54	0	-6	-6	0
χ_{46}	0	0	0	0	0	-18	2	0	36	0	0	-4	-4
χ_{47}	-5	1	1	-1	1	34	-2	0	16	-8	-4	-8	4
χ_{48}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{49}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{50}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{51}	0	0	0	0	0	27	3	-1	54	0	6	6	0
χ_{52}	0	0	0	0	0	27	3	-1	54	0	6	6	0
χ_{53}	3	1	1	-1	0	51	-1	1	-48	-2	-4	8	2
χ_{54}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{55}	-3	-1	-1	1	0	12	-4	0	-24	-4	-8	8	-4
χ_{56}	4	0	0	0	-2	-8	0	0	64	0	0	0	0
χ_{57}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{58}	0	0	0	0	0	0	0	0	0	0	0	0	0
χ_{59}	0	0	0	0	0	0	0	0	81	-9	-3	9	3
χ_{60}	-2	0	0	2	1	-8	0	0	-80	0	8	0	0
χ_{61}	0	0	0	0	0	0	0	0	0	18	0	0	-6
χ_{62}	3	-1	-1	-1	0	-6	-2	0	48	8	-4	-8	4
χ_{63}	0	2	2	0	0	-24	0	0	-96	8	0	0	0
χ_{64}	0	-2	-2	0	0	-24	0	0	-96	-8	0	0	0
χ_{65}	0	0	0	0	0	0	0	0	0	0	0	0	0

Table 5, Part 8: Characters of $M(22)$

$x_i^{(2)}$	C_{53}	C_{54}	C_{55}	C_{56}	C_{57}	C_{58}	C_{59}	C_{60}	C_{61}	C_{62}	C_{63}	C_{64}	C_{65}
x_1	1	1	1	1	1	1	1	1	1	1	1	1	1
x_2	0	2	-6	2	2	0	6	-2	2	-2	2	0	0
x_3	-1	-1	5	5	5	1	13	-3	1	1	1	-1	-1
x_4	-2	2	-11	-3	5	-1	1	9	-3	1	1	1	1
x_5	0	-2	-6	2	10	0	14	6	-2	2	2	0	0
x_6	-1	3	11	-5	3	-1	11	-5	-1	-1	3	-1	-1
x_7	0	0	24	8	0	0	24	8	4	4	0	0	0
x_8	0	0	-15	-7	9	-1	29	-11	1	-3	1	-1	-1
x_9	1	1	10	10	10	2	-14	2	-2	-2	-2	0	0
x_{10}	2	0	26	2	18	0	38	-2	2	-2	2	0	0
x_{11}	0	0	-24	8	0	0	64	0	4	-4	0	0	0
x_{12}	0	0	-24	8	0	0	0	0	-4	4	0	0	0
x_{13}	2	-2	41	1	1	-1	29	5	1	5	1	-1	-1
x_{14}	0	-2	0	0	16	0	-16	-16	0	0	0	0	0
x_{15}	-2	-2	-50	6	-2	0	10	-14	2	-2	-2	0	0
x_{16}	1	3	10	-6	18	-2	-14	18	2	2	-2	0	0
x_{17}	1	3	-5	11	3	-1	83	19	3	3	-1	1	1
x_{18}	1	1	55	-1	7	1	-5	-13	-5	-1	-1	1	1
x_{19}	0	2	15	-9	-1	1	-5	3	-1	3	3	-1	-1
x_{20}	-1	-3	5	-3	-3	-1	33	-7	-7	-3	1	1	1
x_{21}	2	0	-40	-8	0	0	64	0	4	-4	0	0	0
x_{22}	-1	-1	-40	-8	8	0	8	8	0	0	0	0	0
x_{23}	-1	-1	-40	-8	8	0	8	8	0	0	0	0	0
x_{24}	0	0	-30	10	-6	0	-34	22	2	-2	2	0	0
x_{25}	0	0	24	-8	0	0	64	0	-4	4	0	0	0
x_{26}	-1	3	35	-5	3	1	15	23	-1	-5	3	1	1
x_{27}	-2	2	-20	-4	20	0	-4	-20	0	0	-4	0	0
x_{28}	-2	0	16	16	0	0	0	0	0	0	0	0	0
x_{29}	0	0	39	7	-9	-1	-9	-9	-1	-1	-1	-1	-1
x_{30}	2	0	-40	-8	0	0	0	0	-4	4	0	0	0
x_{31}	0	-2	0	0	16	0	-48	16	0	0	0	0	0
x_{32}	0	-2	0	0	16	0	-48	16	0	0	0	0	0
x_{33}	0	0	0	0	0	0	16	-16	0	0	0	σ	$-\sigma$

Table 5, Part 9: Characters of $M(22)$

$\chi_i^{(22)}$	C_{53}	C_{54}	C_{55}	C_{56}	C_{57}	C_{58}	C_{59}	C_{60}	C_{61}	C_{62}	C_{63}	C_{64}	C_{65}
X34	0	0	0	0	0	0	16	-16	0	0	0	-0	0
X35	1	1	10	-6	-14	2	130	-30	2	2	-2	0	0
X36	0	-2	30	-10	-2	0	-6	2	2	-2	-2	0	0
X37	2	0	-16	-16	0	0	0	0	0	0	0	0	0
X38	0	0	-24	-8	0	0	72	24	-4	-4	0	0	0
X39	-1	-3	-10	-10	6	2	-18	30	2	2	2	0	0
X40	0	0	0	0	0	0	0	0	0	0	0	0	0
X41	0	0	0	0	0	0	0	0	0	0	0	0	0
X42	-1	1	-40	-8	-8	0	-8	-8	0	0	0	0	0
X43	-1	1	-40	-8	-8	0	-8	-8	0	0	0	0	0
X44	-2	0	40	-8	0	0	72	24	4	4	0	0	0
X45	0	-2	-45	3	-5	-1	75	11	3	3	-1	1	1
X46	2	0	-16	16	0	0	-80	16	0	0	0	0	0
X47	-2	0	40	8	0	0	0	0	4	-4	0	0	0
X48	0	0	6	-2	-18	0	-54	18	-2	2	-2	0	0
X49	0	0	15	-1	-9	-1	63	15	-5	-5	-1	-1	-1
X50	0	0	-36	12	-12	0	60	-20	0	0	4	0	0
X51	0	2	0	0	-16	0	-48	16	0	0	0	0	0
X52	0	2	0	0	-16	0	-48	16	0	0	0	0	0
X53	0	4	0	0	16	0	-16	-16	0	0	0	0	0
X54	0	0	0	0	0	0	-96	-32	0	0	0	0	0
X55	0	0	0	0	0	0	0	0	0	0	0	0	0
X56	0	0	0	0	0	0	0	0	0	0	0	0	0
X57	0	0	9	9	9	1	81	33	-3	-3	-3	-1	-1
X58	0	0	-30	10	18	0	54	-18	-2	2	2	0	0
X59	1	-3	85	-3	-3	-1	9	-15	1	-3	1	1	1
X60	0	0	0	0	0	0	0	0	0	0	0	0	0
X61	-2	0	40	-8	0	0	-24	-8	4	4	0	0	0
X62	2	0	-40	-8	0	0	-64	0	4	-4	0	0	0
X63	0	0	0	0	0	0	0	0	0	0	0	0	0
X64	0	0	0	0	0	0	0	0	0	0	0	0	0
X65	0	0	-24	8	0	0	0	0	-4	4	0	0	0

Table 5, Part 10: Characters of $M(22)$

	el.	Order of centralizer		el.	Order of centralizer
C_1	1	$ M(22) $	C_{34}	12	$2^5 \cdot 3^3$
C_2	2	$2^{16} \cdot 3^6 \cdot 5 \cdot 7 \cdot 11$	C_{35}	12	$2^5 \cdot 3$
C_3	2	$2^{17} \cdot 3^4 \cdot 5$	C_{36}	12	$2^4 \cdot 3^2$
C_4	2	$2^{16} \cdot 3^3$	C_{37}	12	$2^4 \cdot 3^2$
C_5	13	13	C_{38}	9	$2 \cdot 3^4$
C_6	13	13	C_{39}	18	$2 \cdot 3^3$
C_7	11	$2 \cdot 11$	C_{40}	9	$2^2 \cdot 3^4$
C_8	11	$2 \cdot 11$	C_{41}	18	$2^2 \cdot 3^3$
C_9	22	$2 \cdot 11$	C_{42}	18	$2^2 \cdot 3^3$
C_{10}	22	$2 \cdot 11$	C_{43}	18	$2^2 \cdot 3^2$
C_{11}	7	$2 \cdot 3 \cdot 7$	C_{44}	9	3^3
C_{12}	14	2.7	C_{45}	3	$2^3 \cdot 3^7$
C_{13}	21	3.7	C_{46}	6	$2^3 \cdot 3^3$
C_{14}	5	$2^3 \cdot 3 \cdot 5^2$	C_{47}	12	$2^2 \cdot 3^2$
C_{15}	10	$2^2 \cdot 3 \cdot 5$	C_{48}	3	$2^6 \cdot 3^7$
C_{16}	10	$2^3 \cdot 5$	C_{49}	6	$2^4 \cdot 3^5$
C_{17}	15	$2 \cdot 3 \cdot 5$	C_{50}	6	$2^5 \cdot 3^3$
C_{18}	20	$2^2 \cdot 5$	C_{51}	6	$2^6 \cdot 3^3$
C_{19}	30	$2 \cdot 3 \cdot 5$	C_{52}	6	$2^4 \cdot 3^3$
C_{20}	3	$2^8 \cdot 3^7 \cdot 5 \cdot 7$	C_{53}	12	$2^3 \cdot 3^2$
C_{21}	6	$2^7 \cdot 3^5 \cdot 5$	C_{54}	12	$2^4 \cdot 3^2$
C_{22}	6	$2^8 \cdot 3^3$	C_{55}	4	$2^{10} \cdot 3^2 \cdot 5$
C_{23}	6	$2^7 \cdot 3^3$	C_{56}	4	$2^{10} \cdot 3$
C_{24}	12	$2^5 \cdot 3^2$	C_{57}	4	$2^9 \cdot 3^2$
C_{25}	12	$2^6 \cdot 3^2$	C_{58}	8	2^5
C_{26}	12	$2^5 \cdot 3$	C_{59}	4	$2^{12} \cdot 3^3$
C_{27}	12	$2^6 \cdot 3^2$	C_{60}	4	$2^{12} \cdot 3$
C_{28}	24	$2^4 \cdot 3$	C_{61}	8	$2^7 \cdot 3$
C_{29}	24	$2^4 \cdot 3$	C_{62}	8	$2^7 \cdot 3$
C_{30}	3	$2^7 \cdot 3^9$	C_{63}	8	2^7
C_{31}	6	$2^7 \cdot 3^6$	C_{64}	16	2^5
C_{32}	6	$2^7 \cdot 3^4$	C_{65}	16	2^5
C_{33}	6	$2^7 \cdot 3^3$			

Table 5, Part 11: Conjugacy classes of $M(22)$